

Lock-free by Example

(one very complicated example)

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C++Now, 2015

Guide to Threaded Coding

Guide to Threaded Coding

Use Locks

Guide to Threaded Coding

1. Forget what you learned in Kindergarten
(ie *stop Sharing*)
2. Use Locks
3. Measure
4. Measure
5. Change your Algorithm
6. GOTO 1

∞. **Lock-free**

Lock-free coding is the last thing you want to do.

Guide to Threaded Coding

1. Forget what you learned in Kindergarten
(ie *stop Sharing*)
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∞ . **Lock-free**

$\infty+1$. **Measure. Measure.**

Lock-free coding is the last thing you want to do.

Guide to Threaded Coding

Don't Share
Use Locks

NOTE:

CAS = compare_exchange (_weak or _strong)



NOTE:

CAS = compare_exchange

Not my coding style/structure

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CAS = compare_exchange

Not my coding style/structure

Remember to lower the audience's expectations:

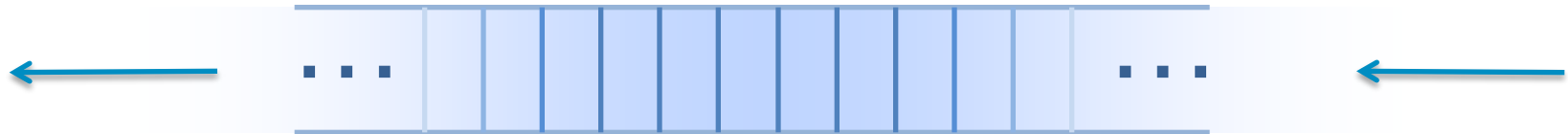
NOTE:

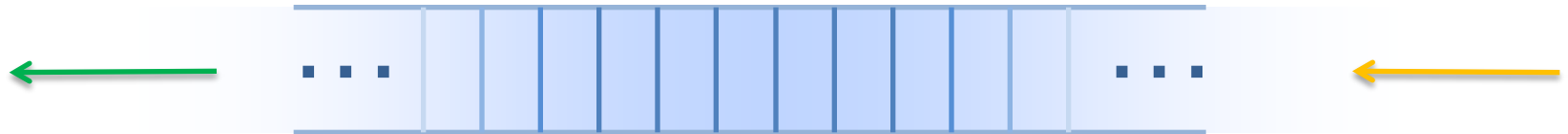
CAS = compare_exchange

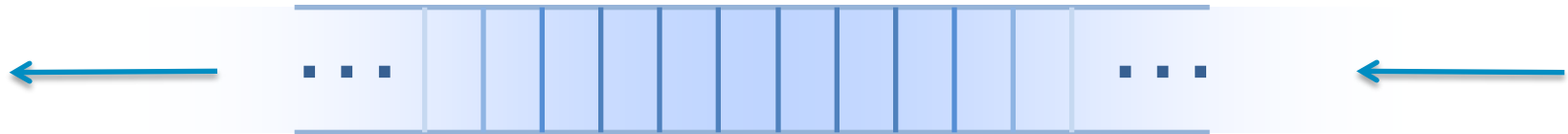
Not my coding style/structure

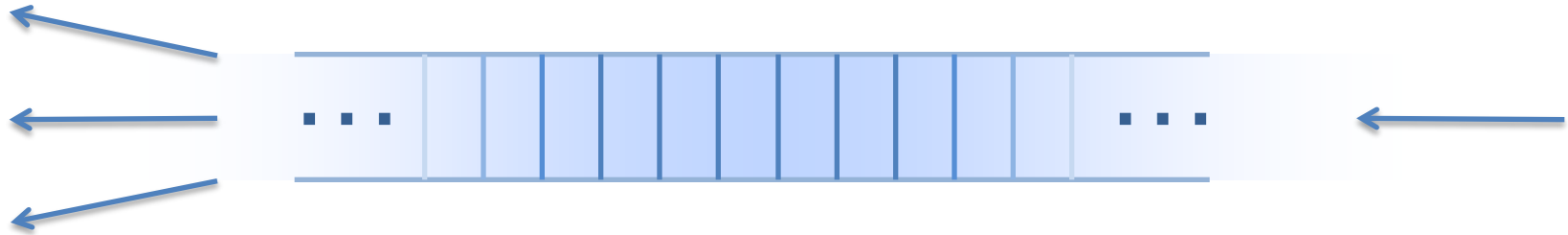
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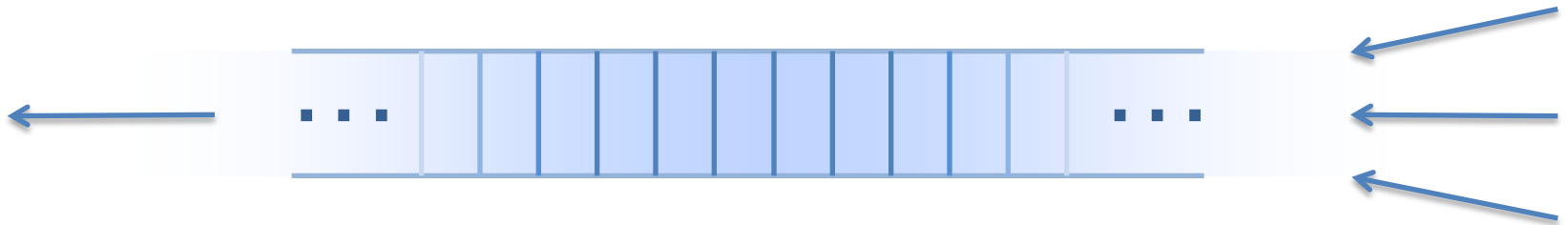
I'm not an expert.

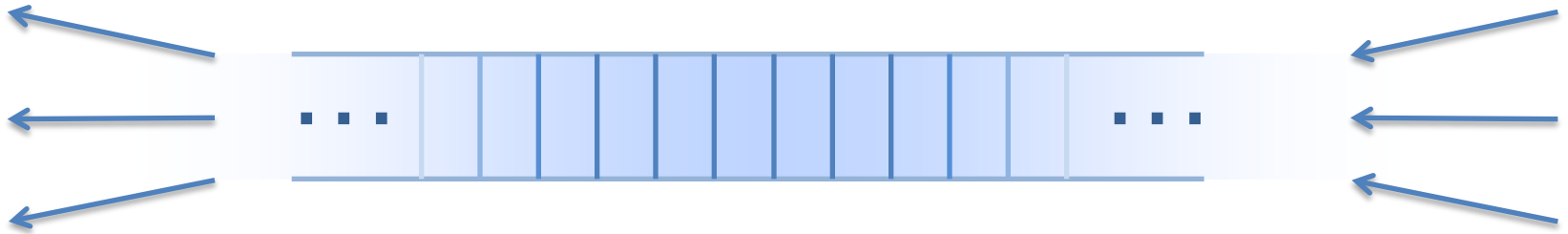




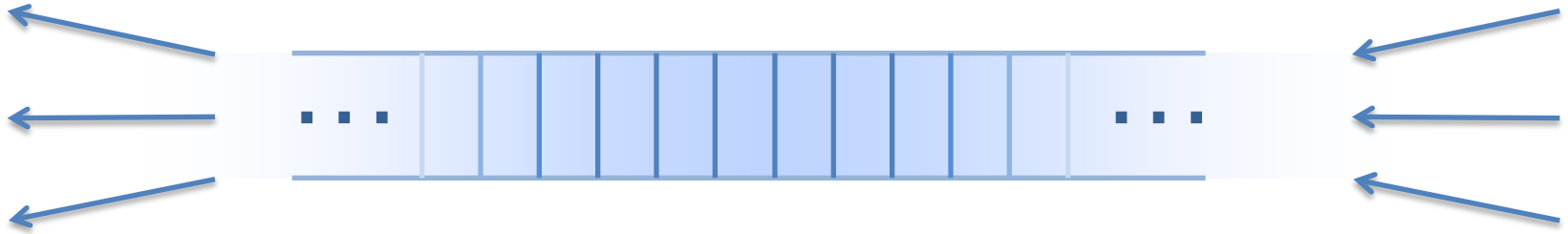




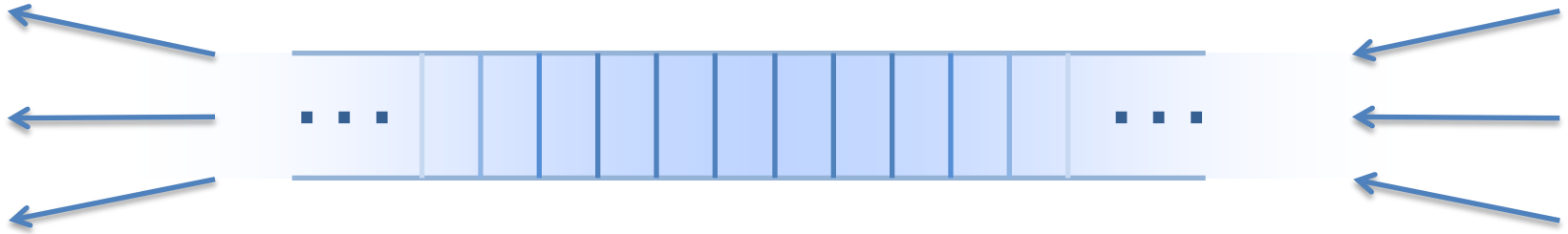




Multi-Producer Multi-Consumer Queue

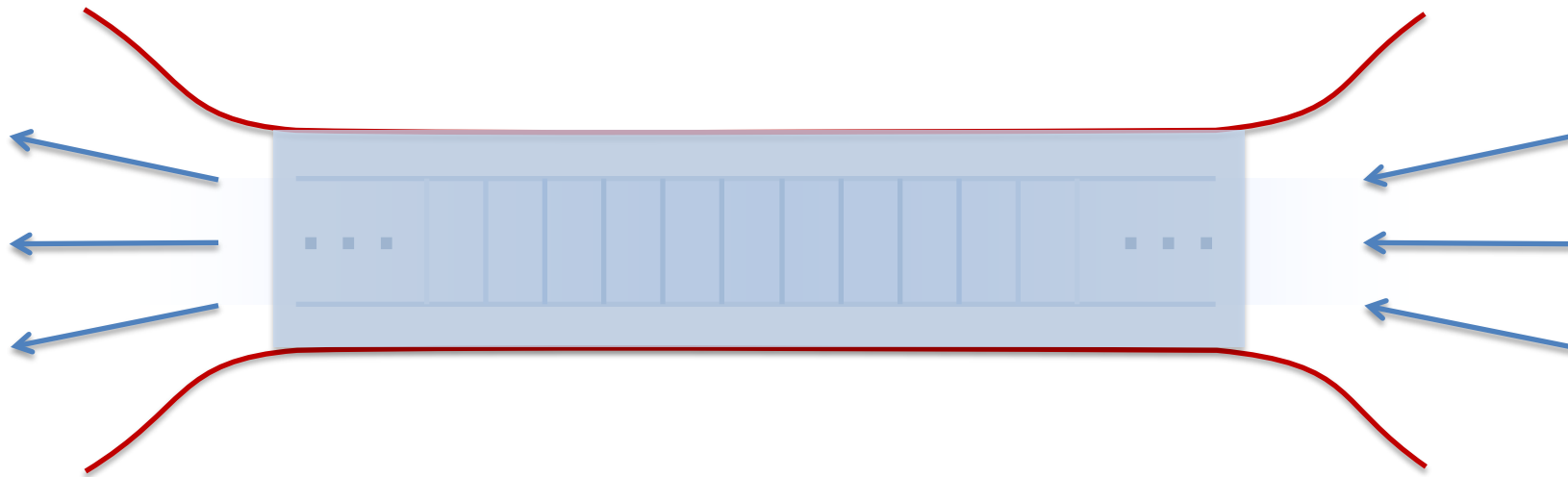


MPMC Queue





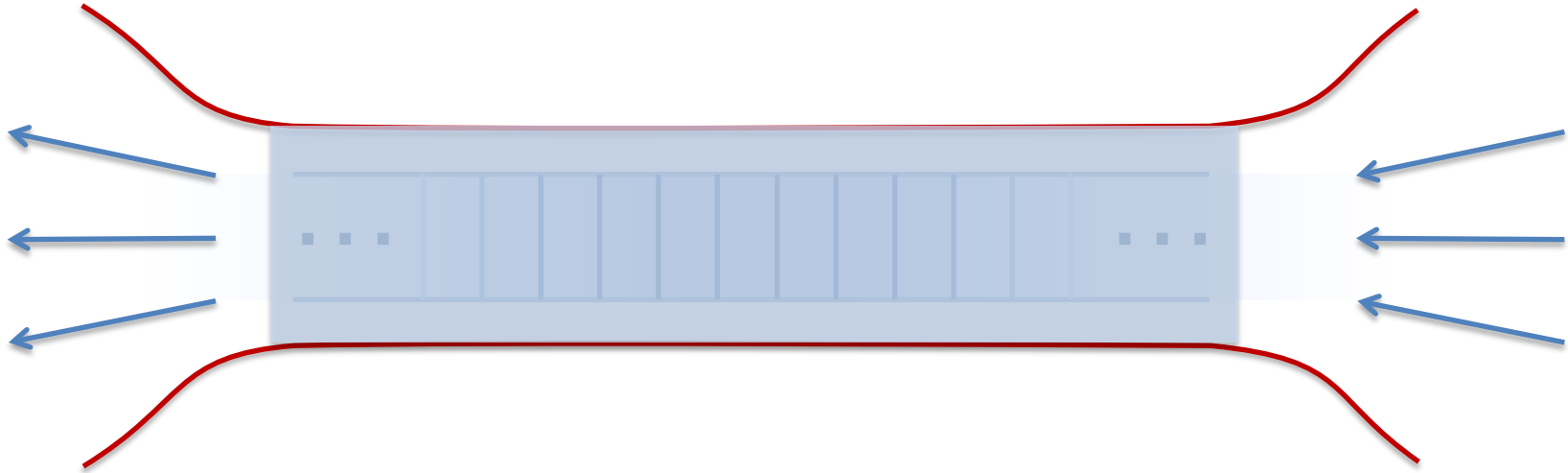
MPMC Queue



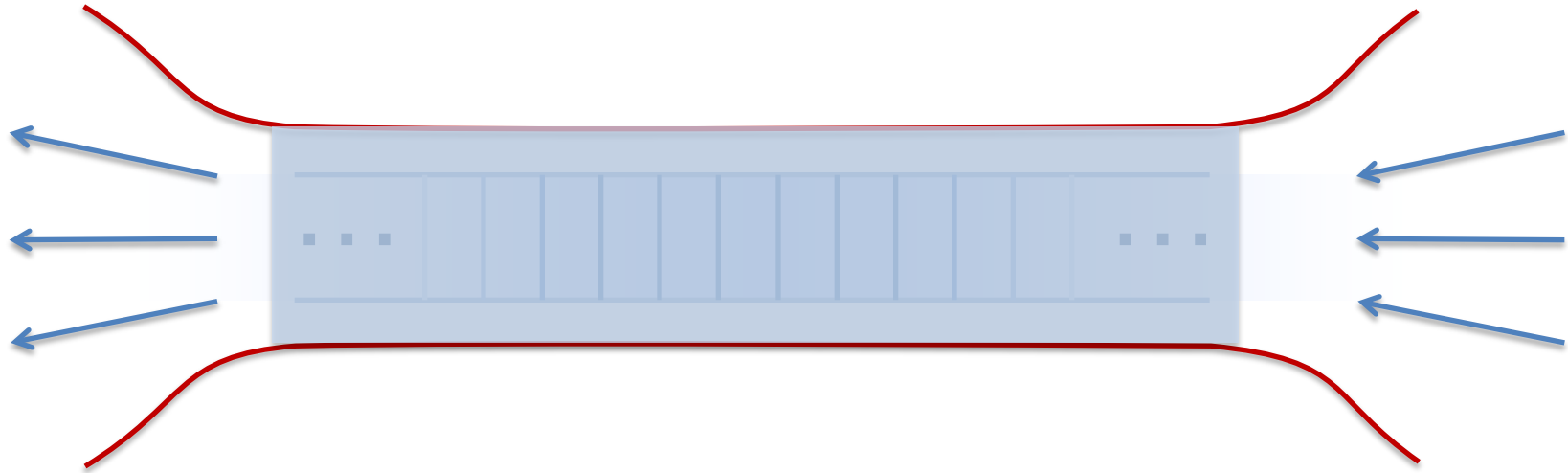


MPMC Queue

SPSC
SPMC
MPSC
MPMC

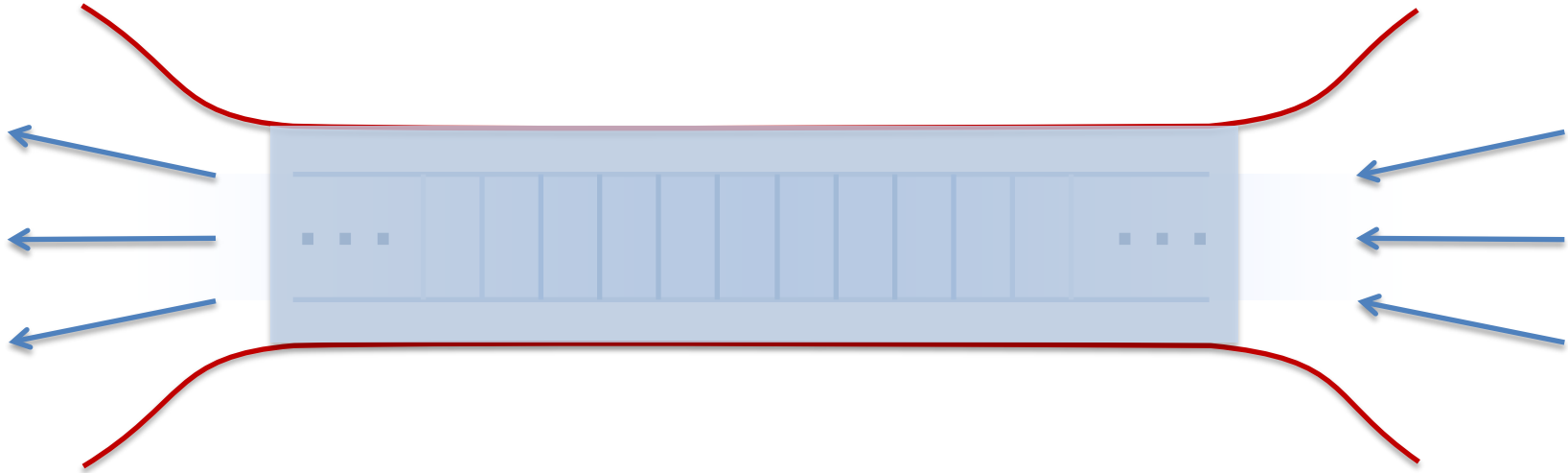


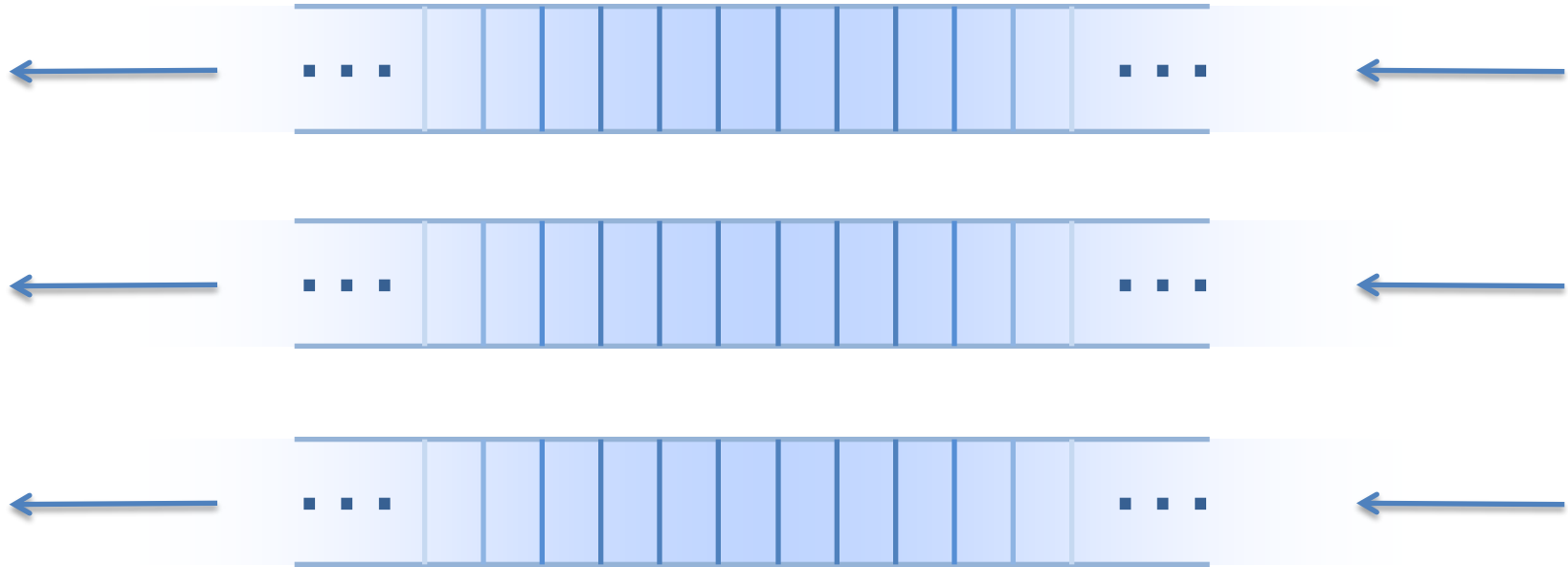
MPMC Queue





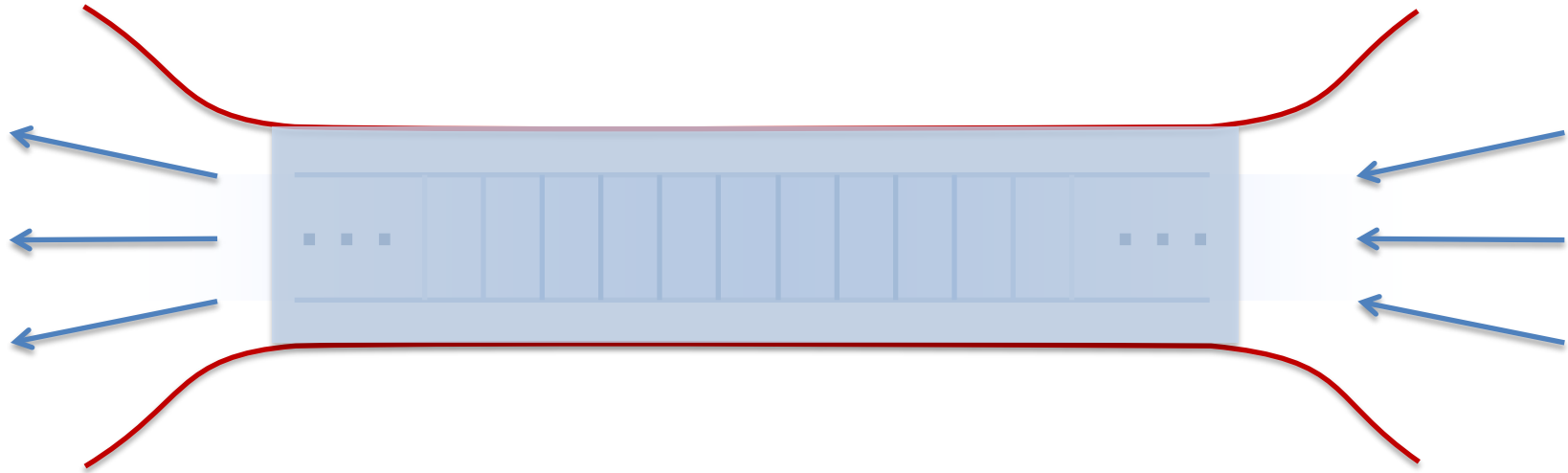
Bottleneck

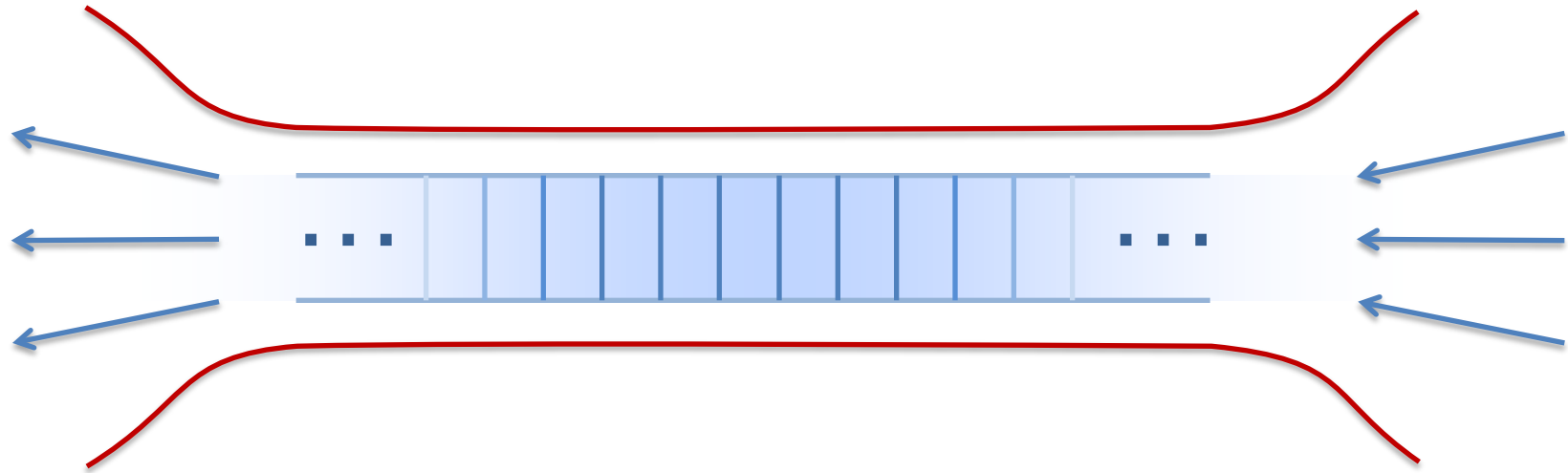


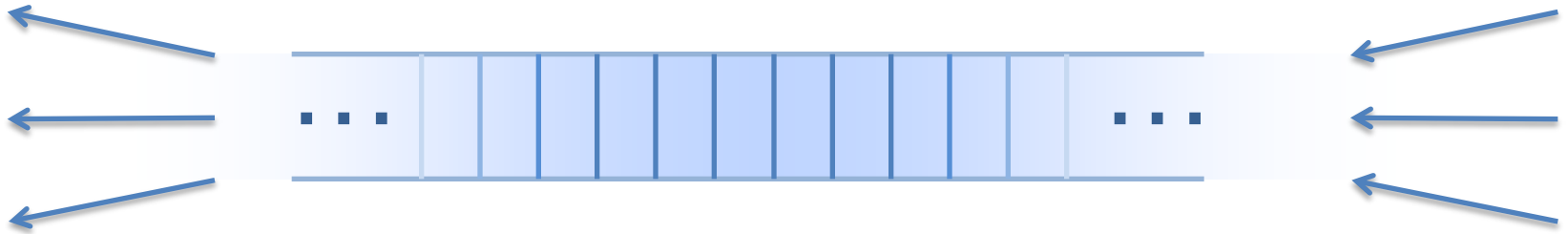


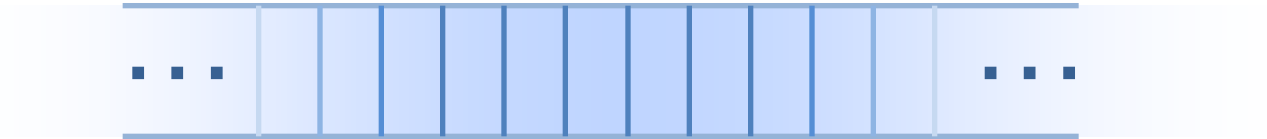


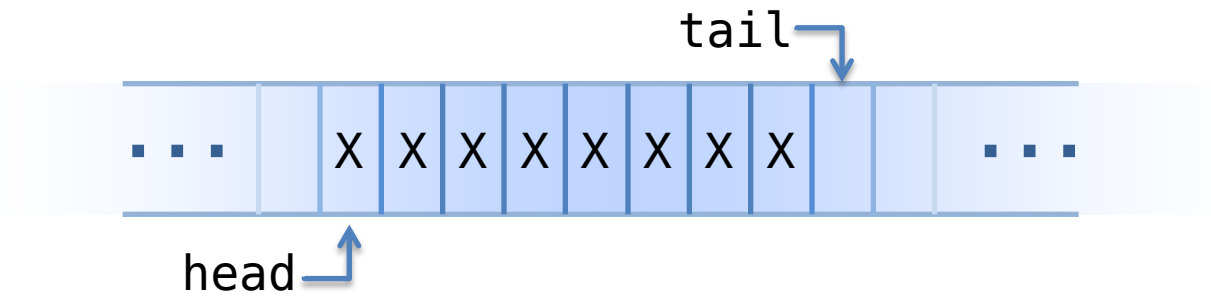






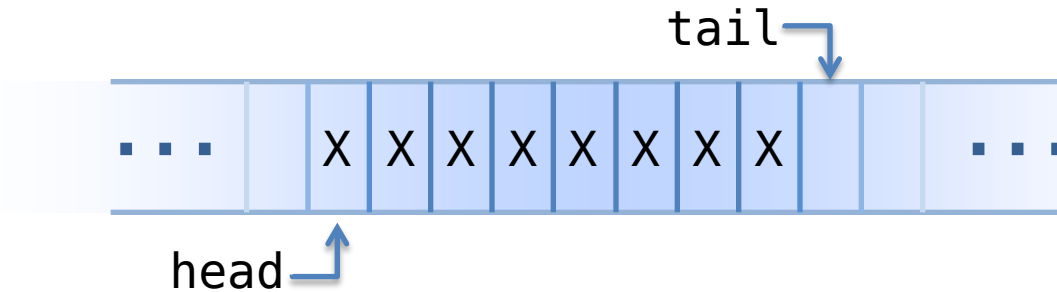






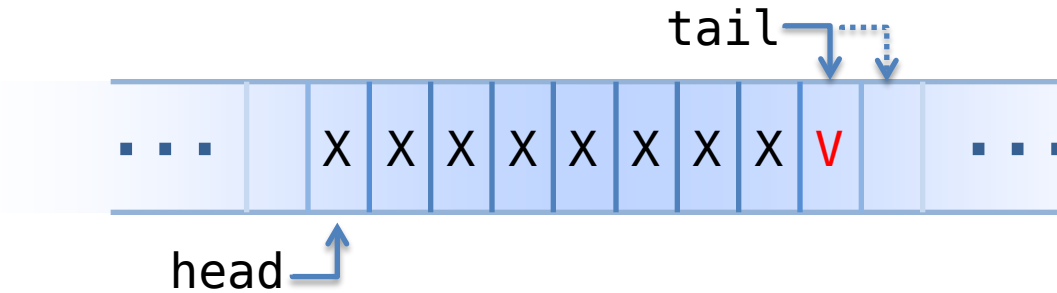


```
class Queue
{
    int buffer[some_size];
    size_t head;
    size_t tail;
};
```



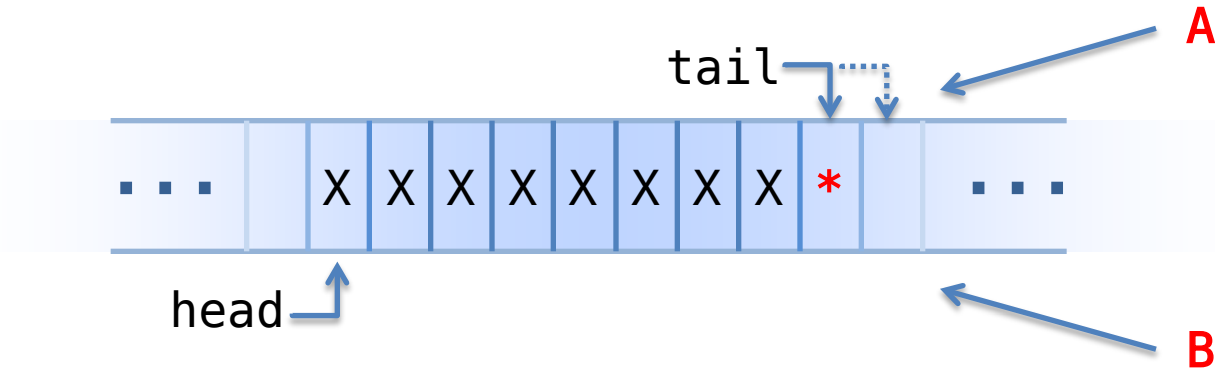


```
void push(int val)
{
    buffer[tail++] = val;
}
```





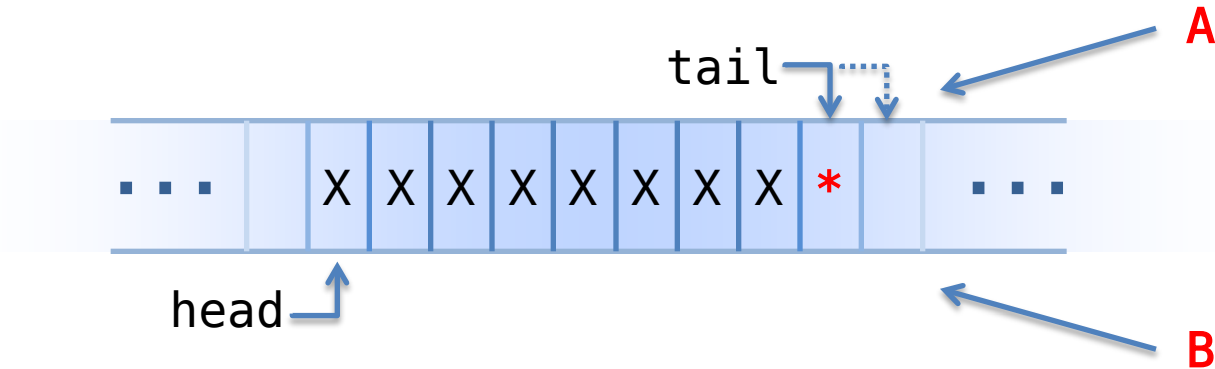
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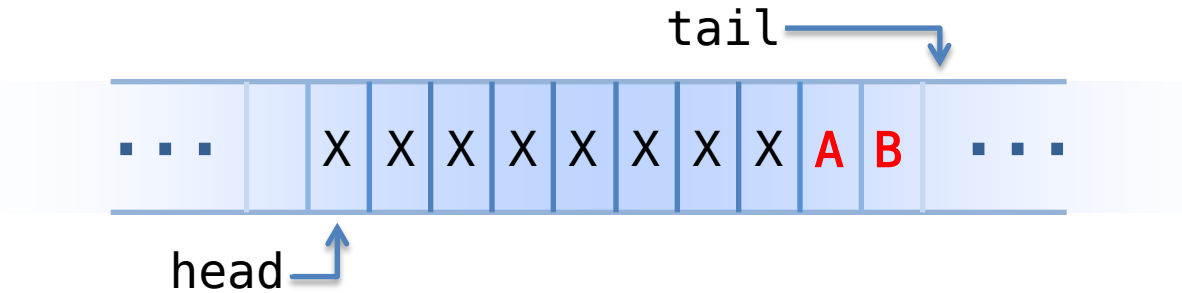


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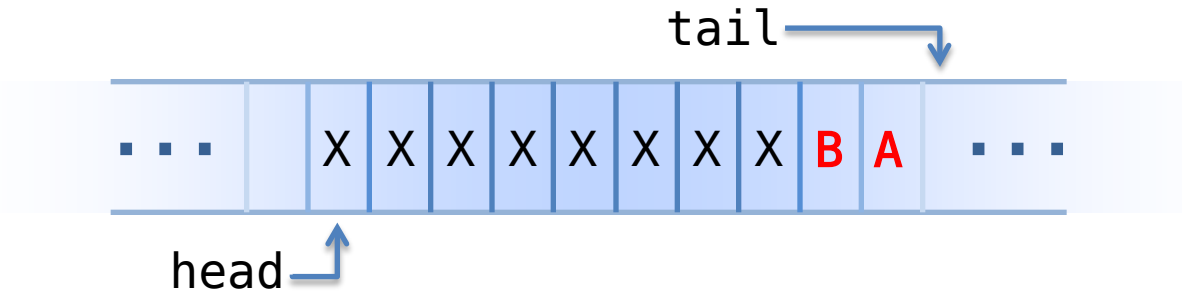
Possible Outcomes?



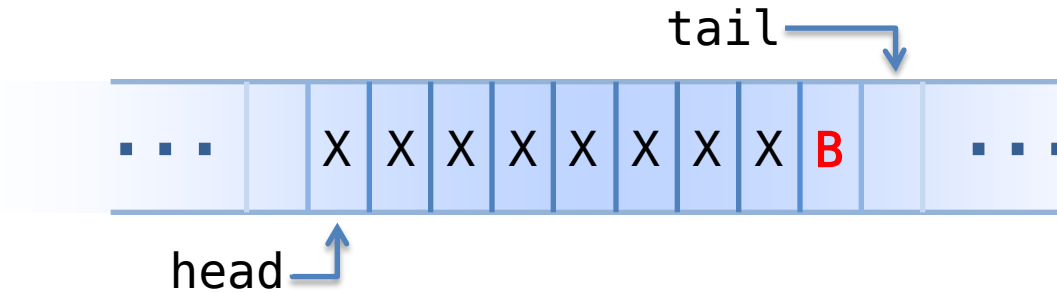
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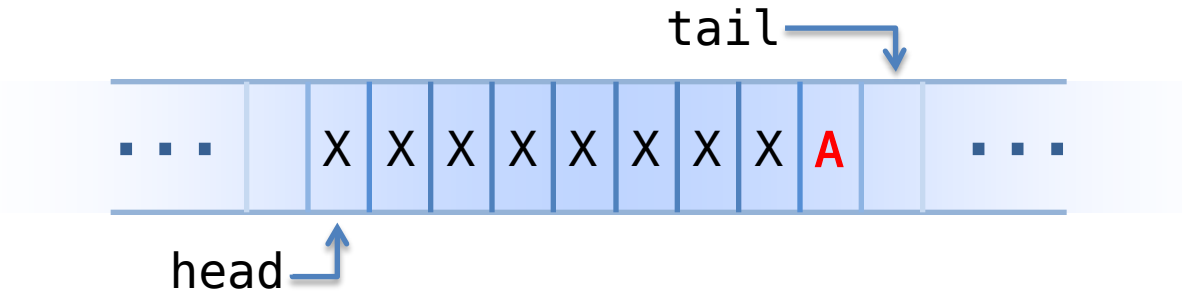
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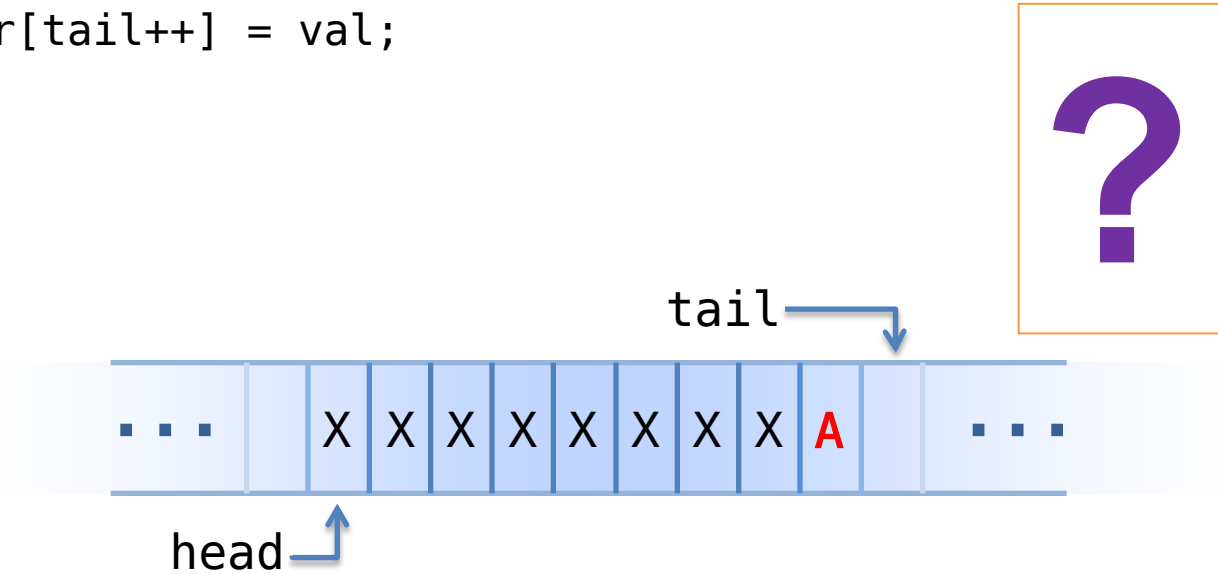


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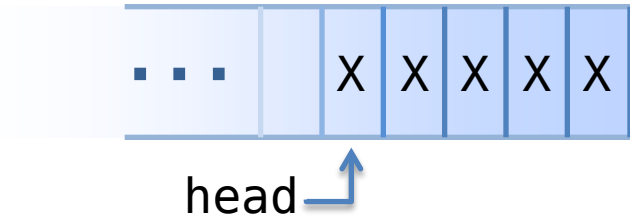


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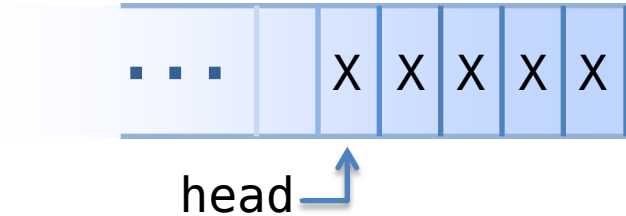


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A

B



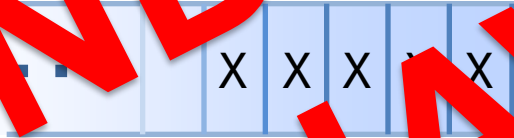
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A

B

UNDEFINED BEHAVIOUR

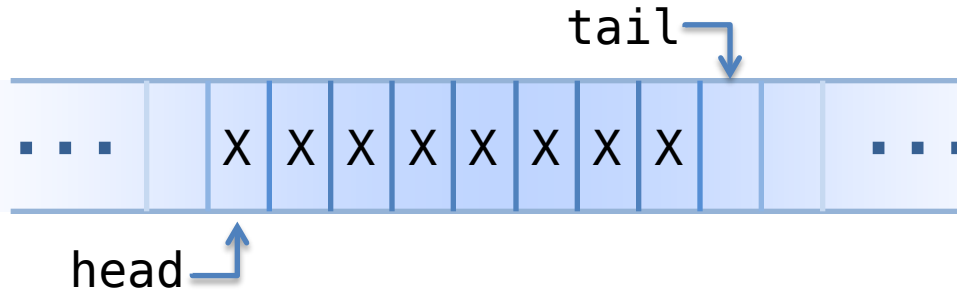


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A

B



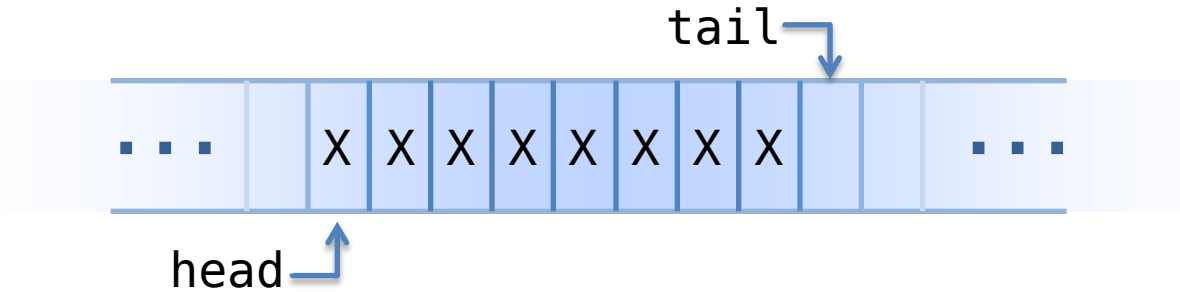


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```
class Queue
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    atomic<int> buffer[SZ];
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};
```

A ←

← **B**



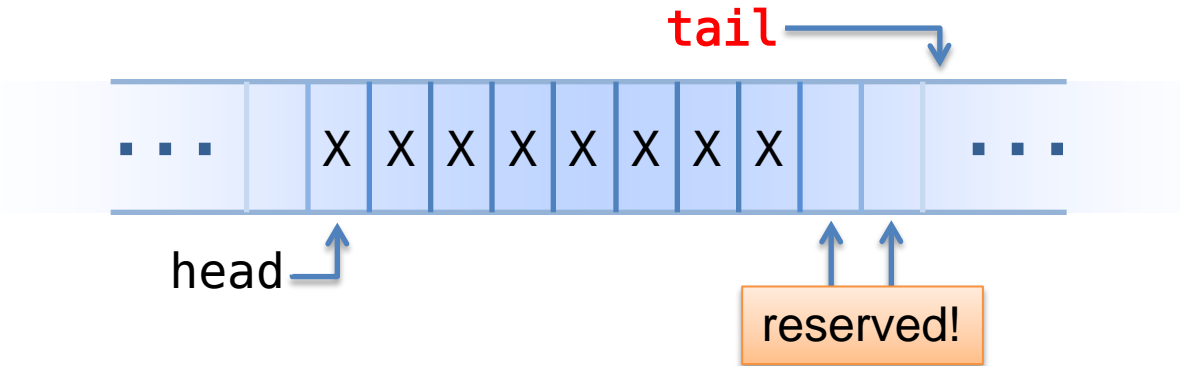


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A

B



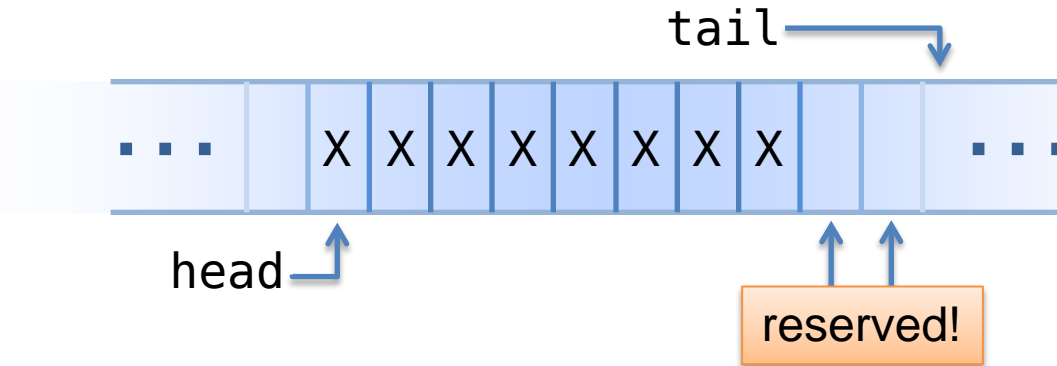


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A

B



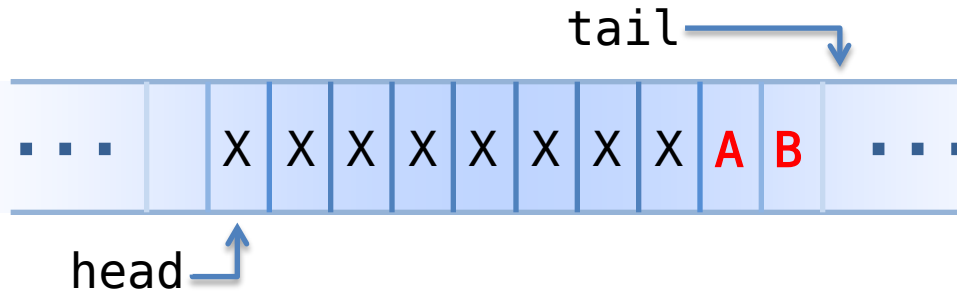


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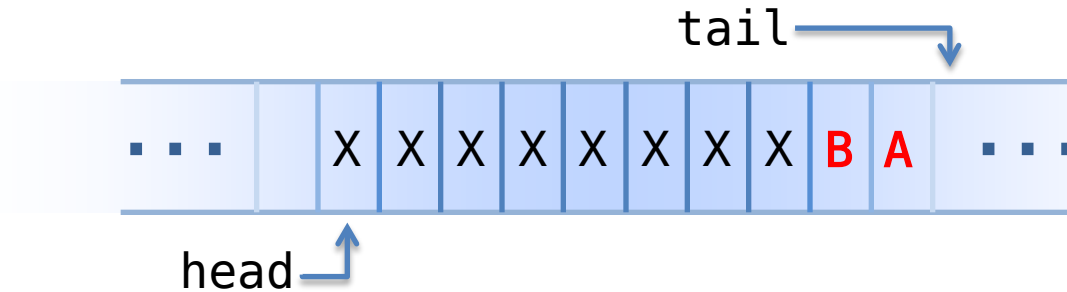
A

B



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A

B

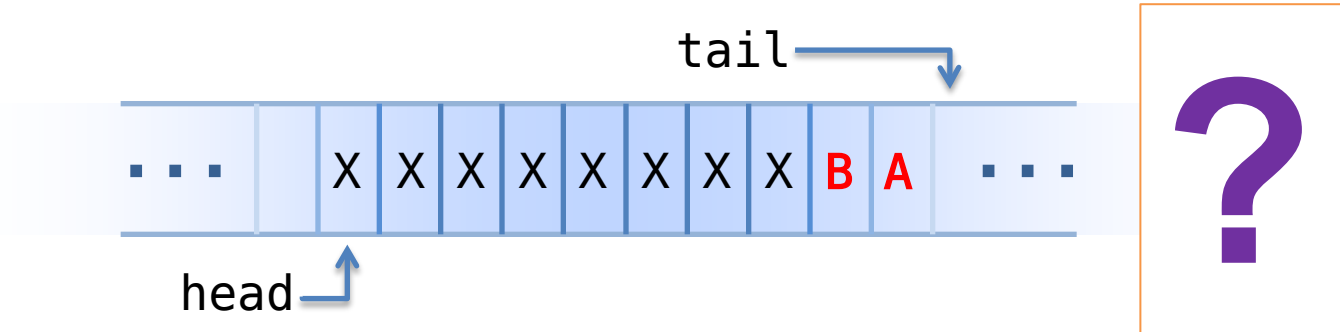


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A

B



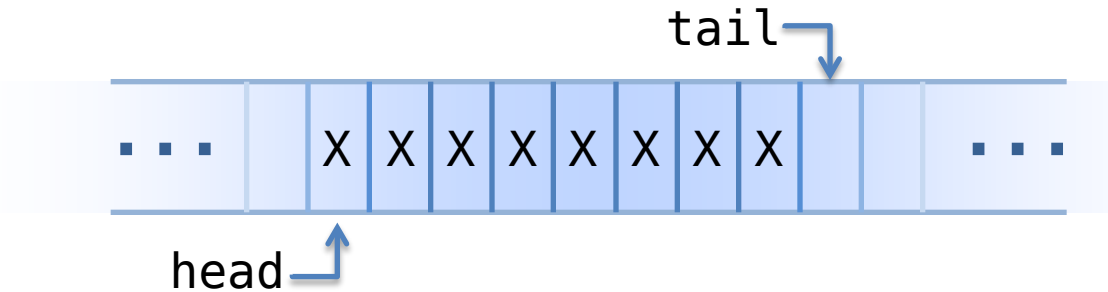


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A

B



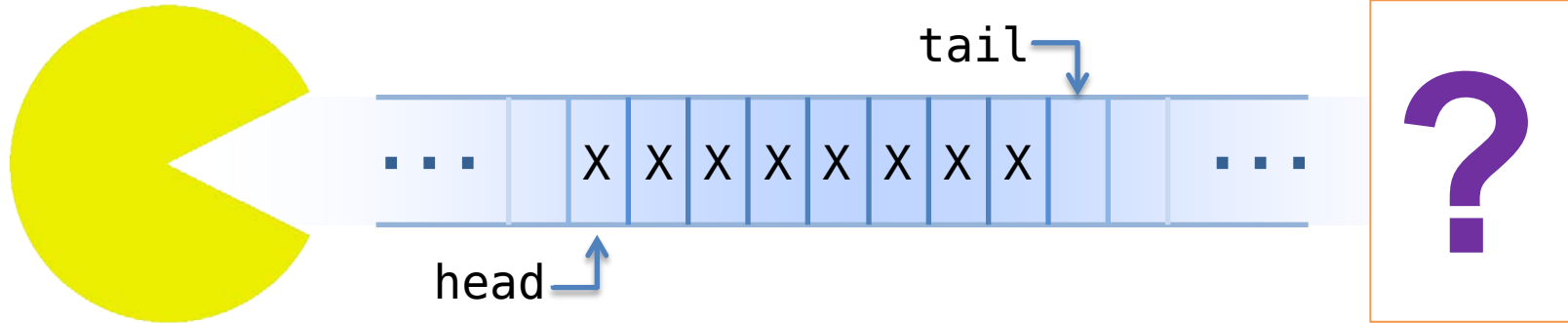


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A

B



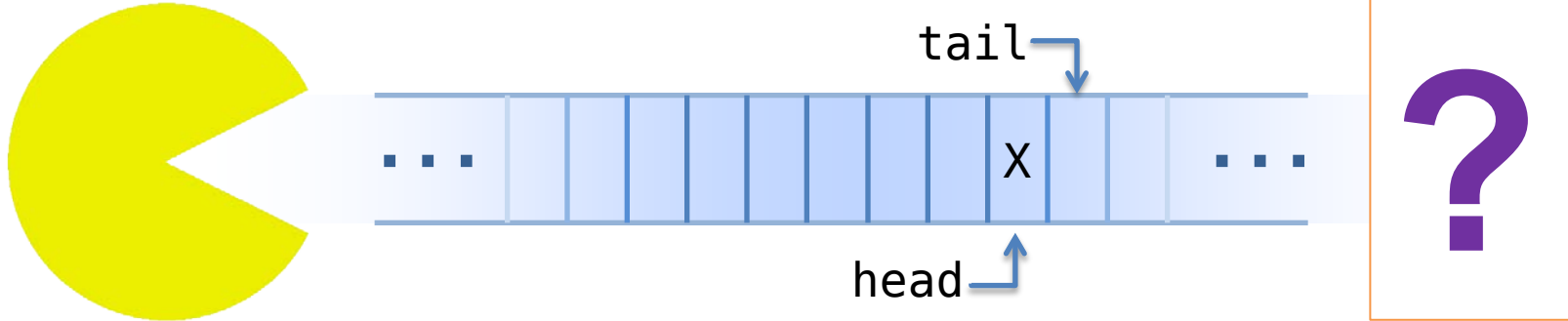


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A

B





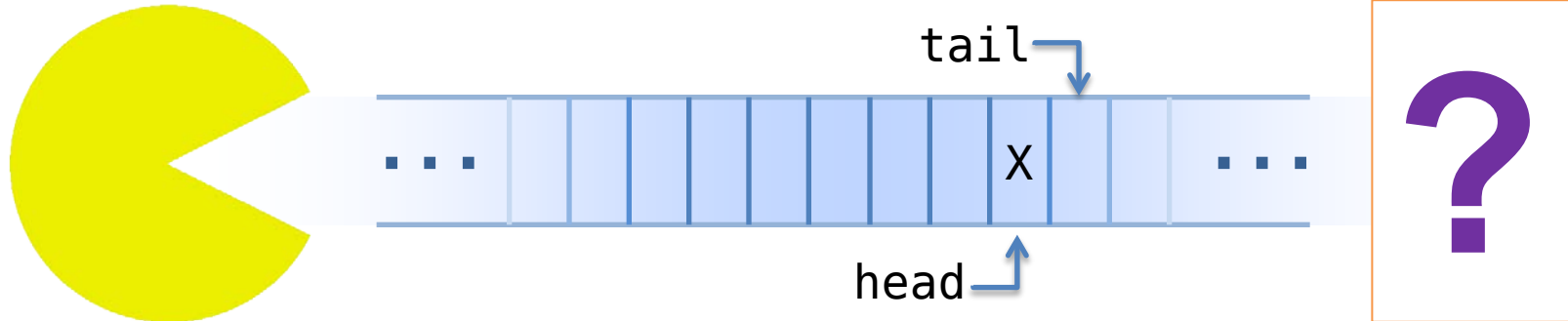
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    buffer[tail++] = val;
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```

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class Queue
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    int buffer[SZ];
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};
```

X...

A

B





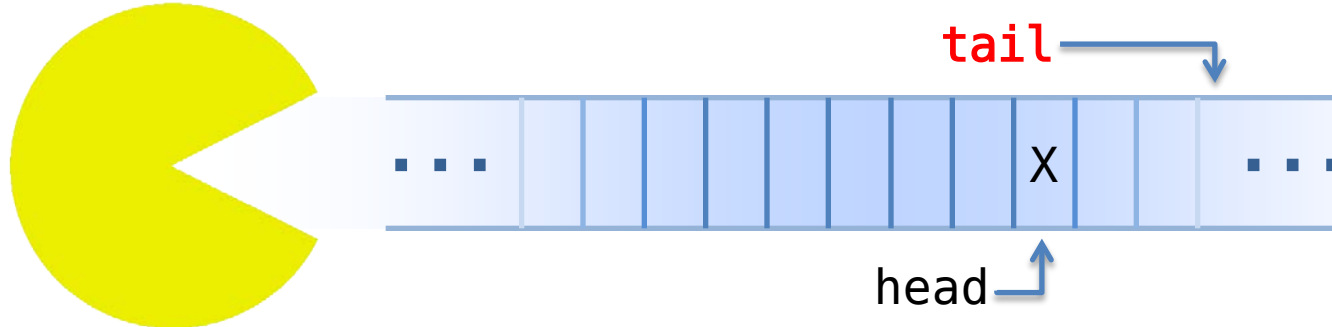
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```

X...

A

B



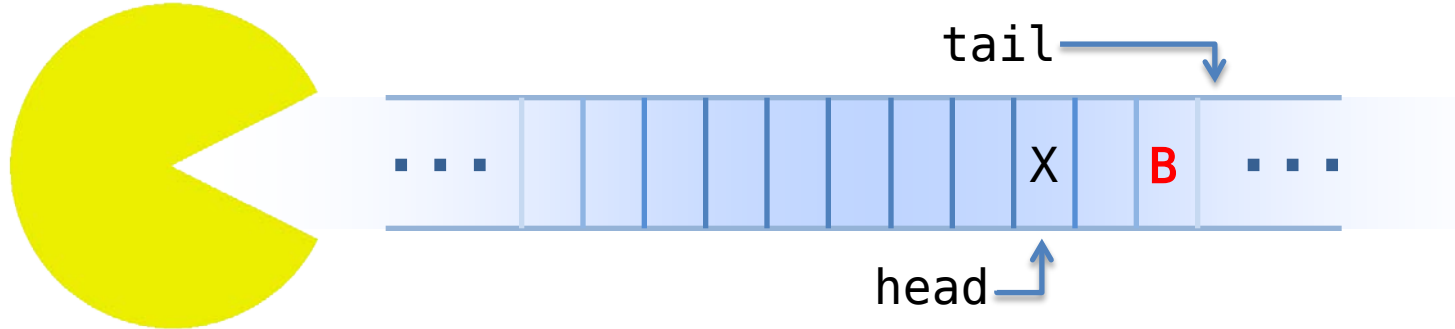


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A B

X...



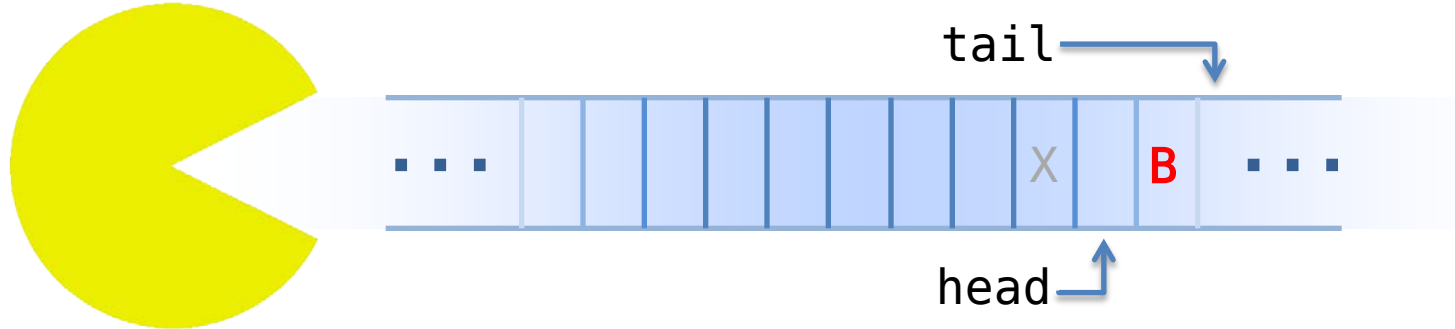


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A B

X...



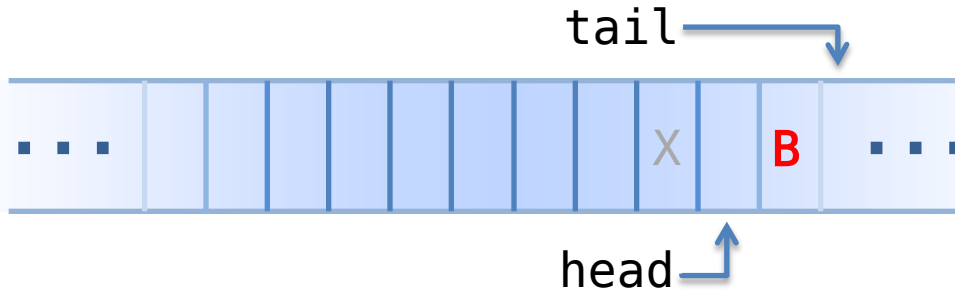


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A B


X...

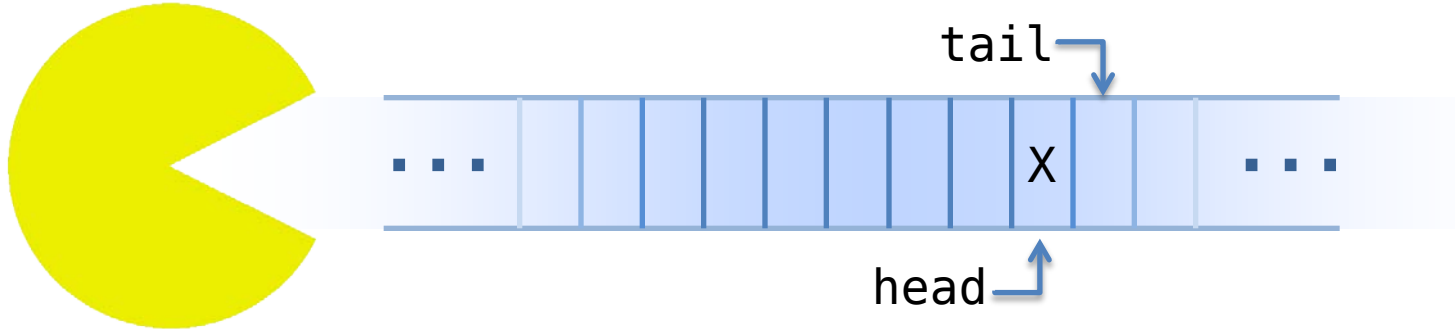




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};
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 **X...**

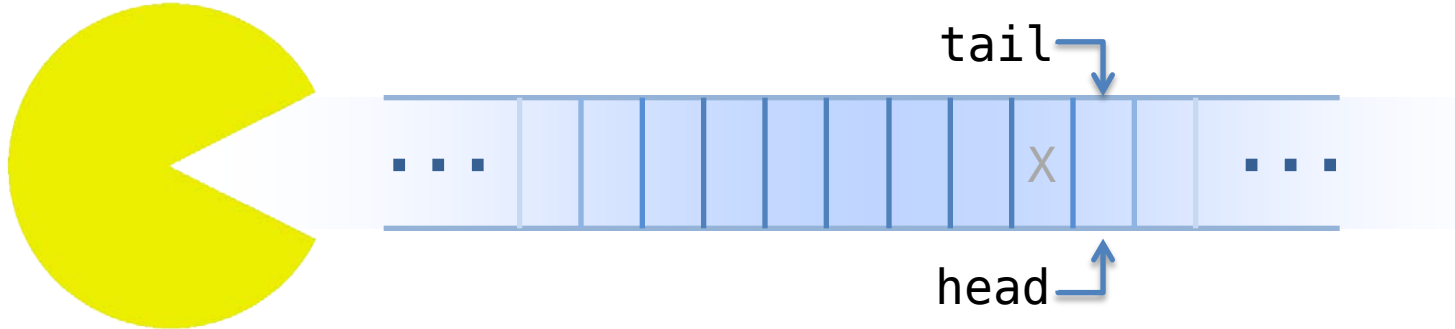




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 **X...**

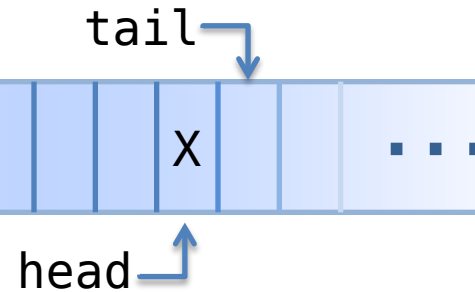




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 **X...**

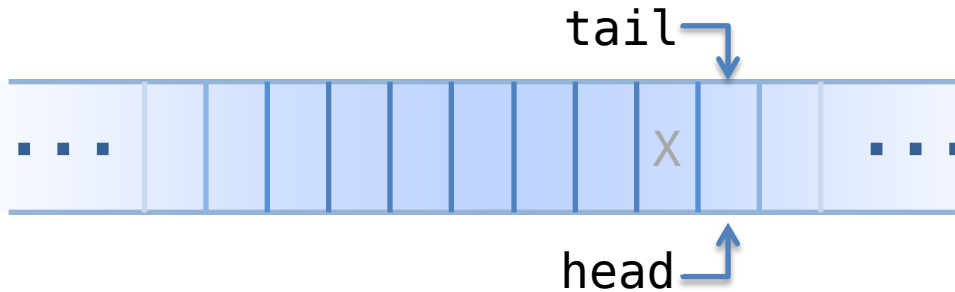




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 **X...**

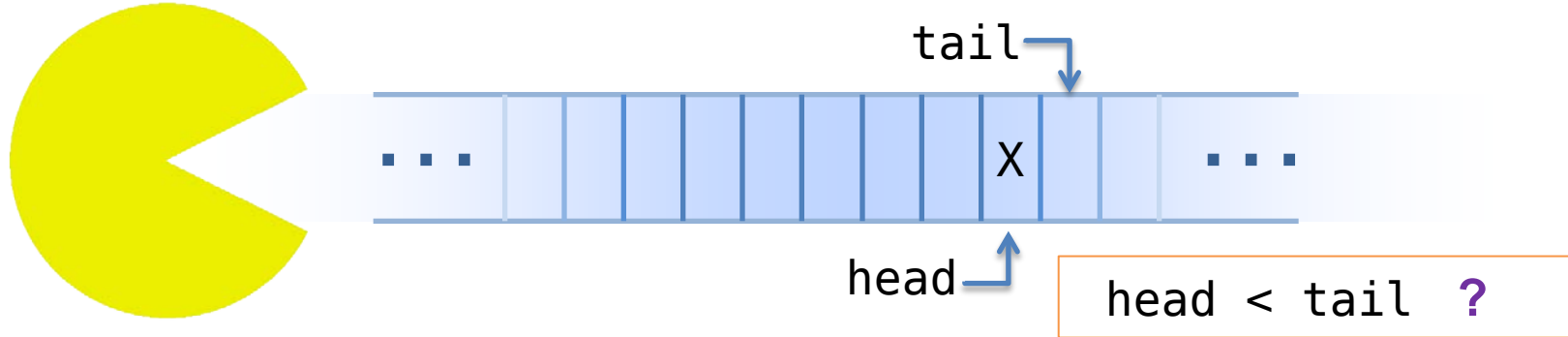




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 **X...**

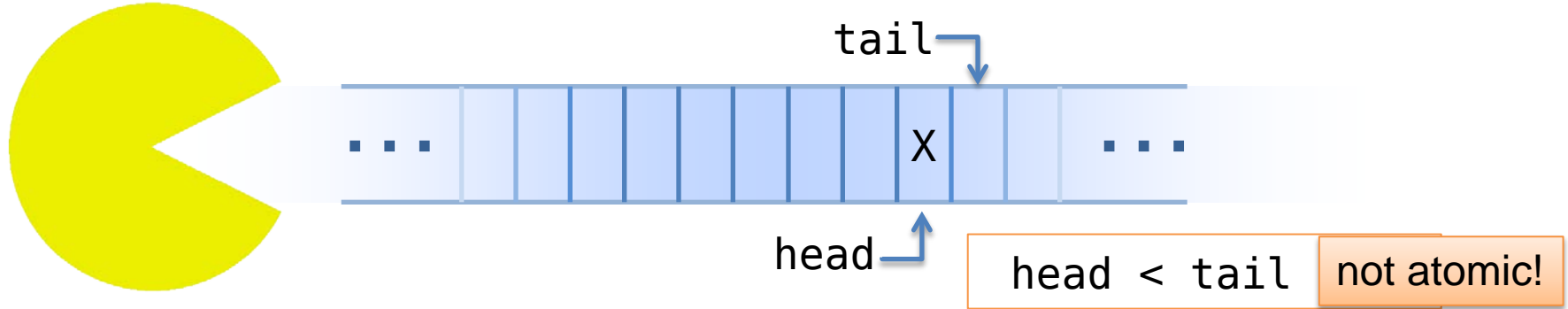




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 **X...**



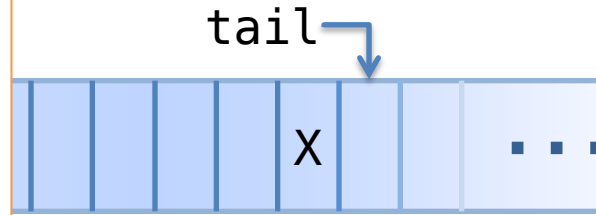


```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...

```
if (atomic_less(head, tail))
{
    read_head();
};
```



head

head < tail

not atomic!

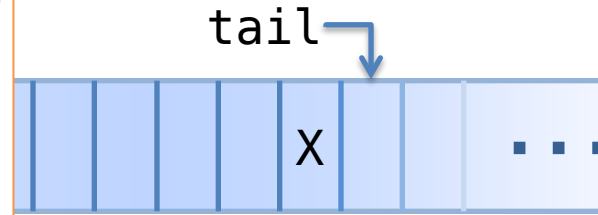


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}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...

```
if (atomic_less(head, tail))
{
    THEN
    read_head();
};
```



head

head < tail

not atomic!



```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SIZE];
    atomic_int tail;
    atomic_int head;
};
```

X...

```
if (atomic_less(head, tail))
{
    THEN
    read_head();
};
```



head < tail not atomic!



```
void put (...) {  
    buf  
}
```

```
if (atom  
{ THEN  
    rea  
};
```

X...

THEN

is a 4-letter word

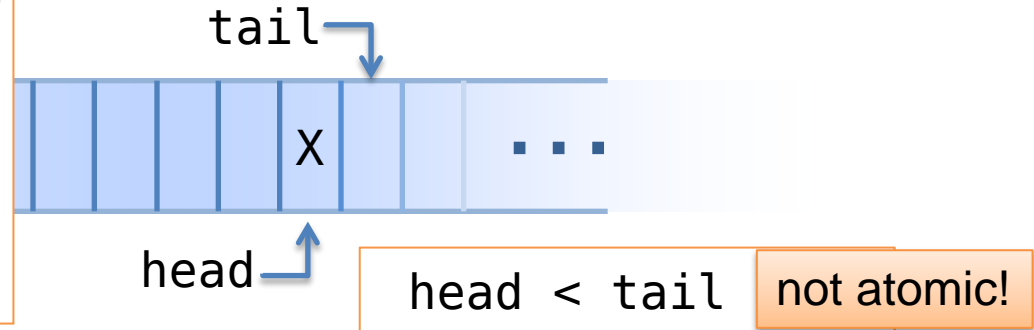
atomic!

```
void push(int val)
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}
```

```
class Queue
{
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};
```

X...


```
if (atomic_less(head, tail))
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    THEN
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```

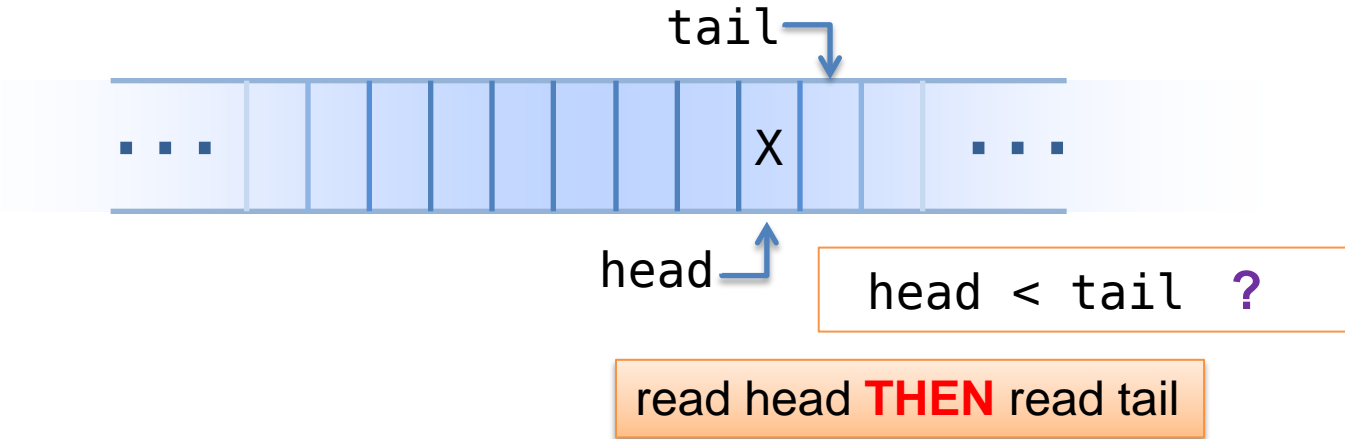




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```


 X...



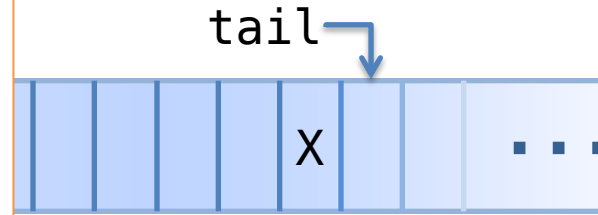


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};
```

 **X...**

```
statement1;
THEN
statement2;
THEN
statement3;
...
```



head

head < tail ?

read head **THEN** read tail



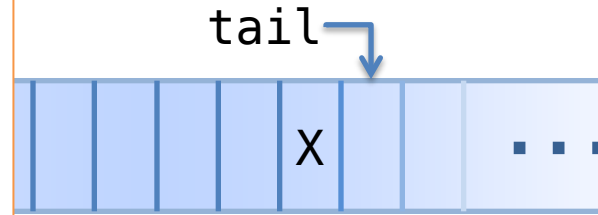
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X...

```
statement1;
THEN
statement2;
THEN
statement3;
...
```

Local vs **Shared**



head

head < tail ?

read head **THEN** read tail



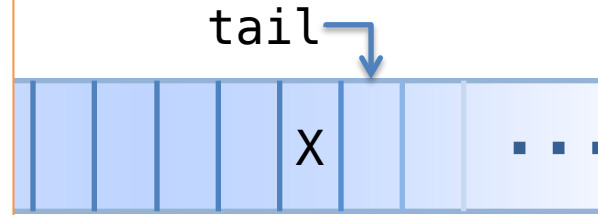
```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...

```
statement1;
THEN
statement2;
THEN
statement3;
...
```

Local vs **Shared**



head


head < tail ?

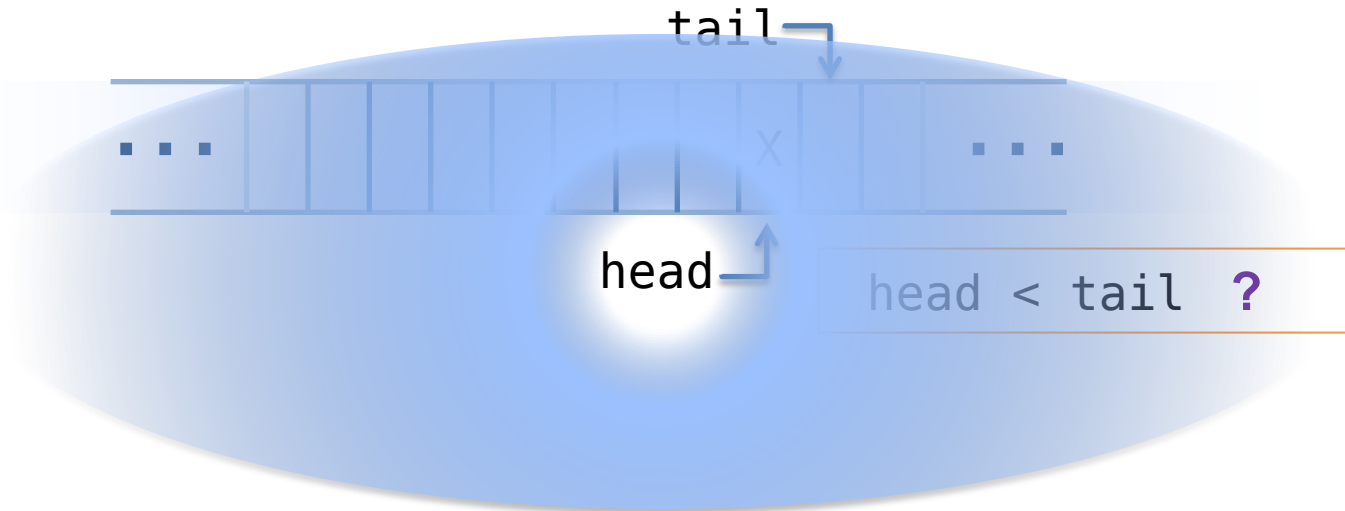
don't assume **STATE**



```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

 **X...**

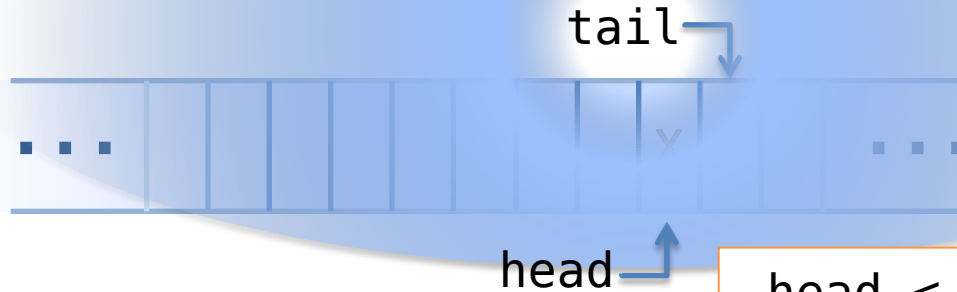




```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...



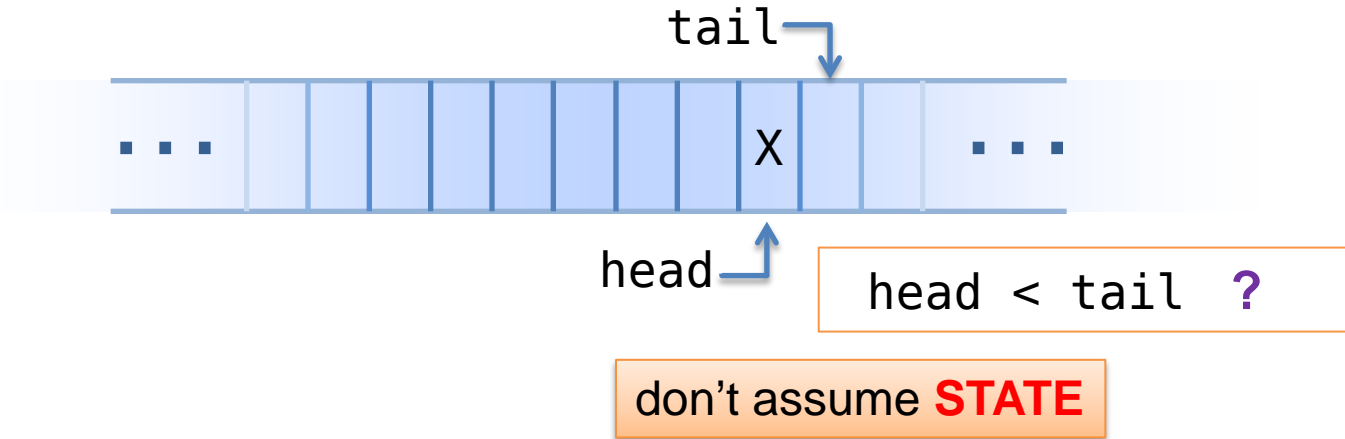
head < tail ?



```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...

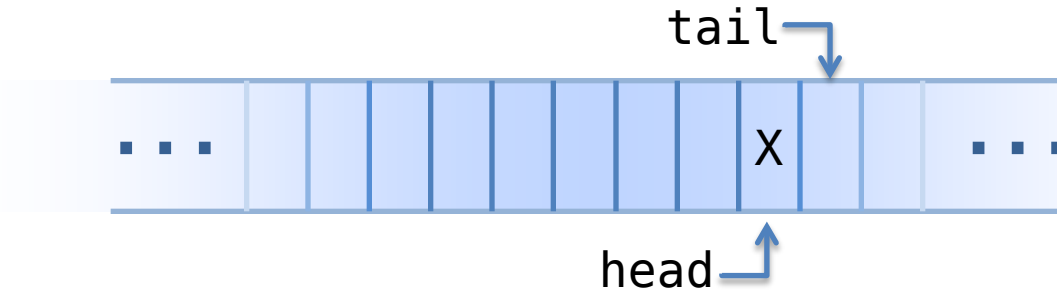




```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...



every **STATE** is a good **STATE**

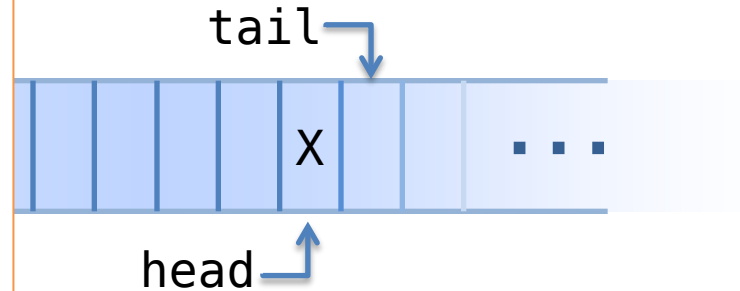


```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...

```
statement1;
THEN
statement2;
THEN
statement3;
...
```



every **STATE** is a good **STATE**

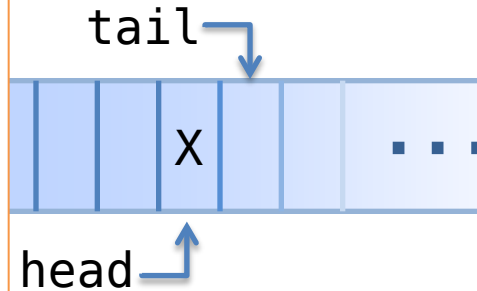


```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
if (some_state) {
    // some_state is still true(?)
    then_do_stuff();
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...




every **STATE** is a good **STATE**

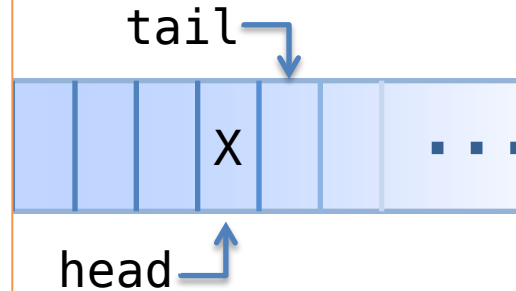


```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
void member_function {
    break_invariants;
    do_stuff;
    restore_invariants;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

 **X...**




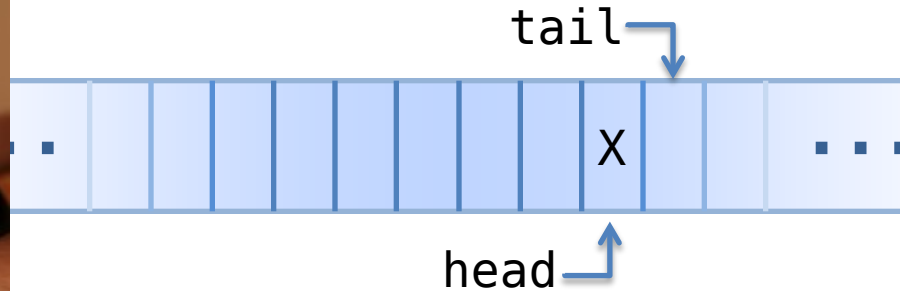
no “temporary suspension” of invariants



```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

 **X...**



no “temporary suspension” of invariants



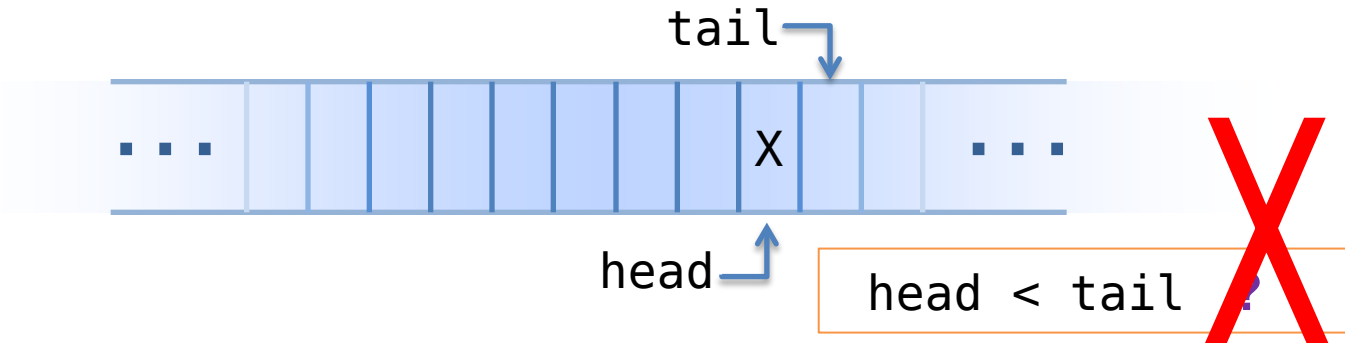
```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...

A

B





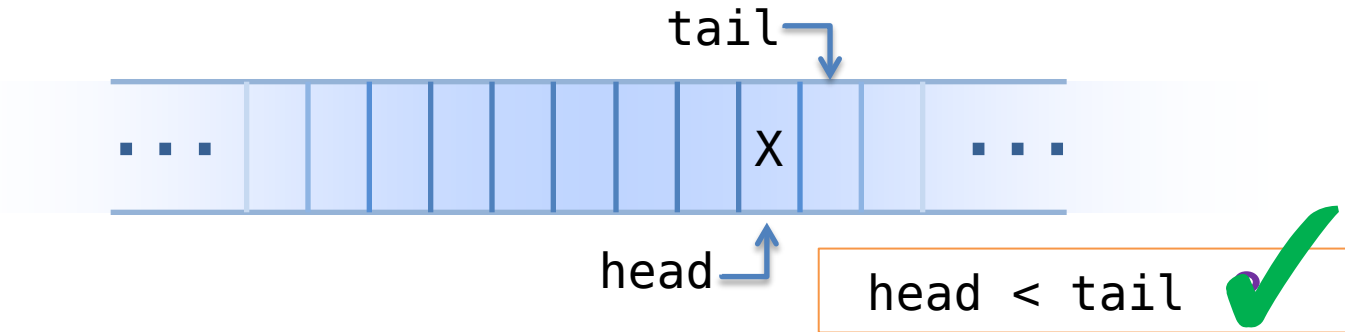
```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...

A

B





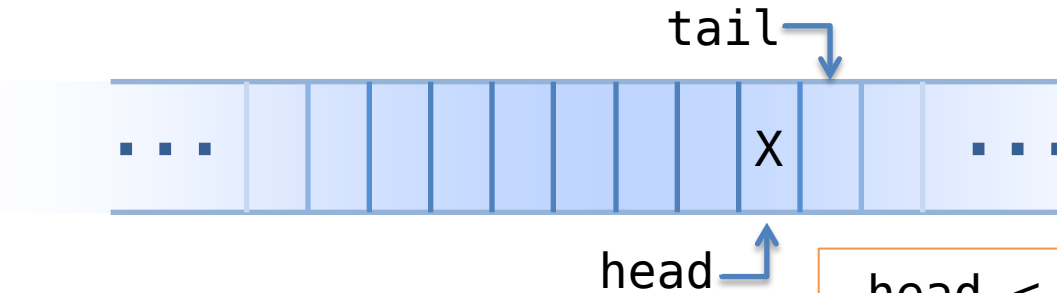
```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...

A

B



head < tail




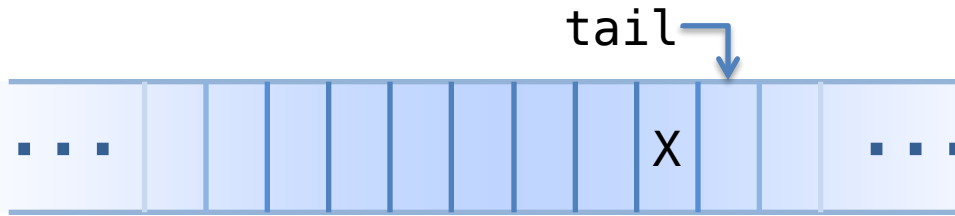
ensure tail is always increasing



```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

 **X...**




head

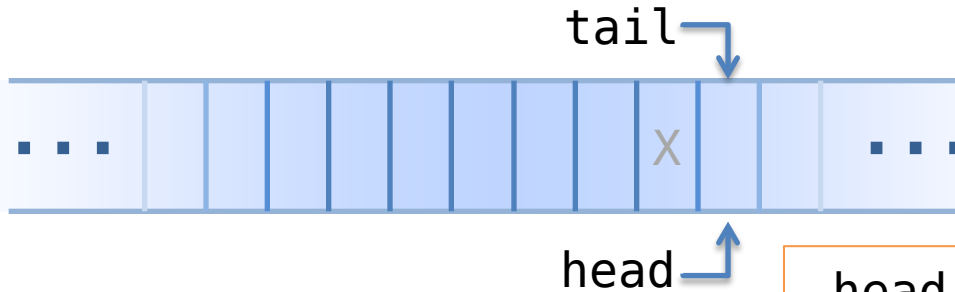
head < tail ?



```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

 **X...**



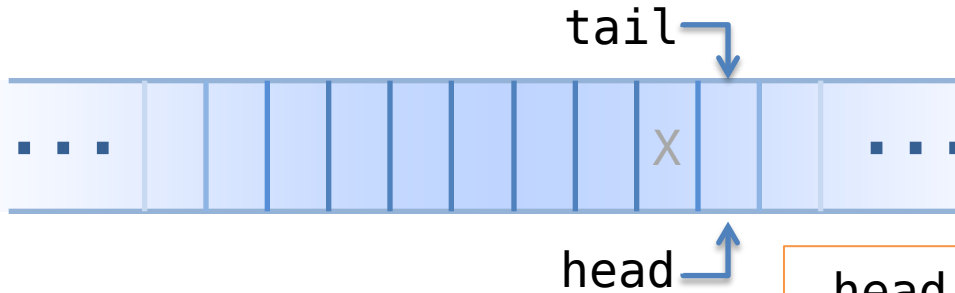
head < tail ?



```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...



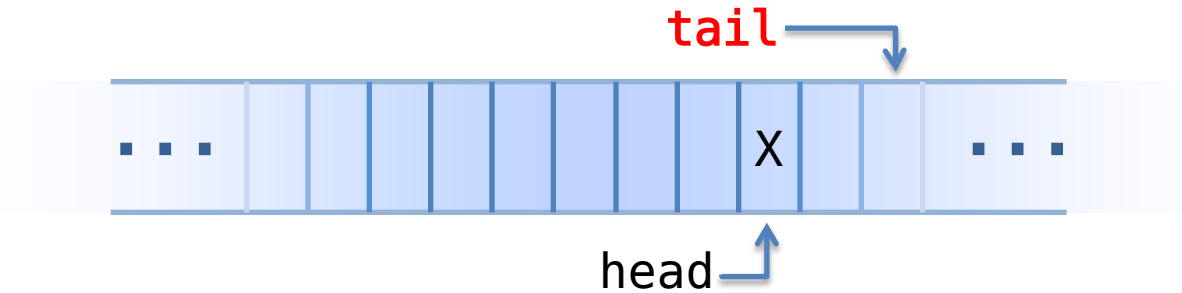
head < tail ?



```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

A



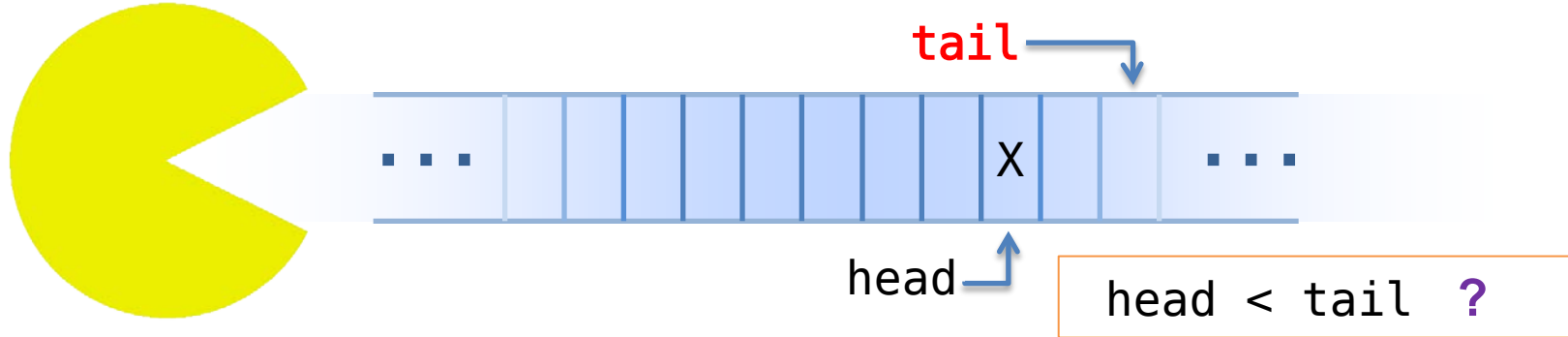


```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...

A



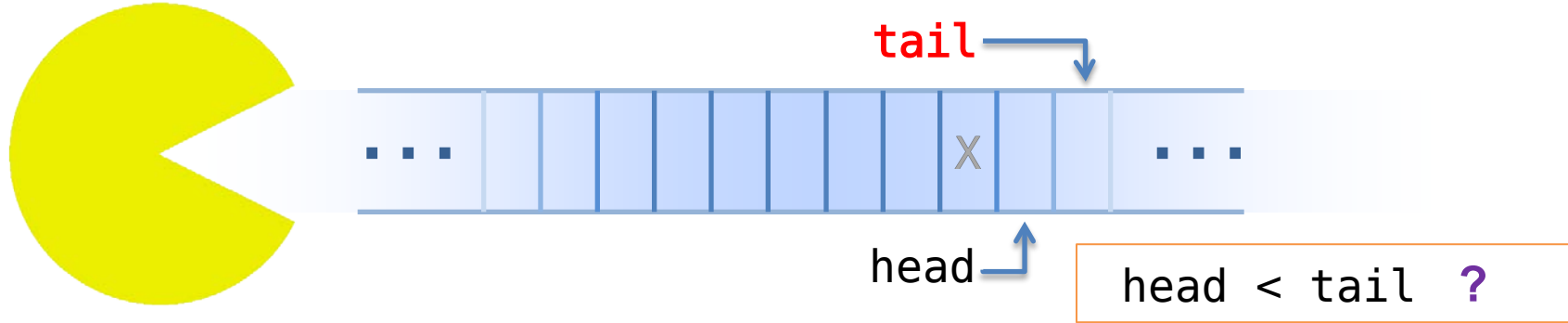


```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X... (with arrow from tail)

A (with arrow from head)

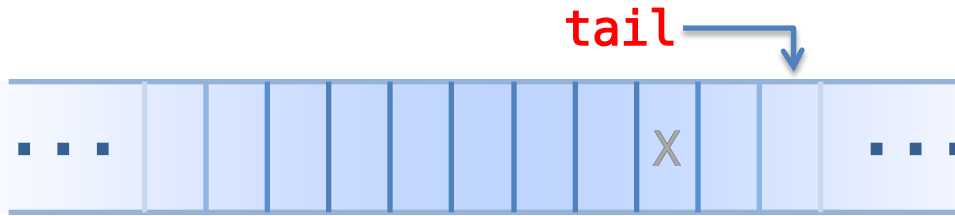




```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...
A



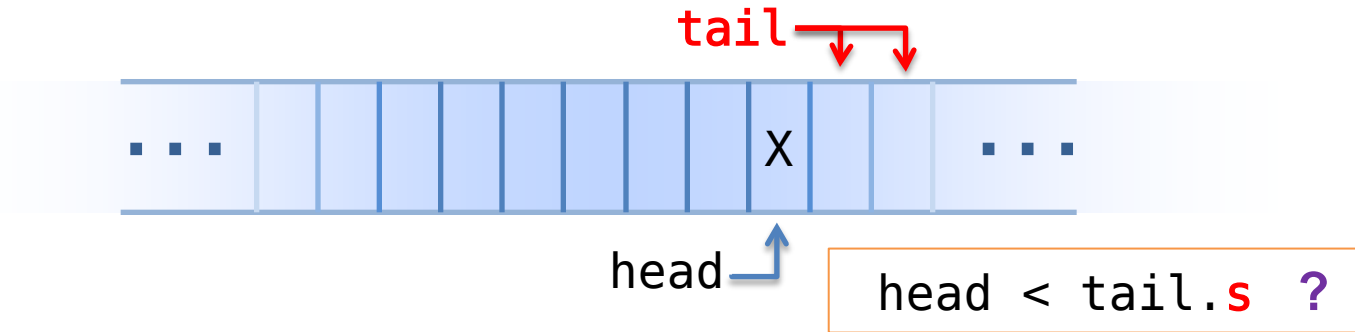
head

head < tail ?



```
void push(int val)
{
    ...
}
```

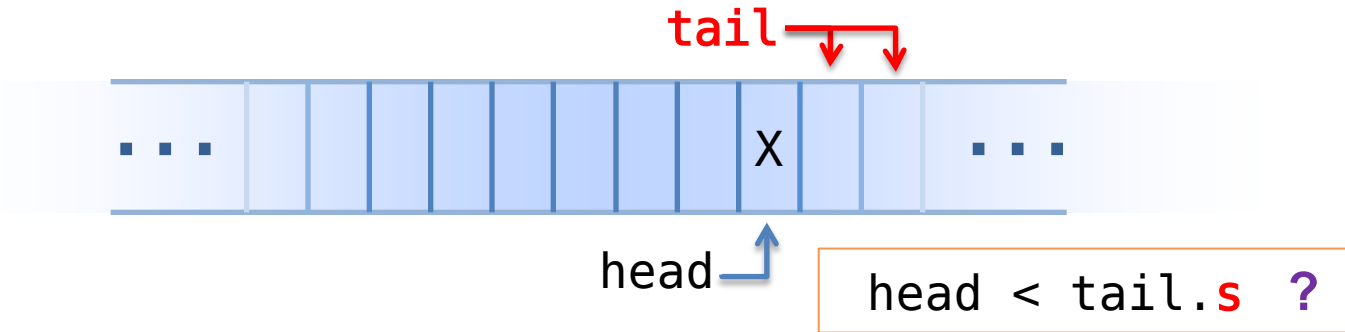
```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct {
        atomic<size_t> s;
        atomic<size_t> e;
    } tail;
};
```





```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    tail.s++;
}
```

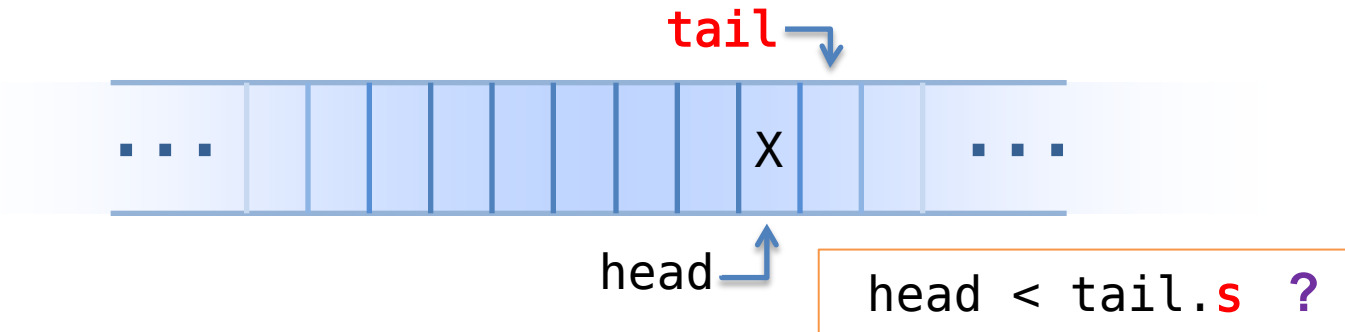
```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
             atomic<size_t> e;
            } tail;
};
```





```
void push(int val)
{
  A → size_t tmp = tail.e++;
  buffer[tmp] = val;
  tail.s++;
}
```

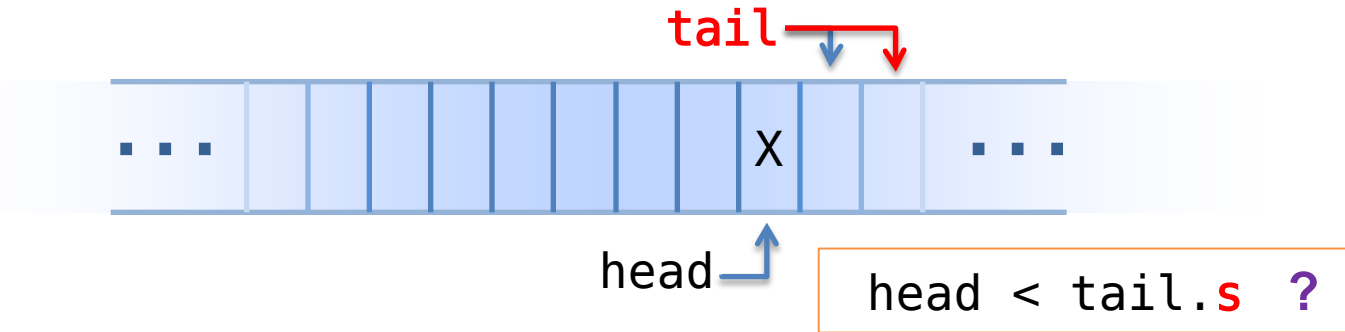
```
class Queue {
  int buffer[SZ];
  atomic<size_t> head;
  struct { atomic<size_t> s;
           atomic<size_t> e;
  } tail;
};
```





```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    tail.s++;
}
```

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct {
        atomic<size_t> s;
        atomic<size_t> e;
    } tail;
};
```

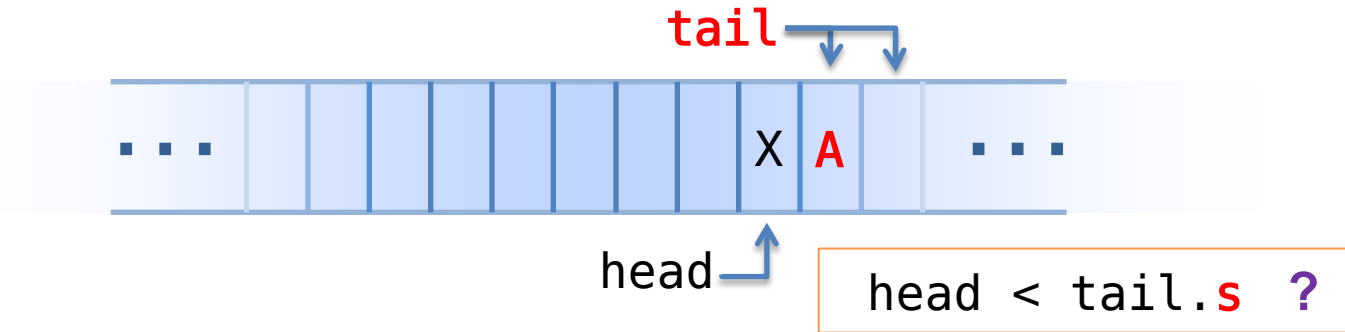




```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    tail.s++;
}
```

A →

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct {
        atomic<size_t> s;
        atomic<size_t> e;
    } tail;
};
```



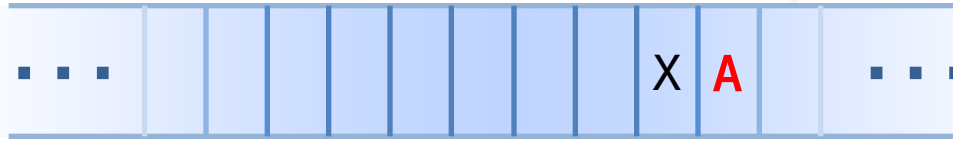


```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    tail.s++;
}
```

A →

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct {
        atomic<size_t> s;
        atomic<size_t> e;
    } tail;
};
```

tail ↓



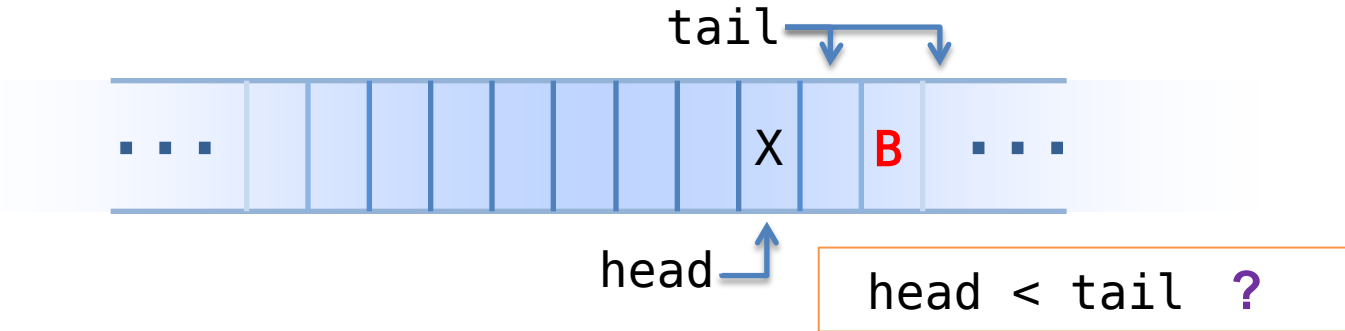
head ↑

head < tail.s ?



```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    tail.s++;
}
```

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
             atomic<size_t> e;
            } tail;
};
```

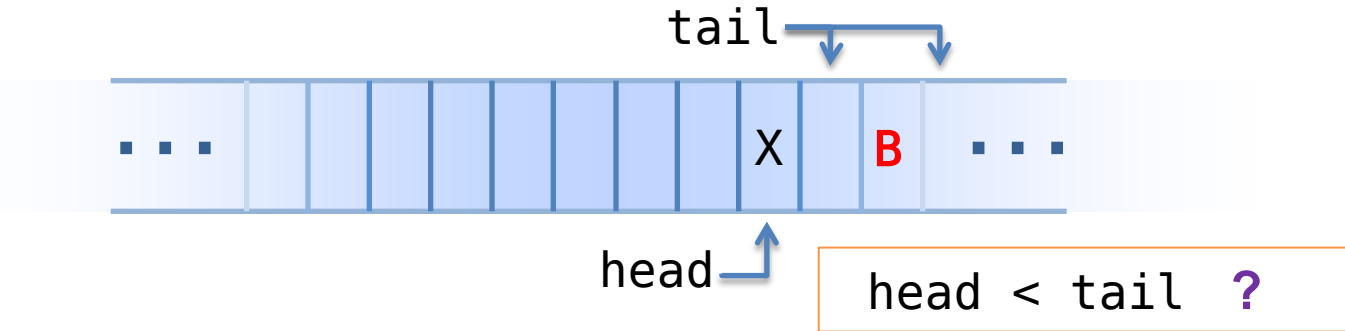




```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    tail.s++;
}
```

A →
B →

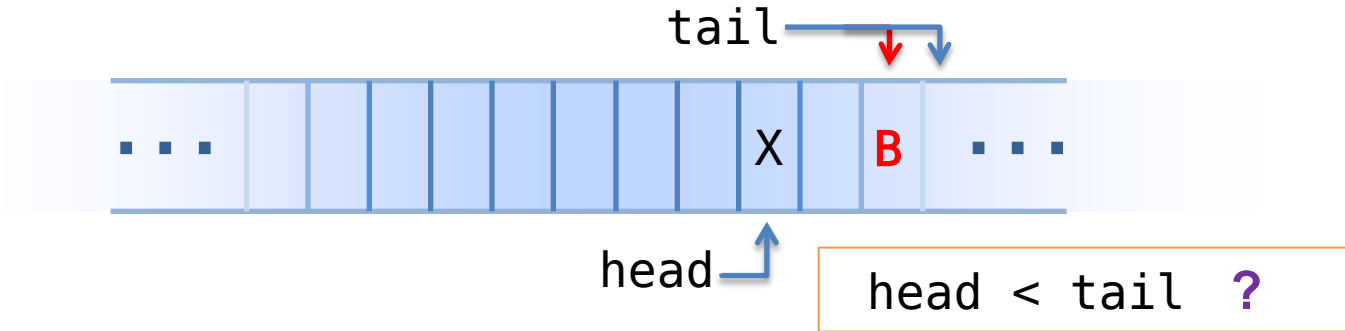
```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
             atomic<size_t> e;
            } tail;
};
```





```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    tail.s++;
}
```

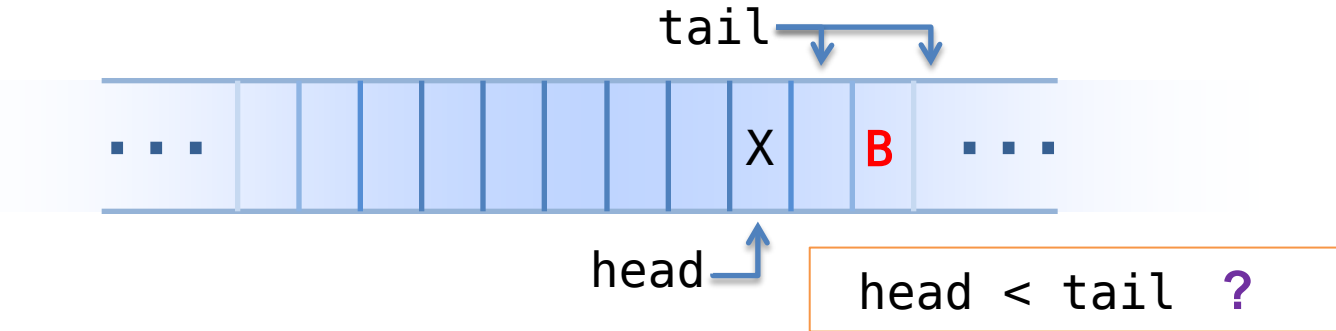
```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct {
        atomic<size_t> s;
        atomic<size_t> e;
    } tail;
};
```





```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    if(tmp == tail.s) {
        tail.s = ...
    }
}
```

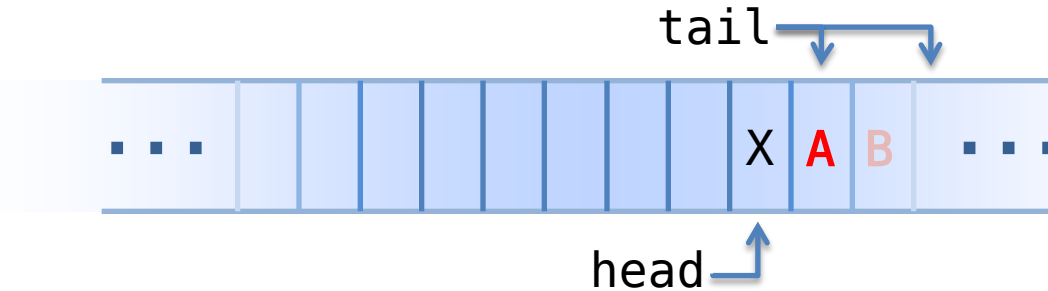
```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct {
        atomic<size_t> s;
        atomic<size_t> e;
    } tail;
};
```





```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    if(tmp == tail.s) {
        tail.s = ...
    }
}
```

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct {
        atomic<size_t> s;
        atomic<size_t> e;
    } tail;
};
```

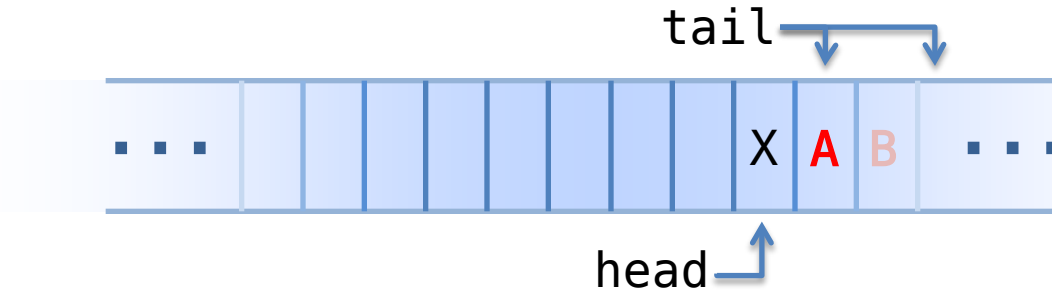




```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    if(tmp == tail.s) {
        tail.s = ...
    }
}
```

THEN

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct {
        atomic<size_t> s;
        atomic<size_t> e;
    } tail;
};
```

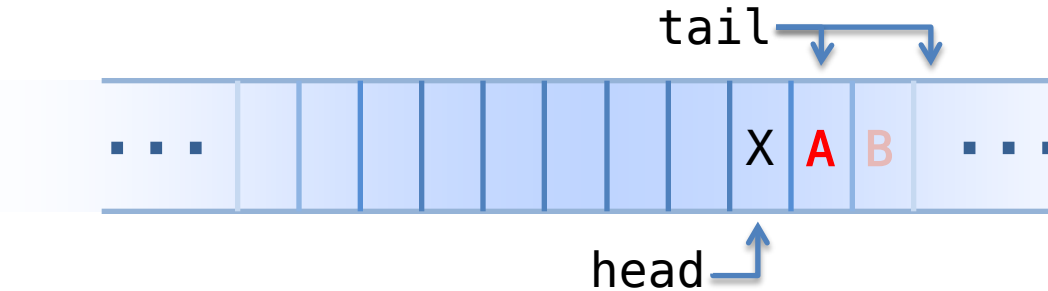




```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    if(tmp == tail.s) {
        tail.s = ...
    }
}
```

✓
THEN

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct {
        atomic<size_t> s;
        atomic<size_t> e;
    } tail;
};
```



```

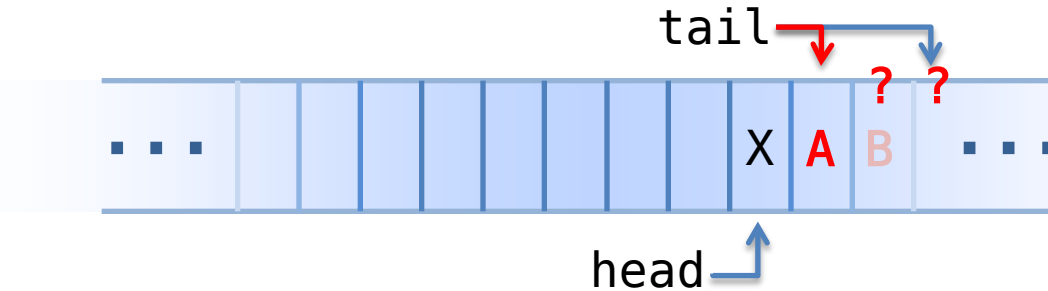
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    if(tmp == tail.s) {
        tail.s = ???
    }
}

```

```

class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct {
        atomic<size_t> s;
        atomic<size_t> e;
    } tail;
};

```




```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    if(tmp == tail.s) {
        tail.s = ???
    }
}
```

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct {        atomic<size_t> s;
                  atomic<size_t> e;
    } tail;
};
```

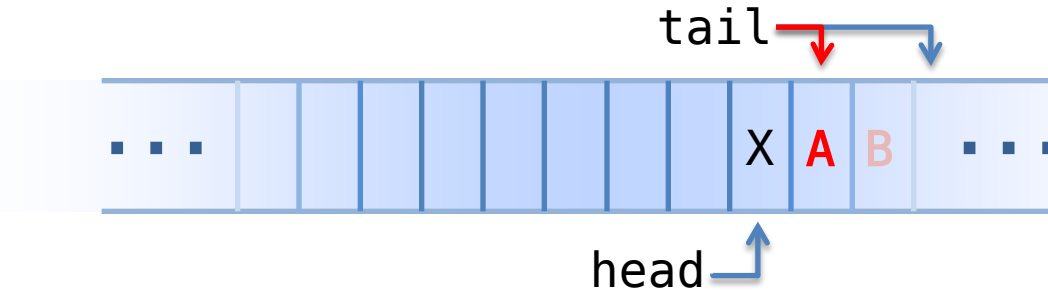
Compromise...

Queue of int -> Queue of int != 0



```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    if(tmp == tail.s) {
        tail.s = ???
    }
}
```

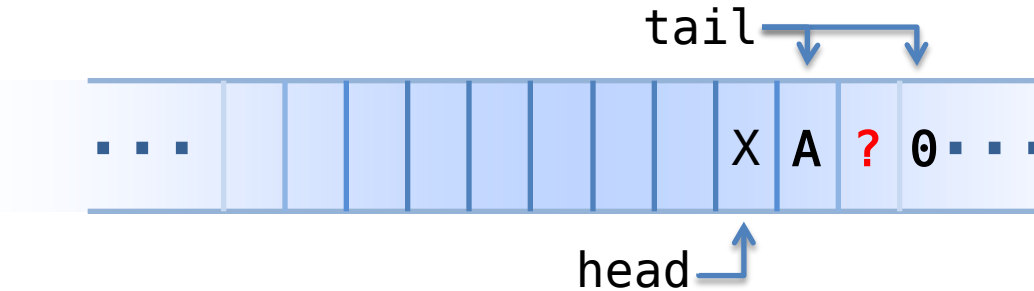
```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct {
        atomic<size_t> s;
        atomic<size_t> e;
    } tail;
};
```





```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    if(tmp == tail.s) {  
        do  
            tail.s++;  
        while (buffer[tail.s]);  
    }  
}
```

```
class Queue {  
    int buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
            atomic<size_t> e;  
    } tail;  
};
```



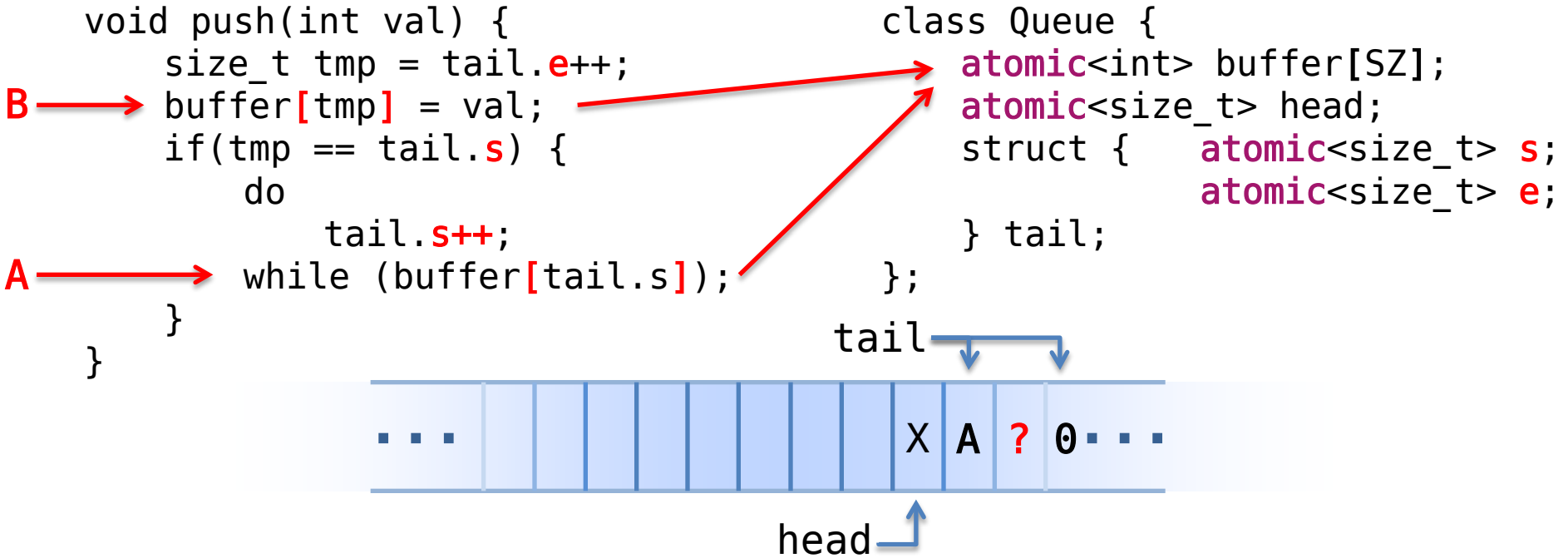


```
void push(int val) {  
    size_t tmp = tail.e++;  
    B → buffer[tmp] = val;  
    if(tmp == tail.s) {  
        do  
            tail.s++;  
        A → while (buffer[tail.s]);  
    }  
}
```

```
class Queue {  
    int buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```

tail

head





```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    if(tmp == tail.s) {  
        do  
            tail.s++;  
        while (buffer[tail.s]);  
    }  
}
```

THEN**THEN**

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```

tail

head



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    if(tmp == tail.s) {  
        do  
            tail.s++;  
        while (buffer[tail.s]);  
    }  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```

tail

head



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    B → if(tmp == tail.s) {  
        do  
            A → tail.s++;  
        while (buffer[tail.s]);  
    }  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```

tail

head



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    if(tmp == tail.s) {  
        do  
            tail.s++;  
        while (buffer[tail.s]);  
    }  
}
```

B →
A →

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```

tail

head



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    if(tmp == tail.s) {  
        do  
            CAS(tail.s, tmp, tmp+1);  
        while (buffer[++tmp]);  
    }  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```

tail

head



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    if(tmp == tail.s) {  
        do  
            CAS(tail.s, tmp, tmp+1);  
        while (buffer[++tmp]);  
    }  
}
```

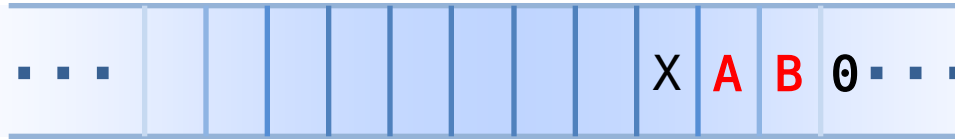
```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```

same

B
A

tail

head





```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```

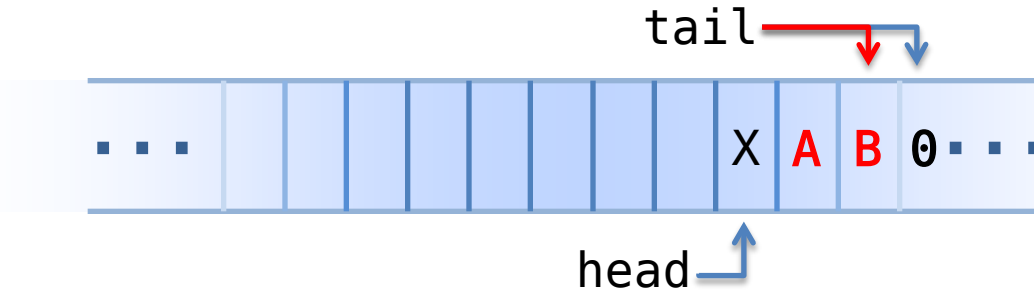
tail

head



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    bool r;  
    do  
        r = CAS(tail.s, tmp, tmp+1);  
    while (r && buffer[++tmp]);  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```

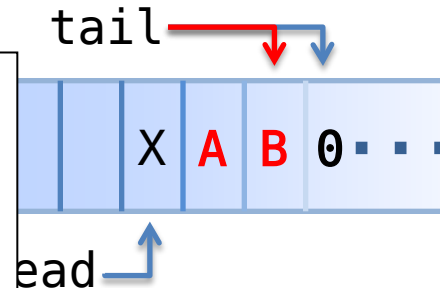




```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    bool r;  
    do  
        r = CAS(tail.s, tmp, tmp+1);  
    while (r && buffer[++tmp]);  
}
```

```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

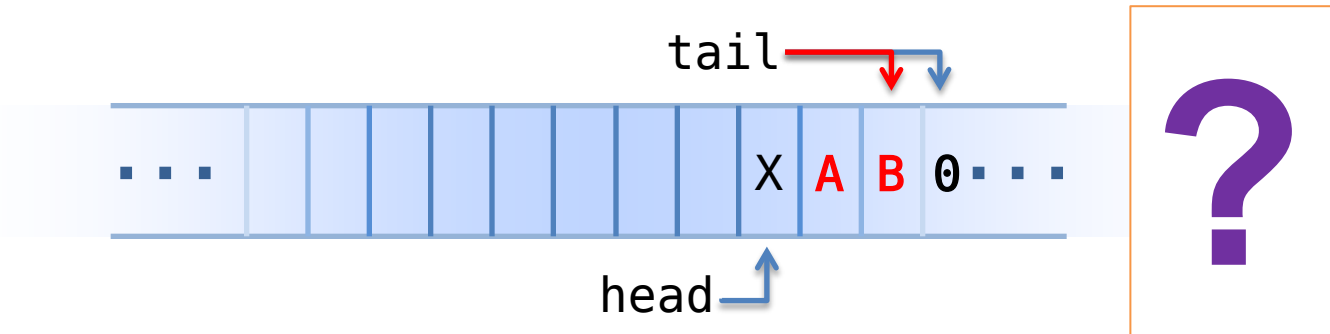
```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```





```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```

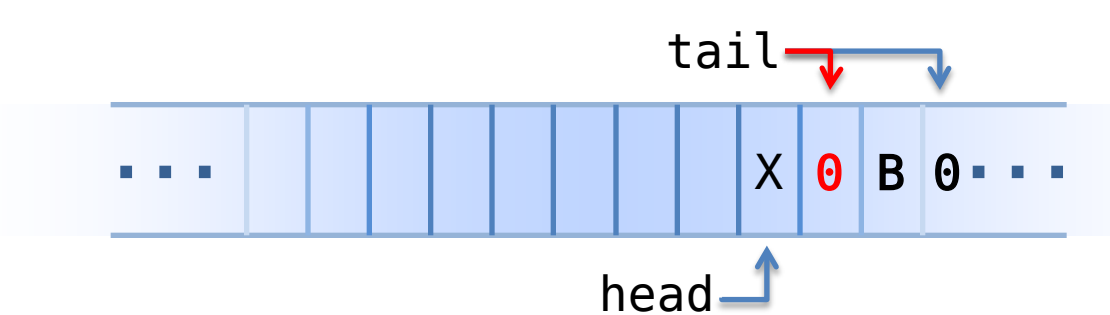




```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

A → **PAUSE**

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```

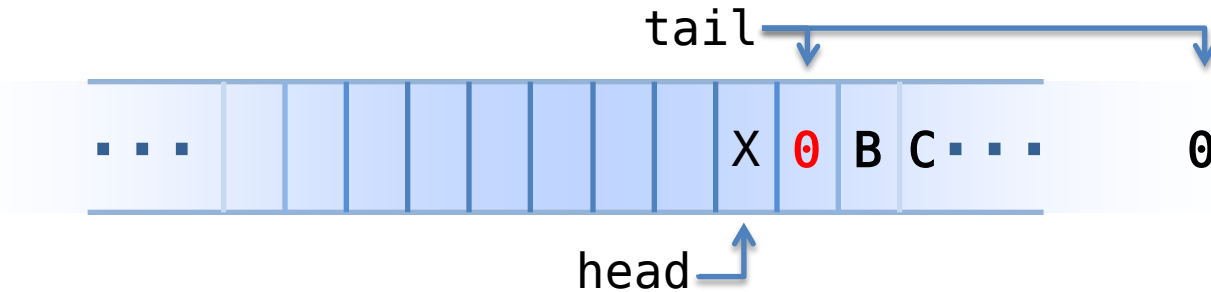




```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

A → **PAUSE**

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```

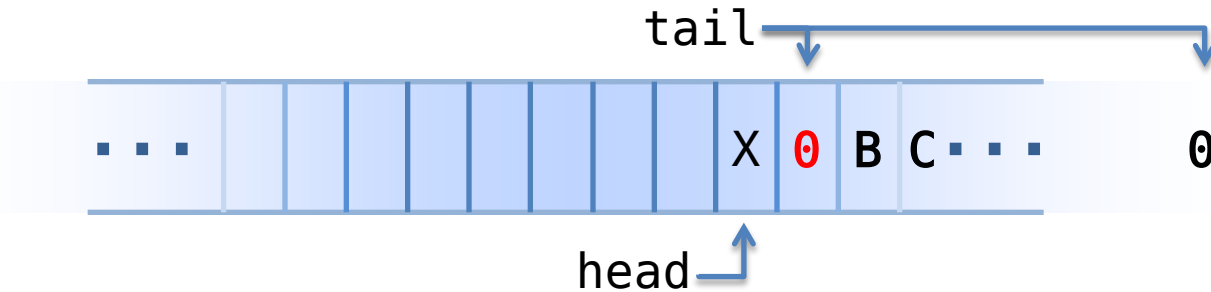




```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

A → **PAUSE**

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```



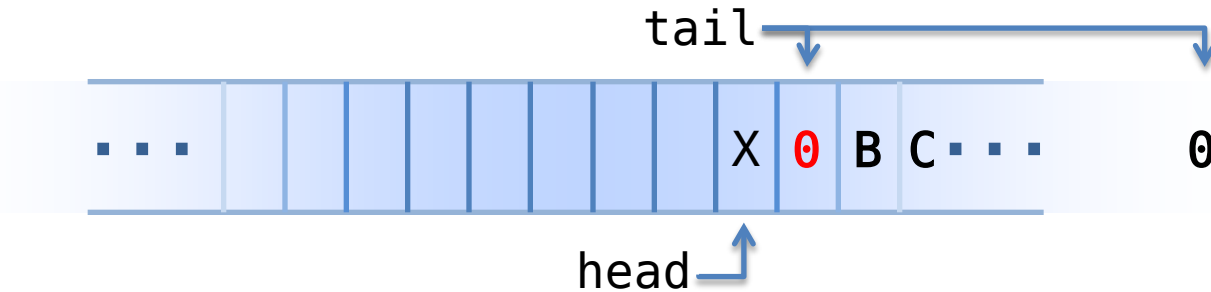
OK ?



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

A → **PAUSE**

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```



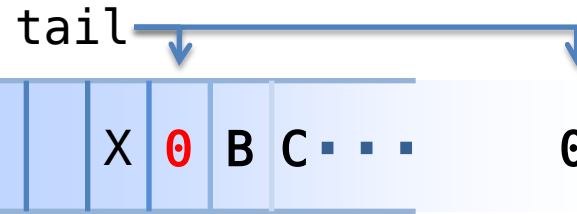
lock-free ?



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

A → **PAUSE**

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```



head ↑

```
int pop() {  
    if/while(!(head < tail.s))  
        return/wait;  
    ...  
}
```

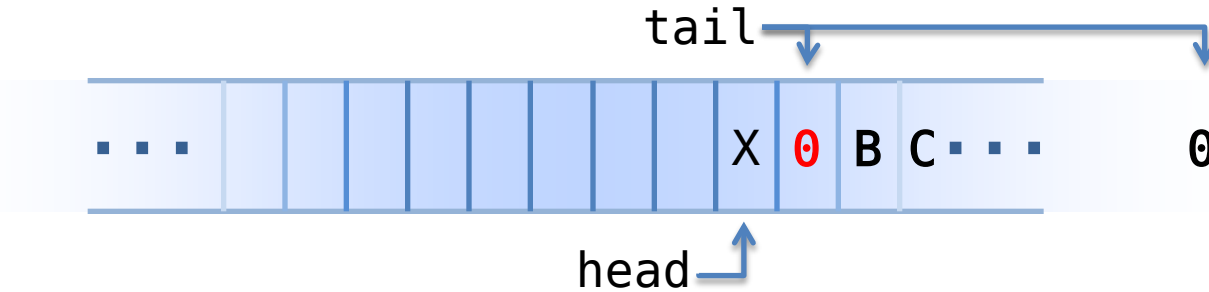
lock-free ?



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

A → **PAUSE**

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```



```
int pop() {  
    if/while(!(head < tail.s))  
        return/wait;  
    ...  
}
```

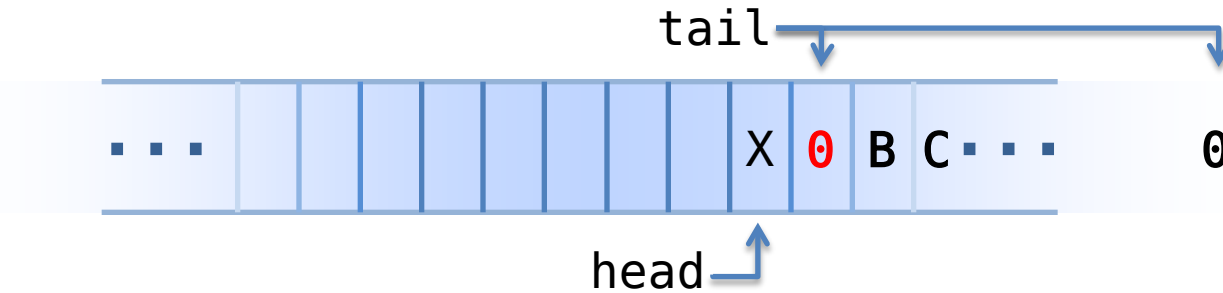
“block-free” ?



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

A → **PAUSE**

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```



```
int pop() {  
    if/while(  
        retur  
    ...  
}
```

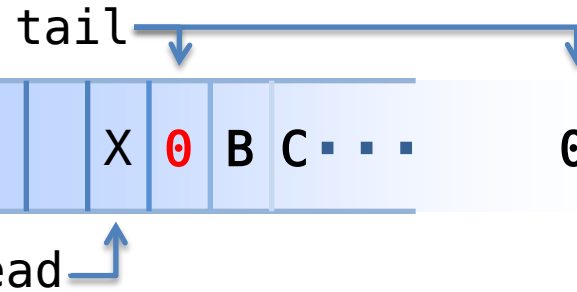
An algorithm is **lock-free** if at all times **at least one thread** is guaranteed to be **making progress**.



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

A → **PAUSE**

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```



```
int pop() {  
    if/  
    ...  
}
```

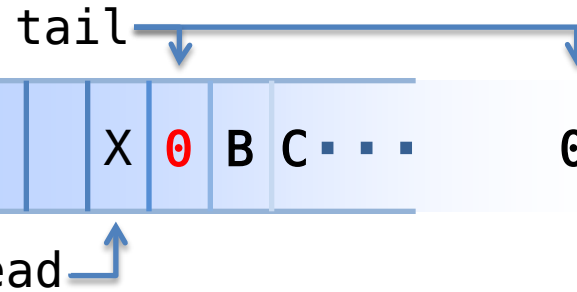
If I suspended a certain thread at the worst time, for a long time or forever, do bad things happen?
Yes -> not lockfree.



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

A → **PAUSE**

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```



```
int pop() {  
    if/while(!(head < tail.s))  
        return/wait;  
    ...  
}
```

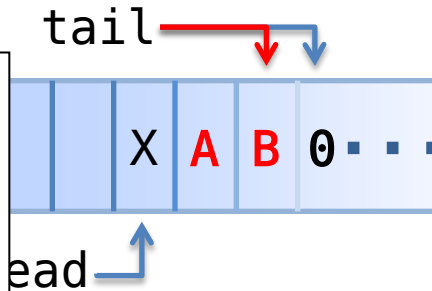
!= lock-free



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    bool r;  
    do  
        r = CAS(tail.s, tmp, tmp+1);  
    while (r && buffer[++tmp]);  
}
```

```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e;  
    } tail;  
};
```



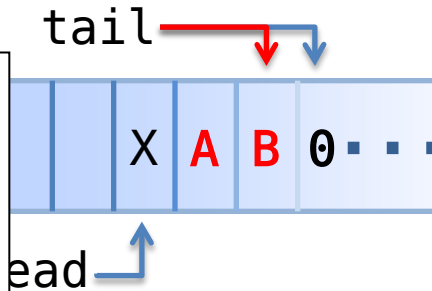


```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    bool r;  
    do  
        r = CAS(tail.s, tmp, tmp+1);  
    while (r && buffer[++tmp]);  
}
```

A →
PAUSE

```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e;  
    } tail;  
};
```





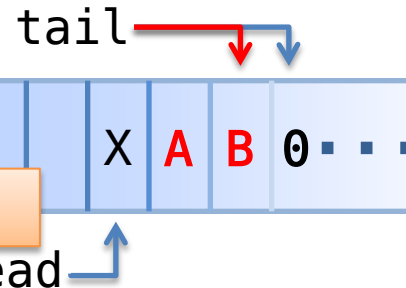
```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    bool r;  
    do  
        r = CAS(tail.s, tmp, tmp+1);  
    while (r && buffer[++tmp]);  
}
```

!= lock-free**A →**
PAUSE

```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

~= lock-free

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```

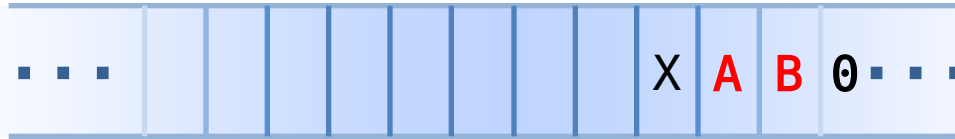




```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    bool r;  
    tmp = tail.s;  
    while (buffer[tmp]) {  
        r = tail.s.CAS(tmp, tmp+1);  
        if (r) tmp++;  
    }  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```

tail



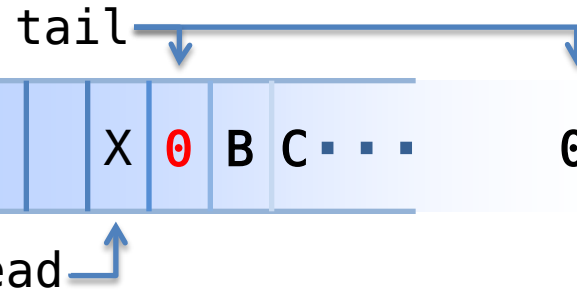
head



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    bool r;  
    tmp = tail.s;  
    while (buffer[tmp]) {  
        r = tail.s.CAS(tmp, tmp+1);  
        if (r) tmp++;  
    }  
}
```

A →
PAUSE

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```



```
int pop() {  
    if/while(!(head < tail.s))  
        return/wait;  
    ...  
}
```

!= lock-free



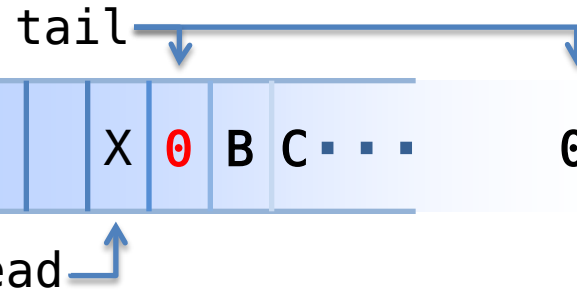




```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    bool r;  
    tmp = tail.s;  
    while (buffer[tmp]) {  
        r = tail.s.CAS(tmp, tmp+1);  
        if (r) tmp++;  
    }  
}
```

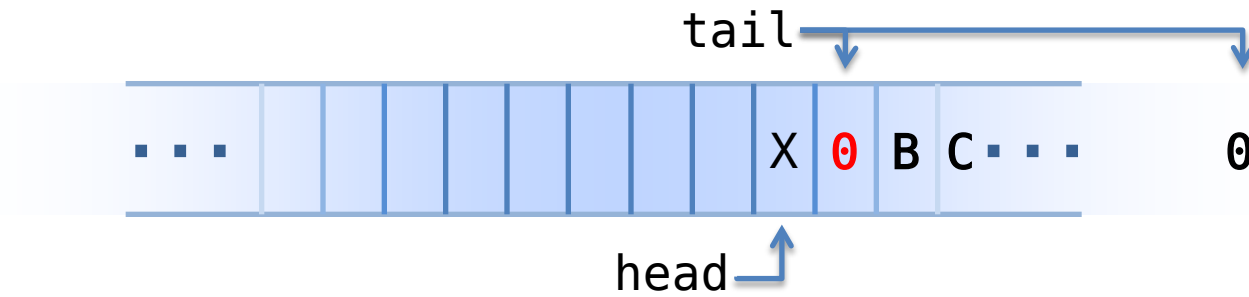
A →
PAUSE

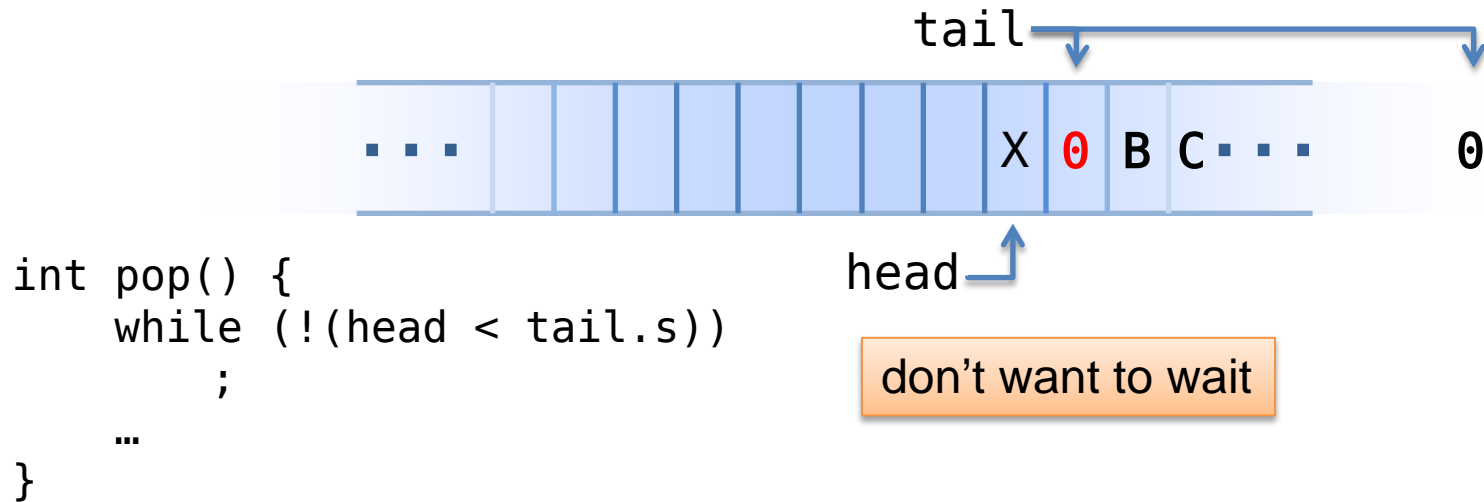
```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```

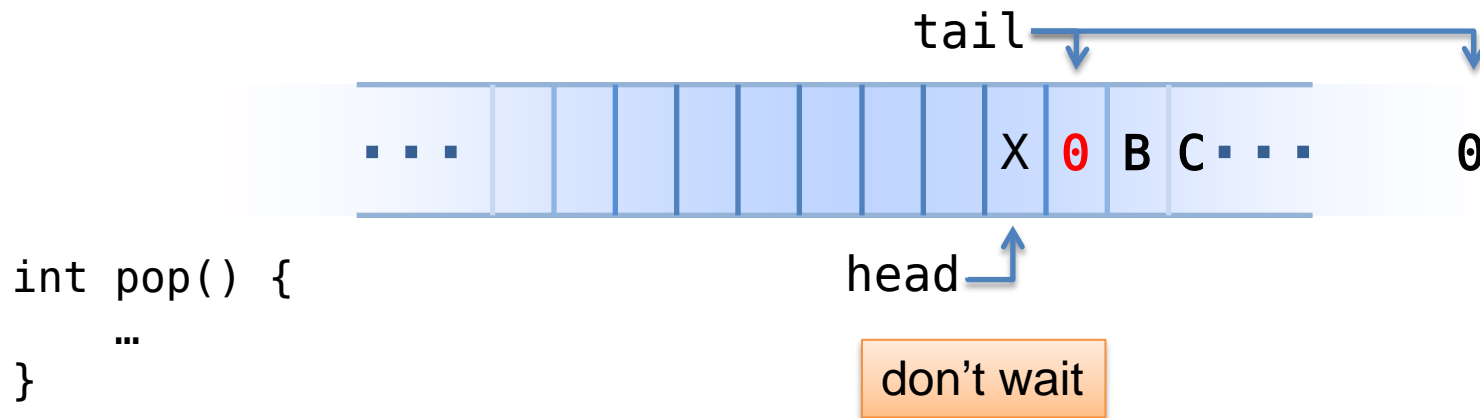


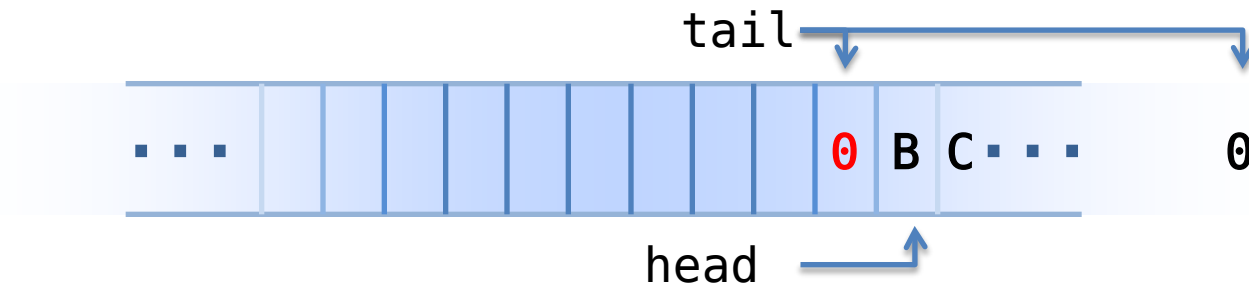
```
int pop() {  
    while  
    ;  
    ...  
}
```

An algorithm is **lock-free** if at all times **at least one thread** is guaranteed to be **making progress**.

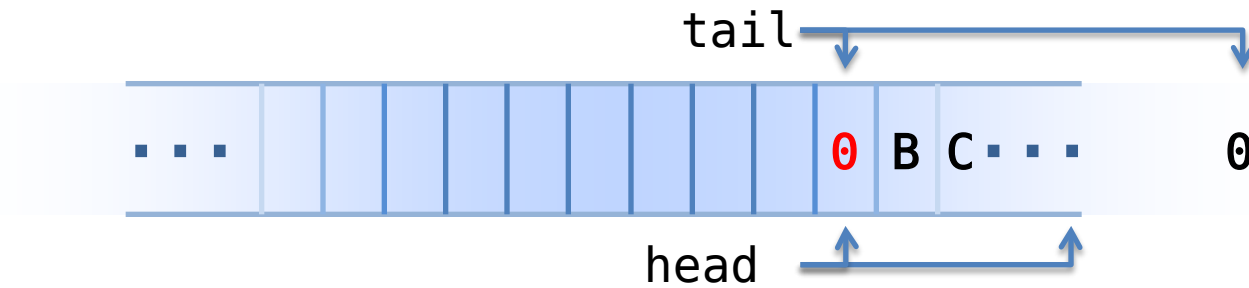






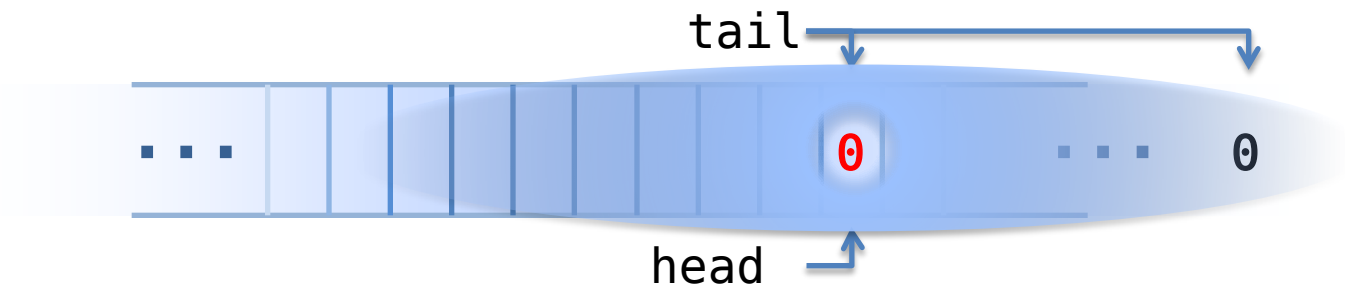


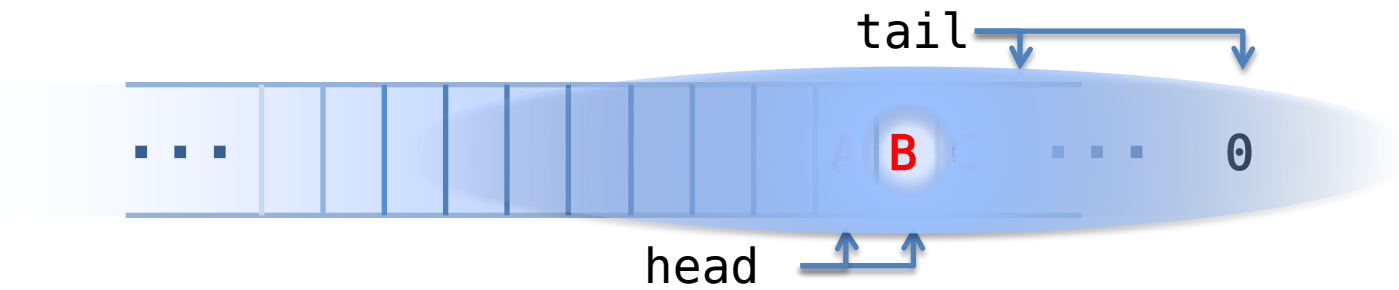
don't wait! (?)



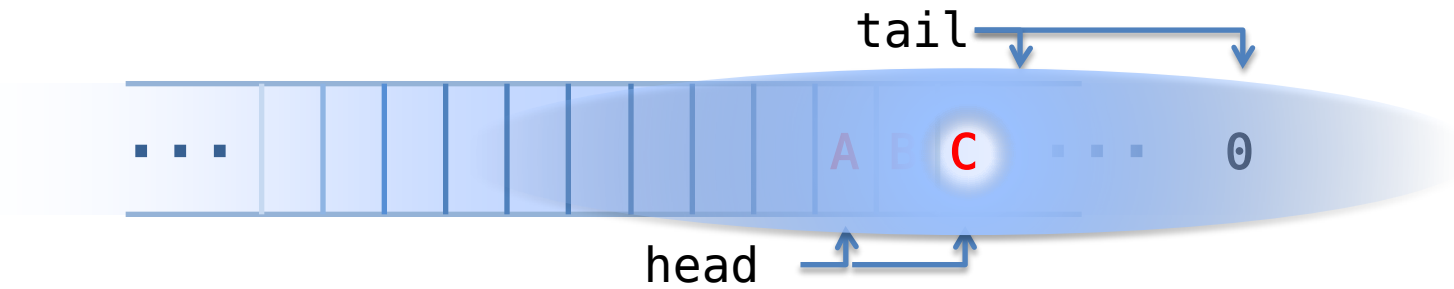
come back later (when?)



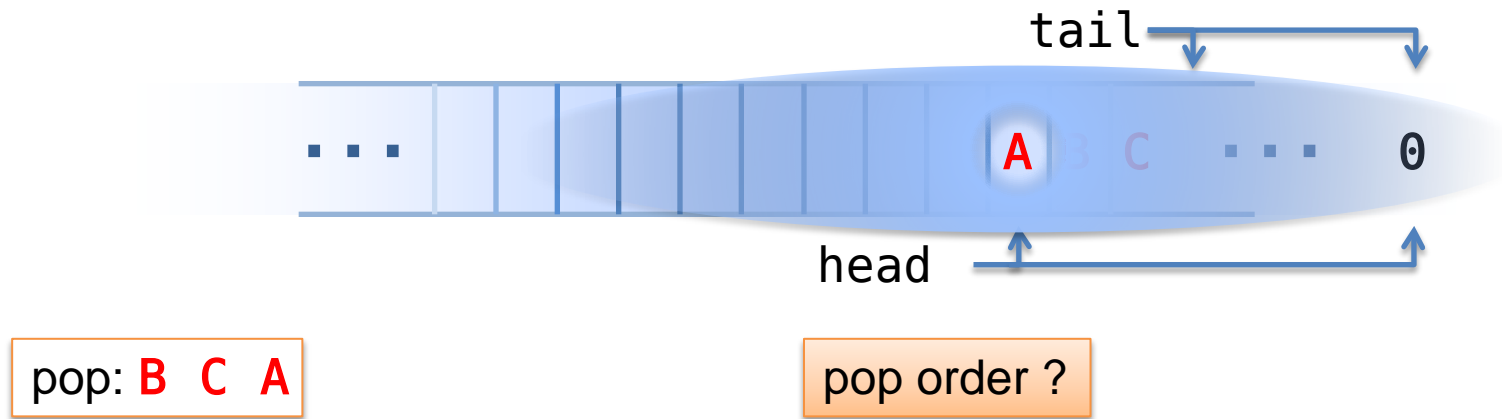


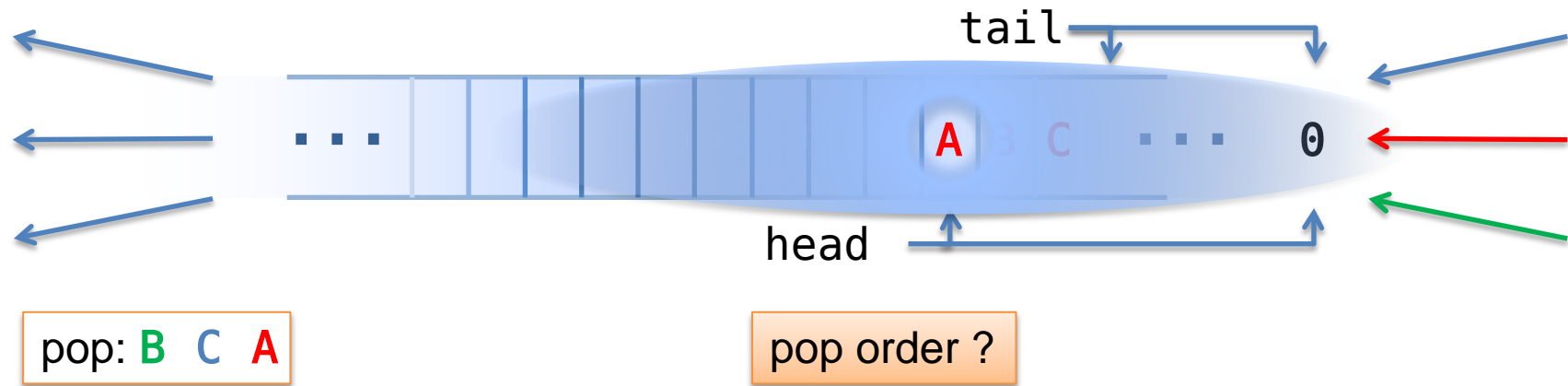


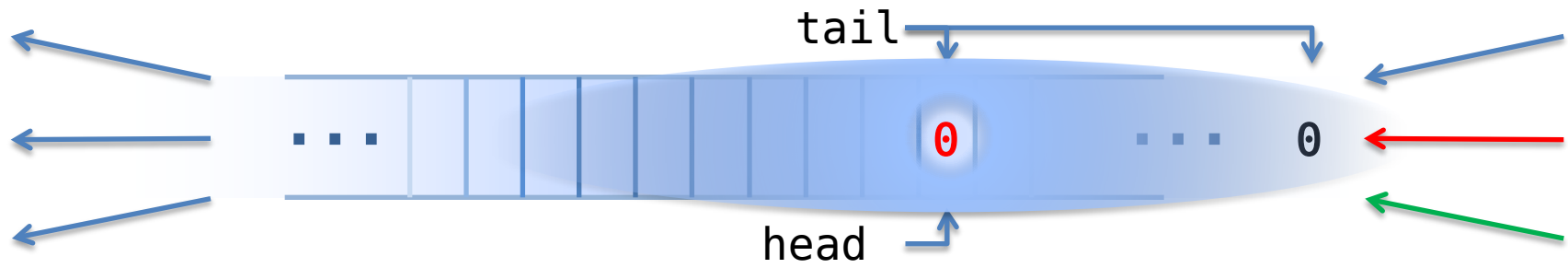
pop: **B**

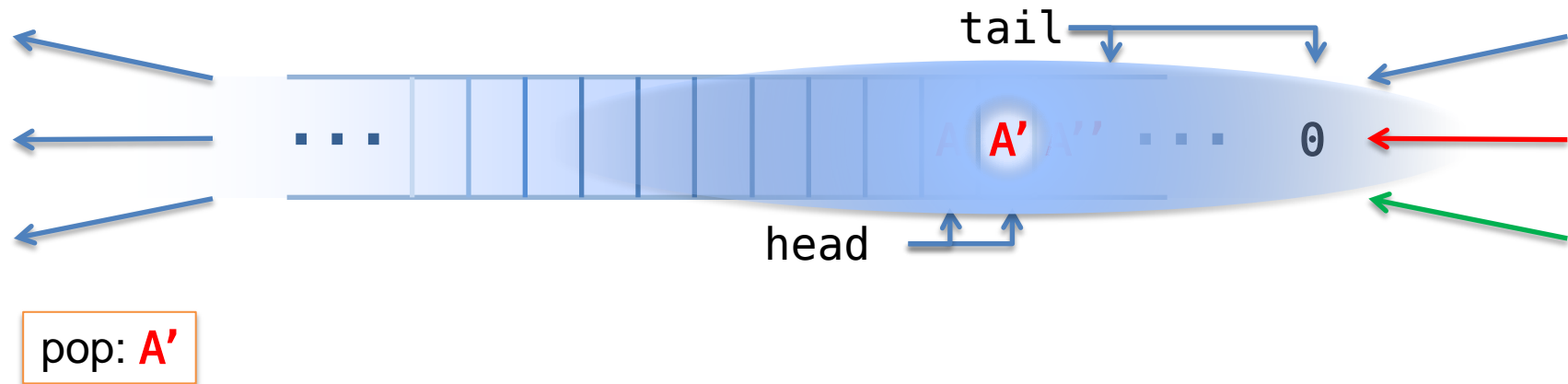


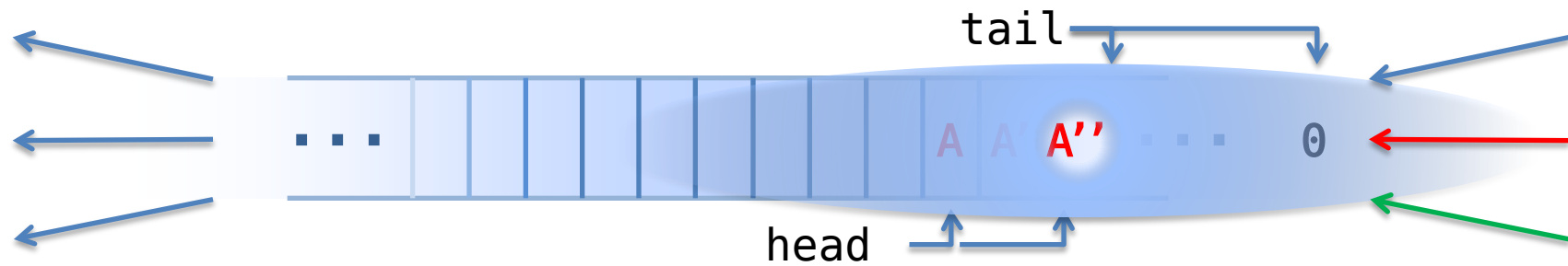
pop: **B** **C**



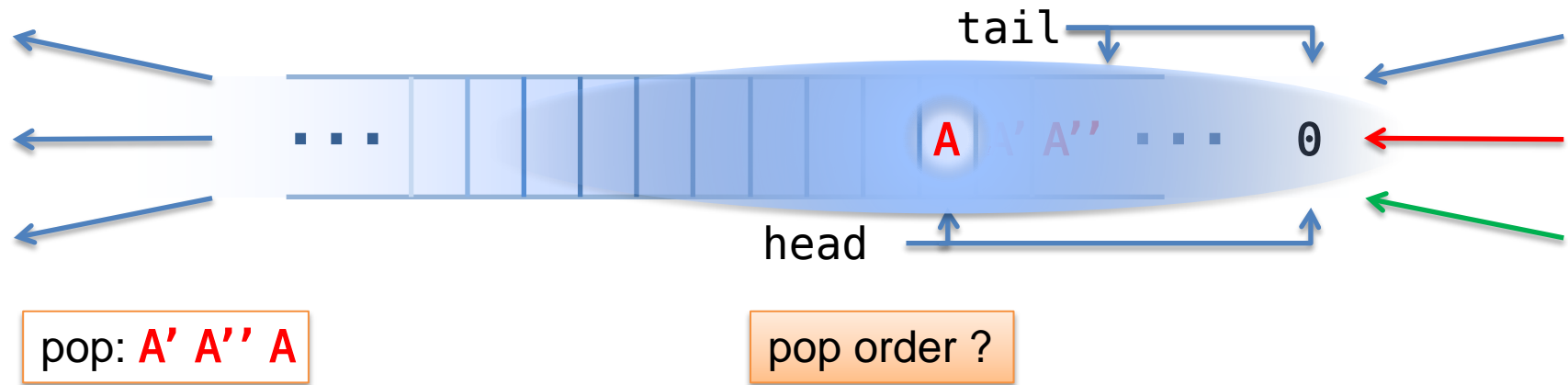


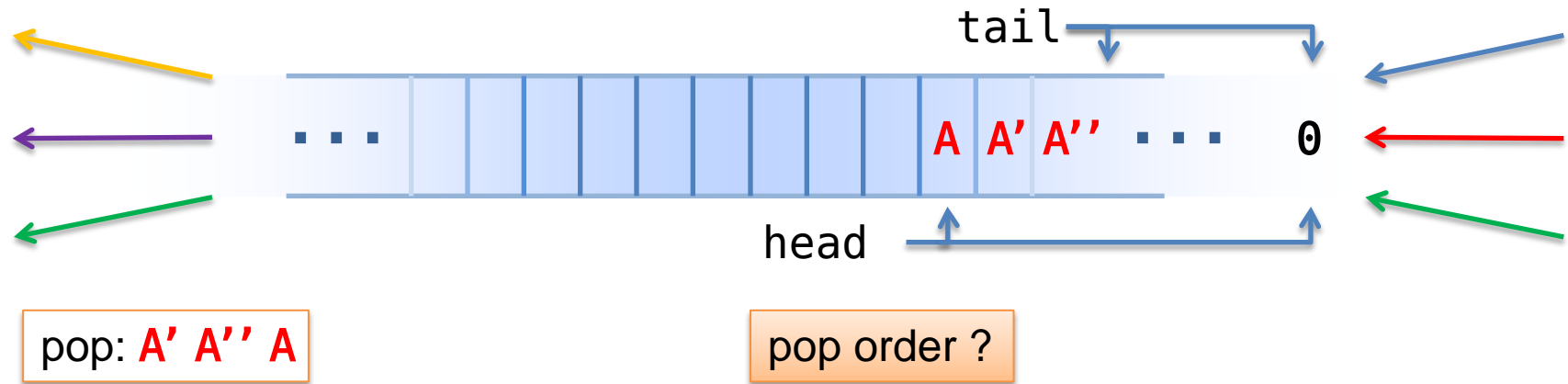


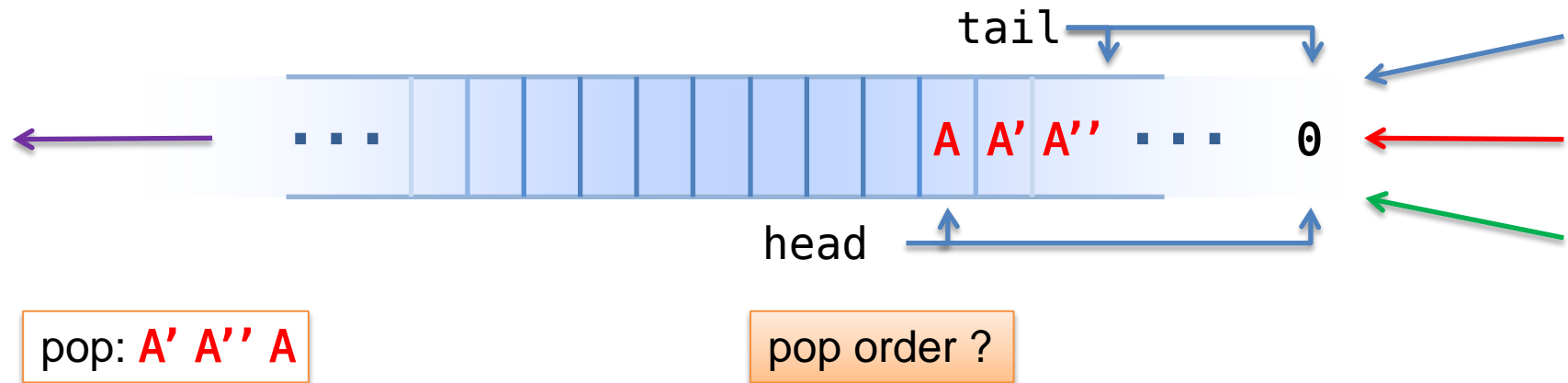


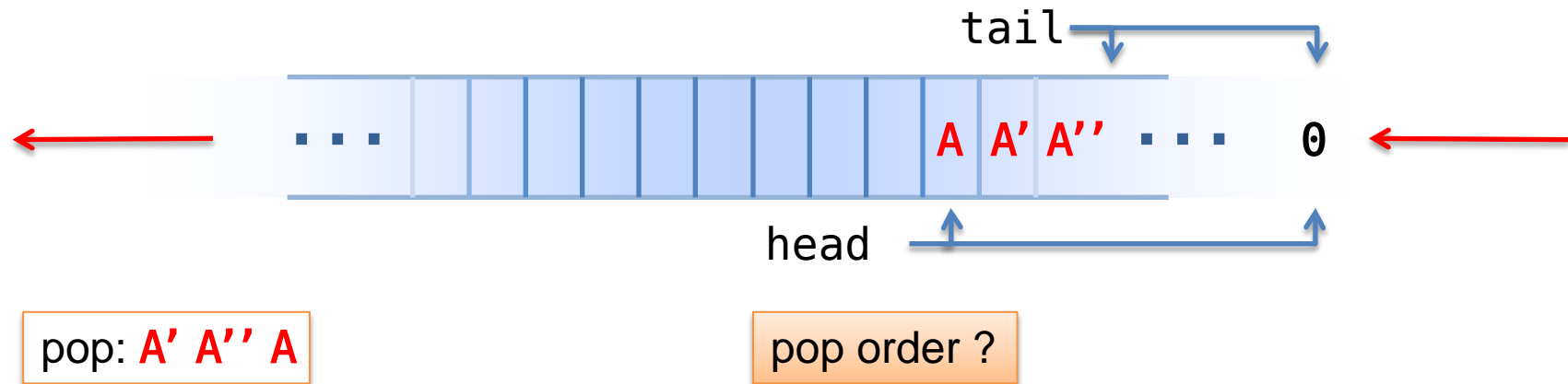


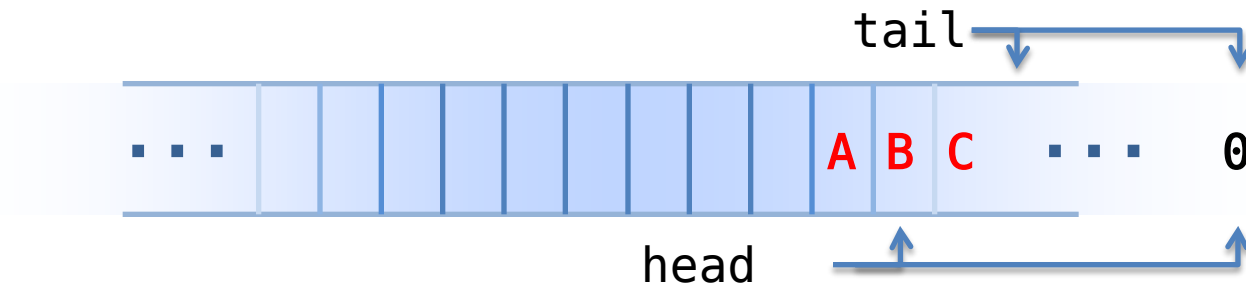
pop: **A'** **A''**







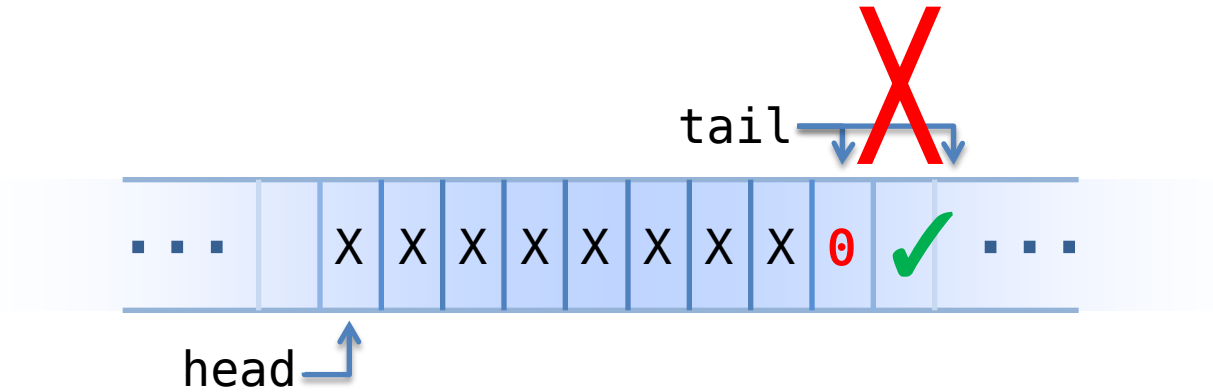


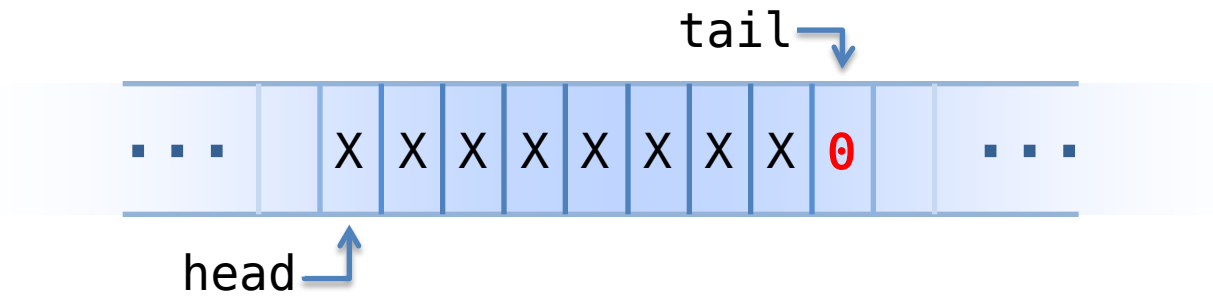


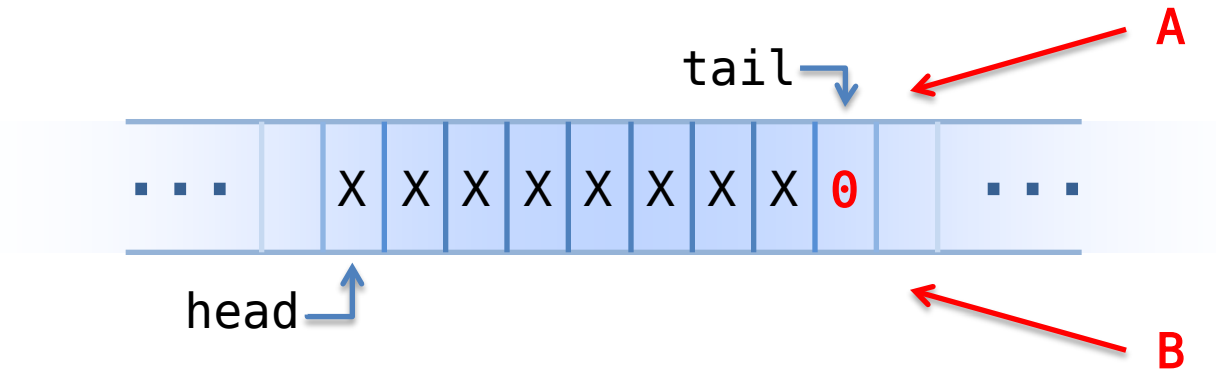
pop: **B C A ... B?**

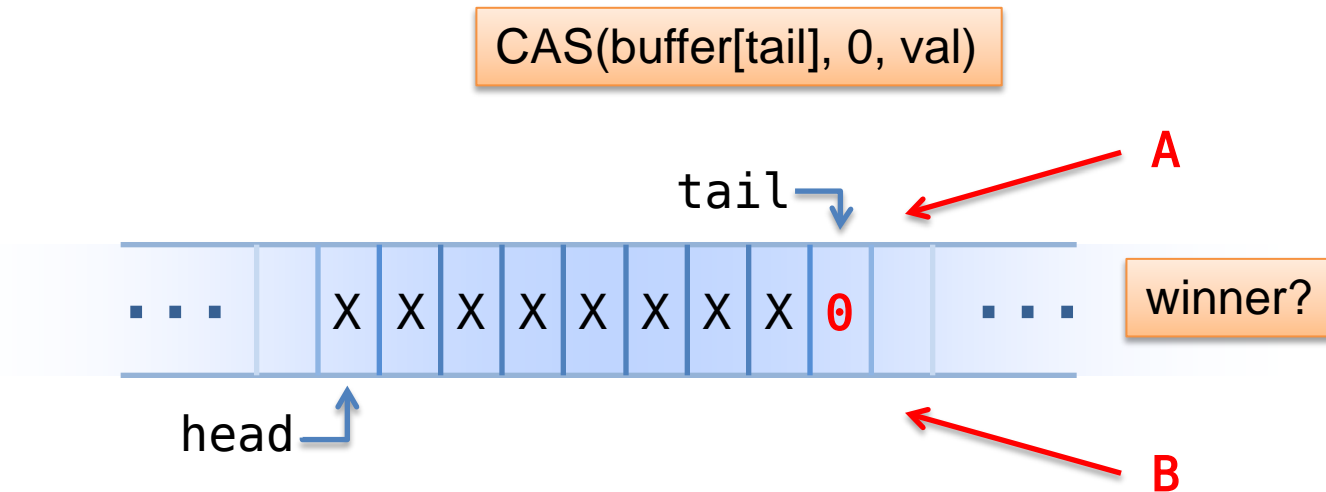
did I read B already ?

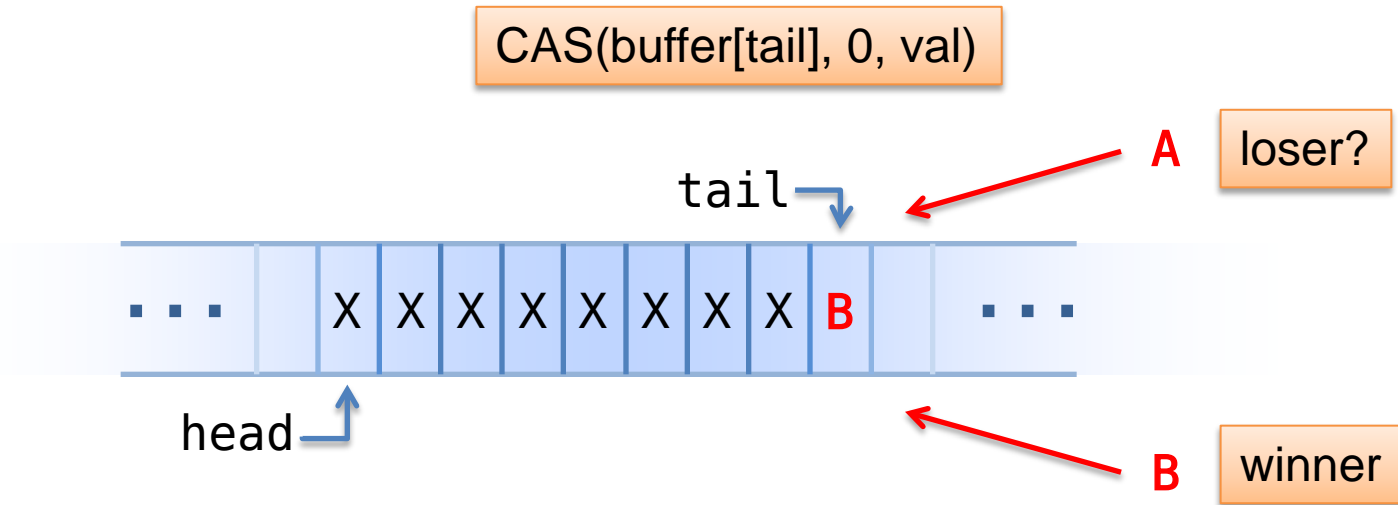






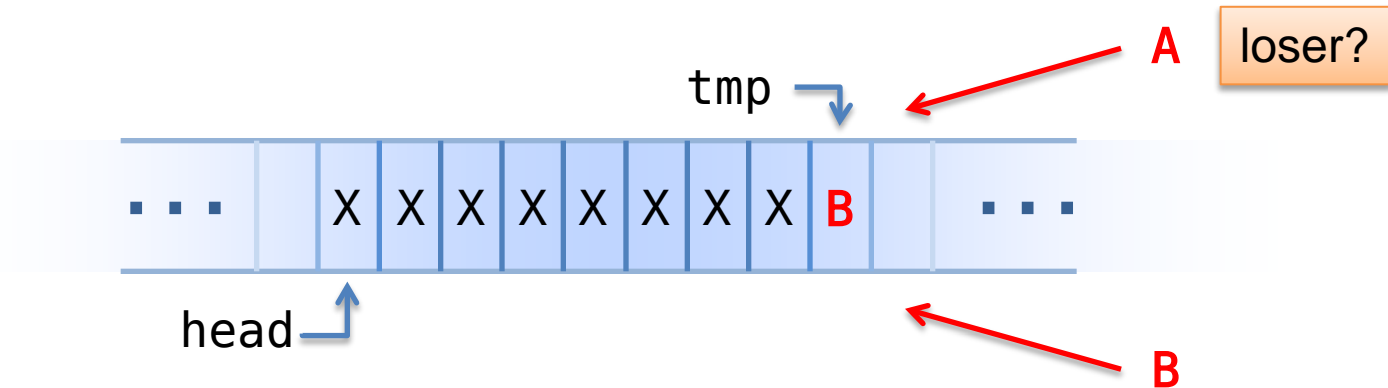








```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```





do

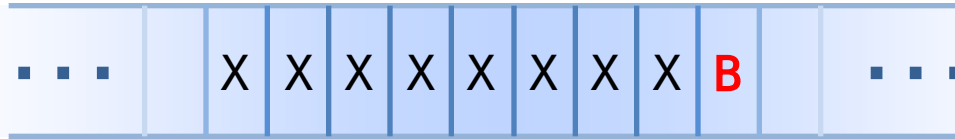
```
tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```

wait for tail?

tmp

A

loser?

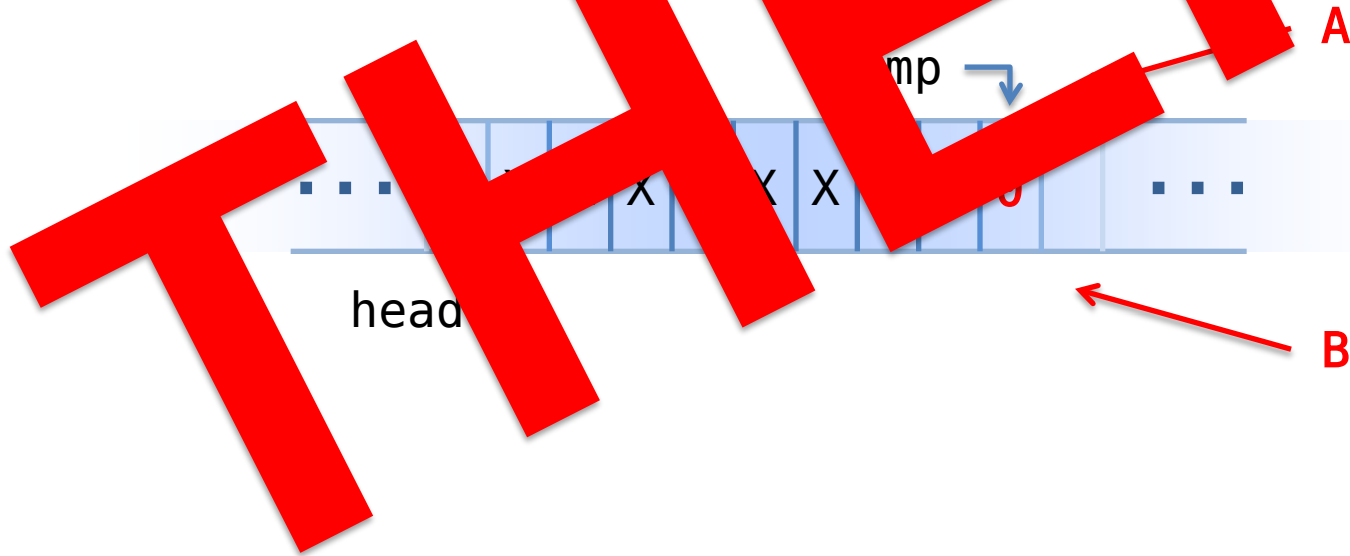


head

B

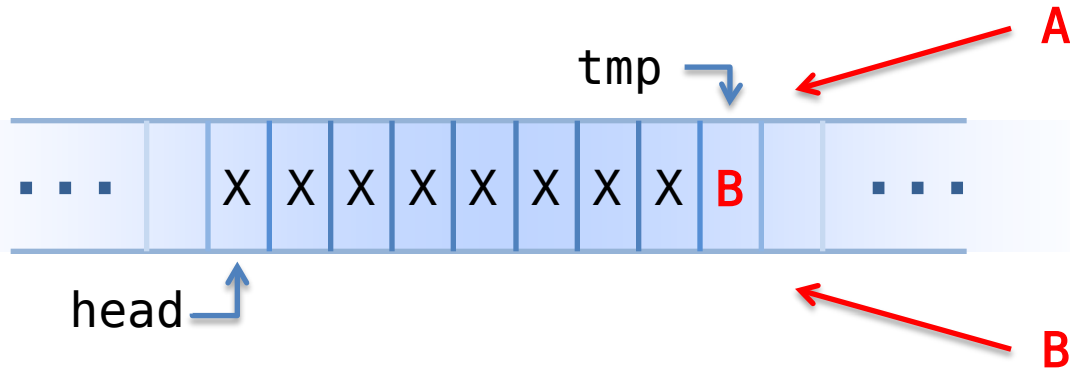


```
do { tmp = tail.load();  
    while (!CAS(buffer[tmp], 0, val) );
```



```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```

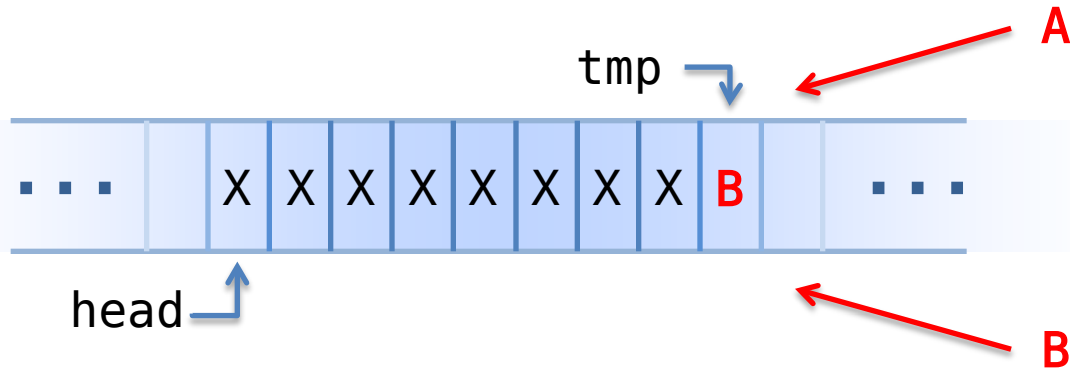
if CAS fails
THEN try again





```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```

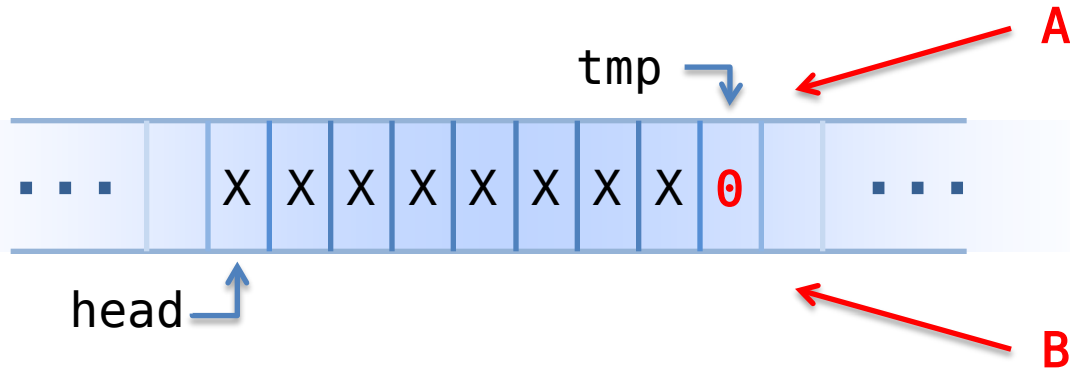
read tail
THEN read buffer





```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```

read tail
THEN read buffer





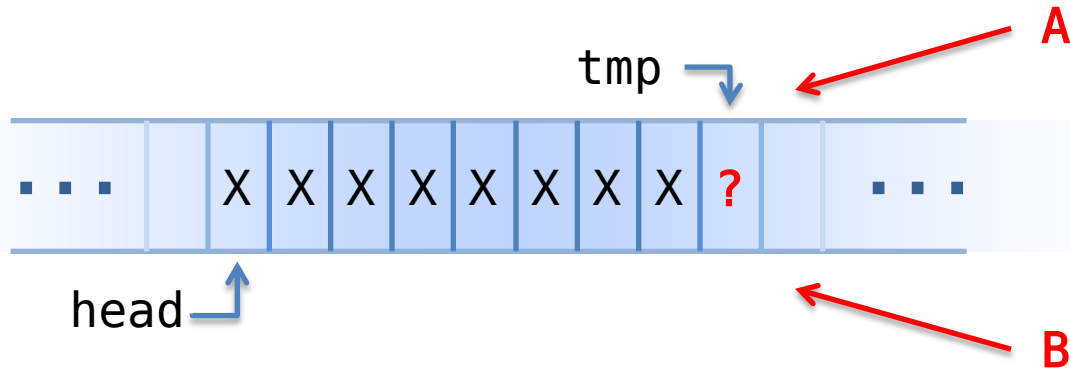
do

tmp = tail.load();

while (! CAS(buffer[tmp], 0, val));

read tail

THEN read buffer





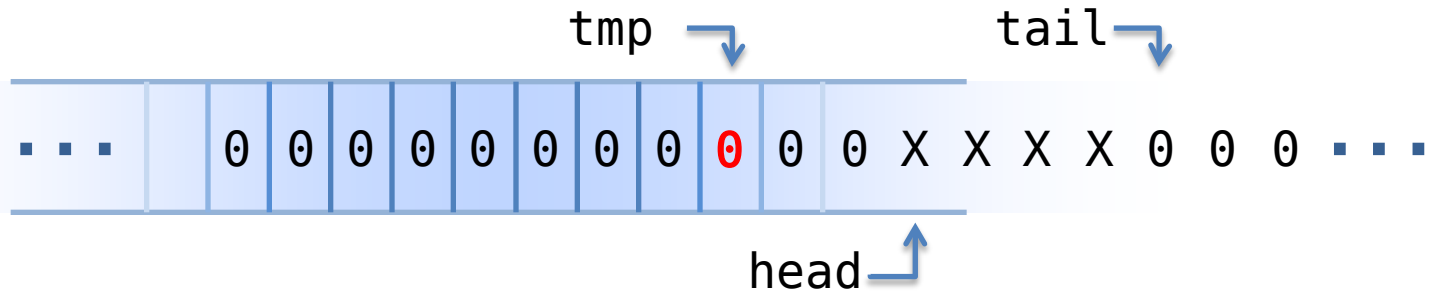
do

`tmp = tail.load();`

`while (! CAS(buffer[tmp], 0, val));`

read tail

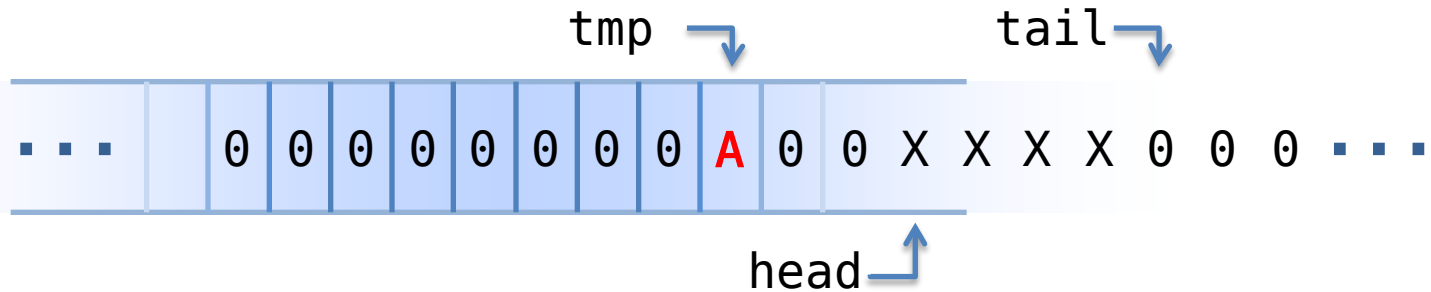
THEN read buffer





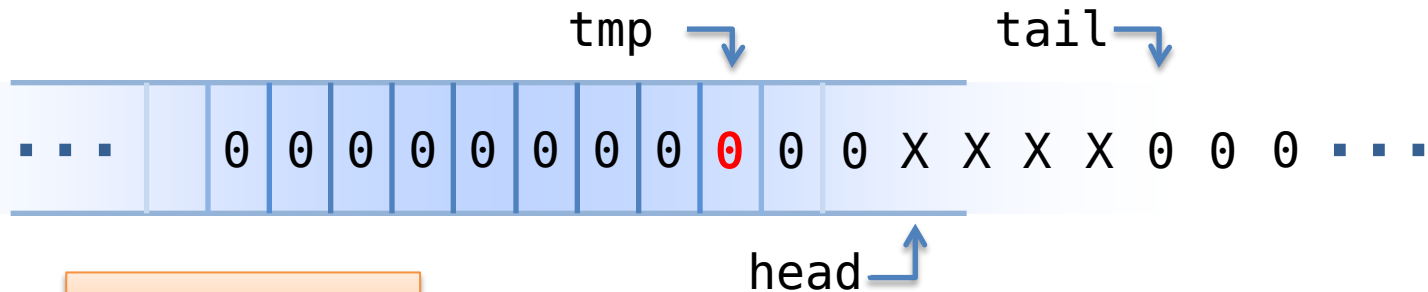
```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```

read tail
THEN read buffer





```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```

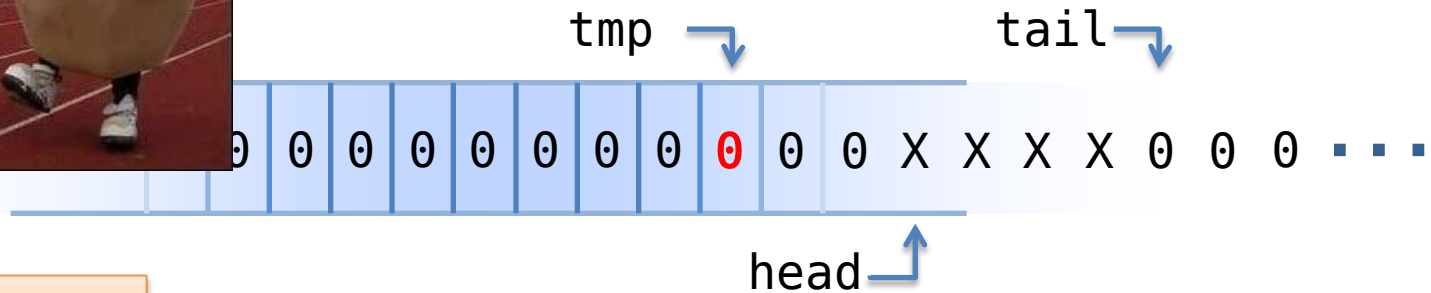


trailing zeros ?



do

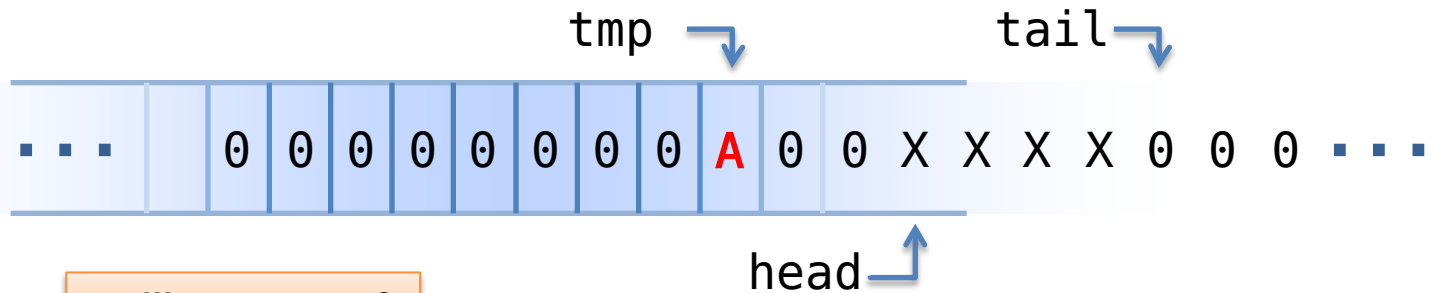
```
tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```



pop() ?



```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```



trailing zeros ?



```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```

Compromise...

Queue of int

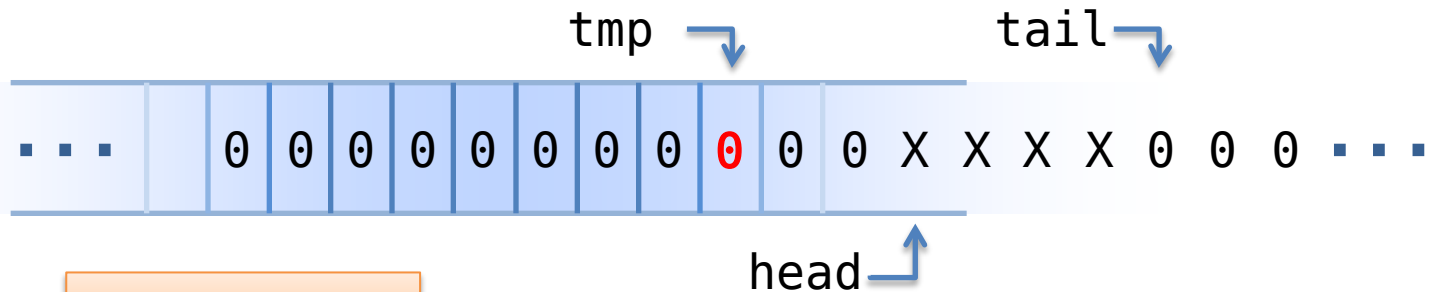
-> Queue of int != 0

-> Queue of int != 0 or 1

0 0 0 ...



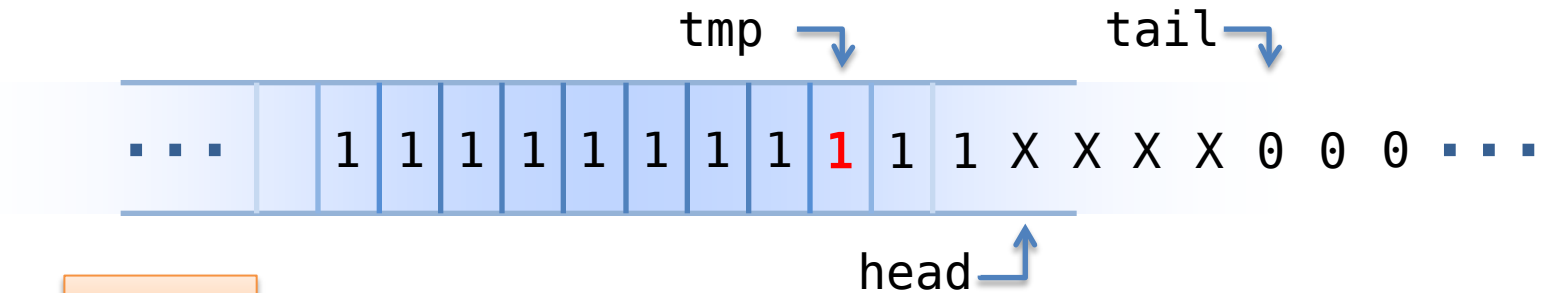
```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```



trailing zeros ?



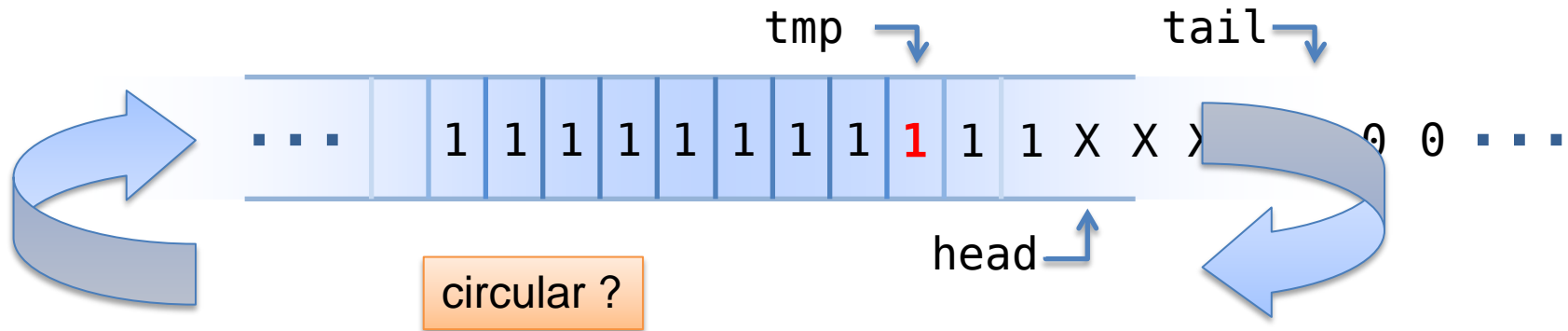
```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```



pop() ?



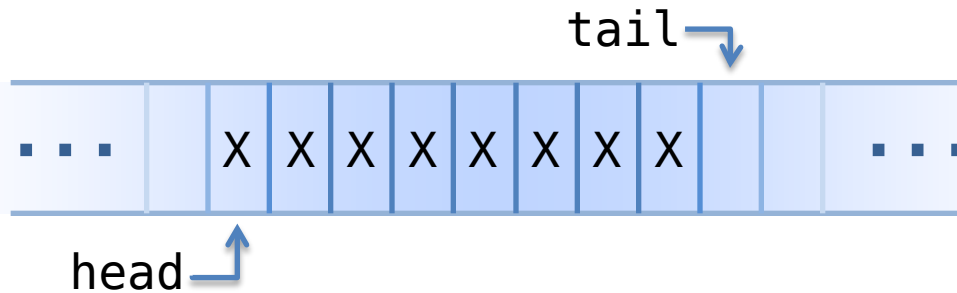
```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```





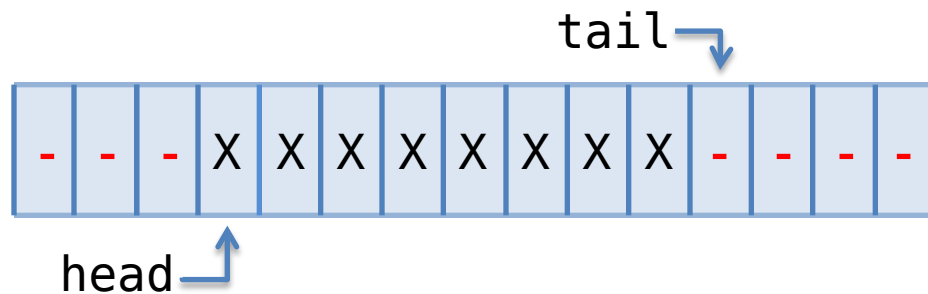


```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```



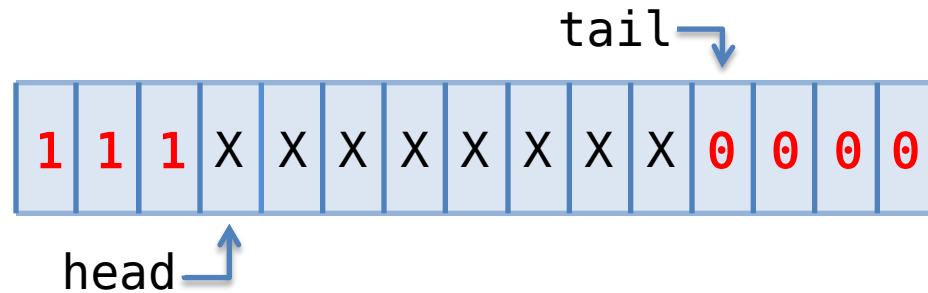


```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```





```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```

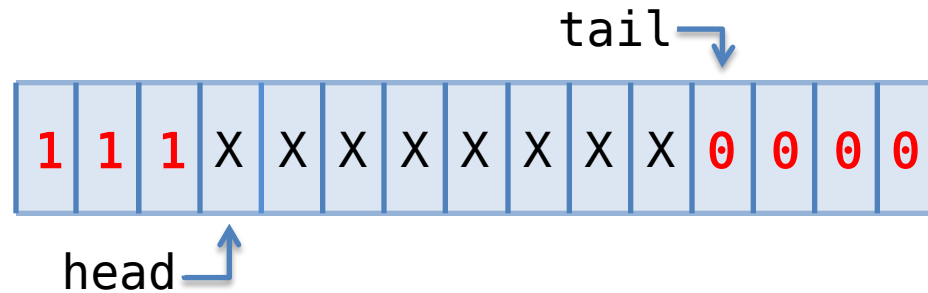




1	1	1	X	X	X	X	X	X	X	X	0	0	0	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---



```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```





```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```

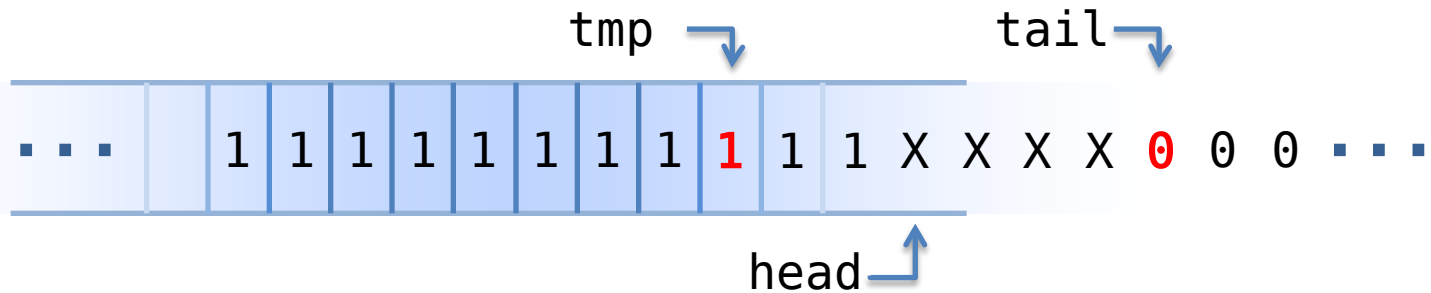
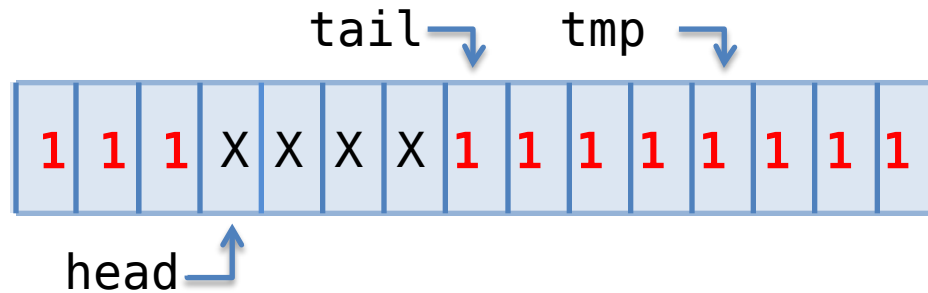




Diagram illustrating a linked list structure with 15 nodes. The nodes contain the values: X, X, X, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, X. The pointers are positioned as follows: tail points to the first '1', tmp points to the second '1', and head points to the last '1'.



```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```





```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```

Compromise...



```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```

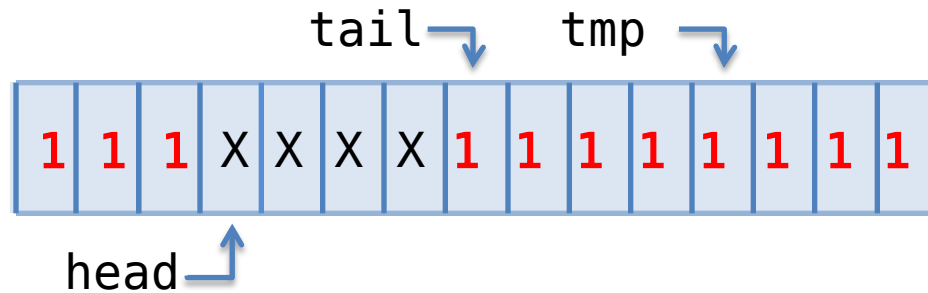
Compromise...

Queue of int

- > Queue of int != 0
- > Queue of int != 0 or 1
- > Queue of int < 0

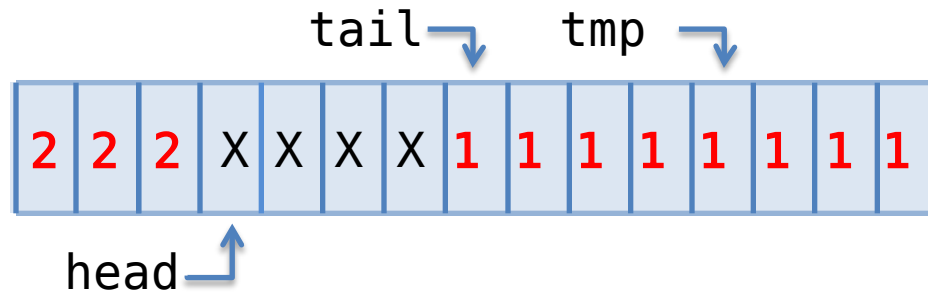


```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```



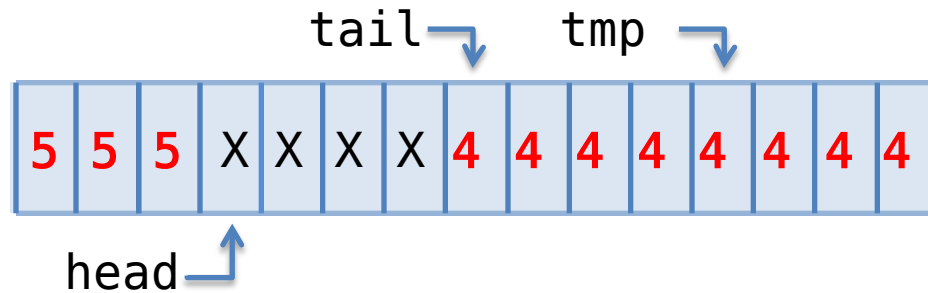


```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```



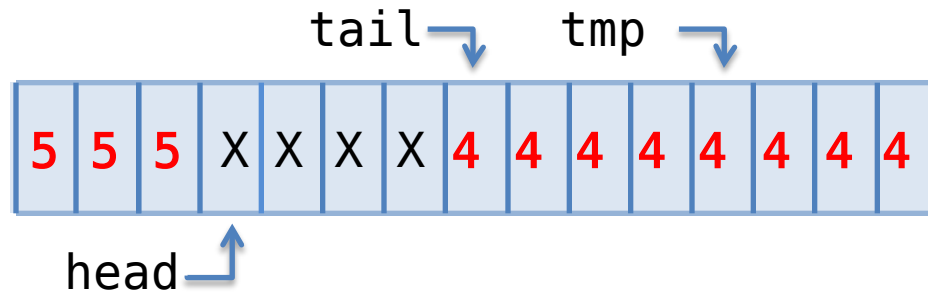


```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```



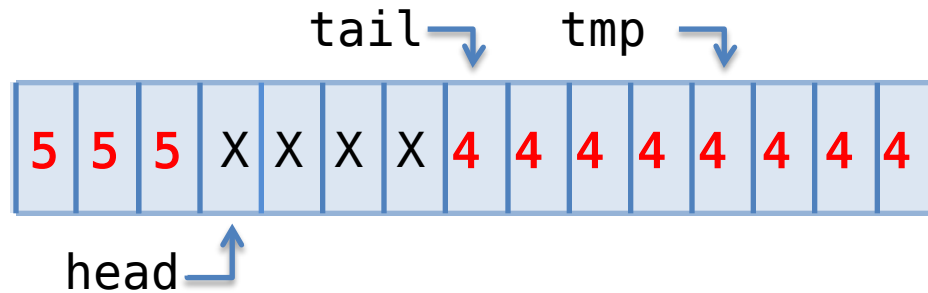


```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```



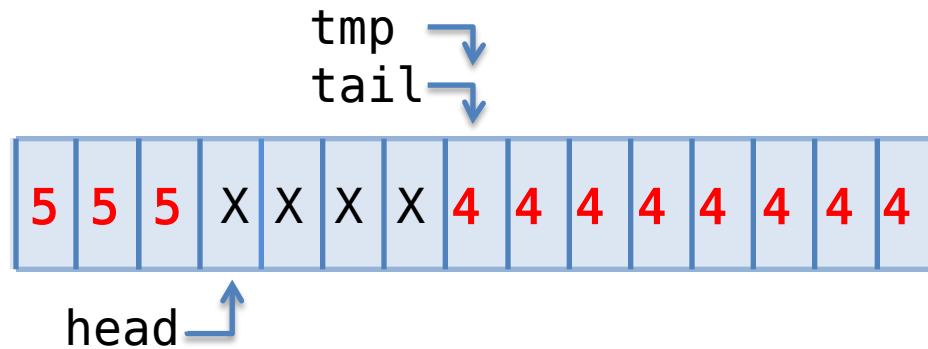


```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```



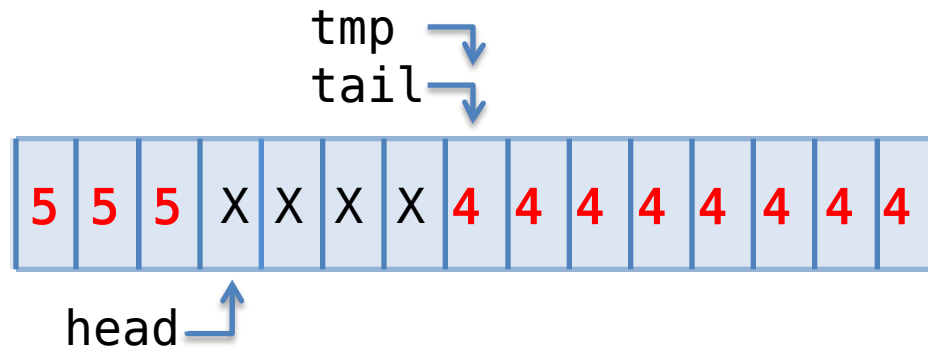


```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], 0, val) );
```





```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 4, val) );
```

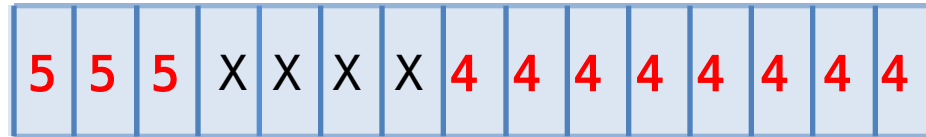




```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
    atomic<size_t> generation;  
};
```

```
do  
    tmp = t  
while (!CA
```

tmp
tail



head





MOAR

do

tmp =
(!C

```
class Queue {  
    atomic<int> buff[SZ];  
    atomic<size_t> head;  
    atomic<size_t> s;  
    atomic<size_t> e;  
    atomic<size_t> generation;  
};
```

tmp
tail



head

STATE



MOAR

do

tmp =
(!C

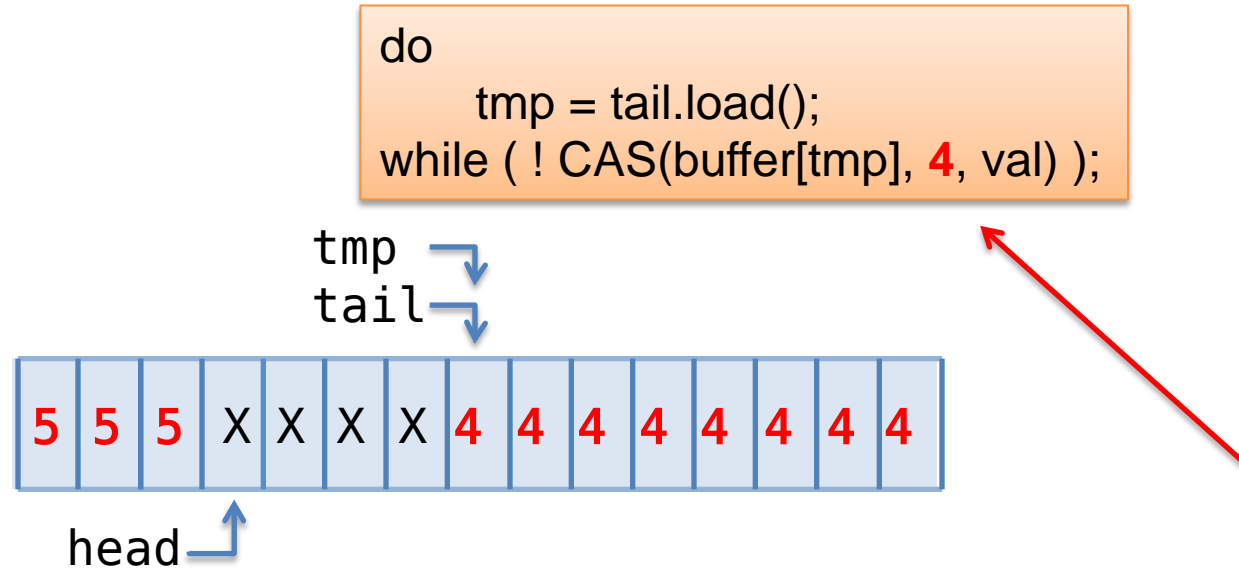
```
class Queue {  
    atomic<int> buff[SZ];  
    atomic<size_t> read;  
    atomic<size_t> s;  
    atomic<size_t> e;  
    } tail;  
    atomic<size_t> generation;  
};
```

tmp
tail



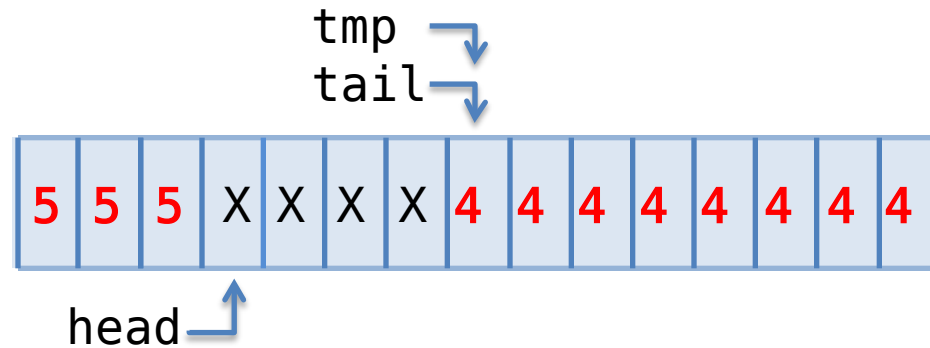
head

THEN





```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], gen(tmp), val) );
```



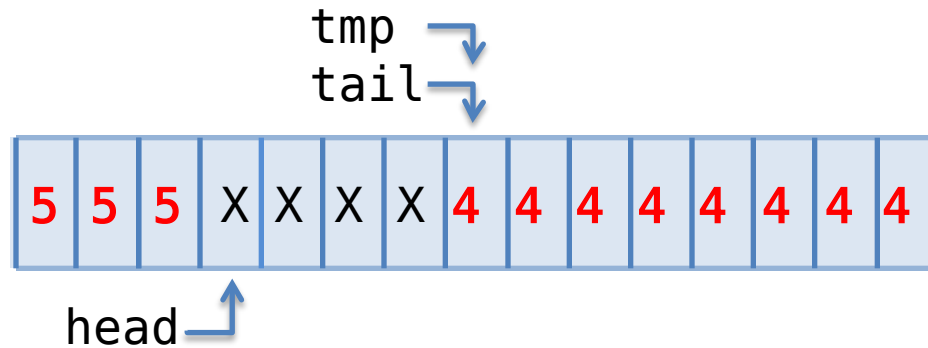

```
do  
    tmp = tail.load();  
while ( ! CAS(buffer[tmp], gen(tmp), val) );
```

tmp ↘

Compromise...

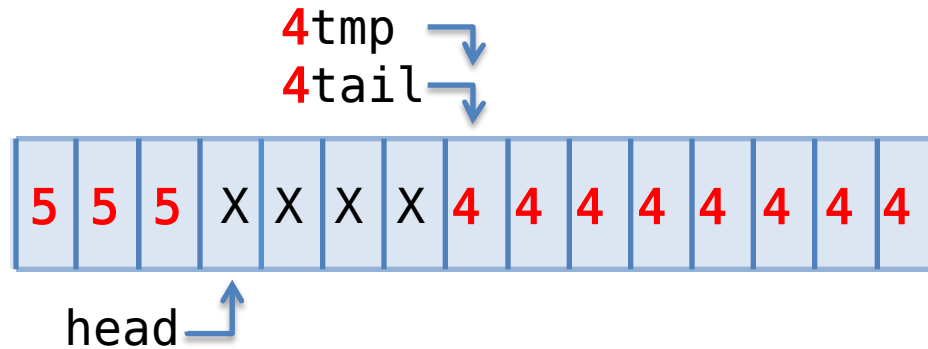


```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], gen(tmp), val) );
```



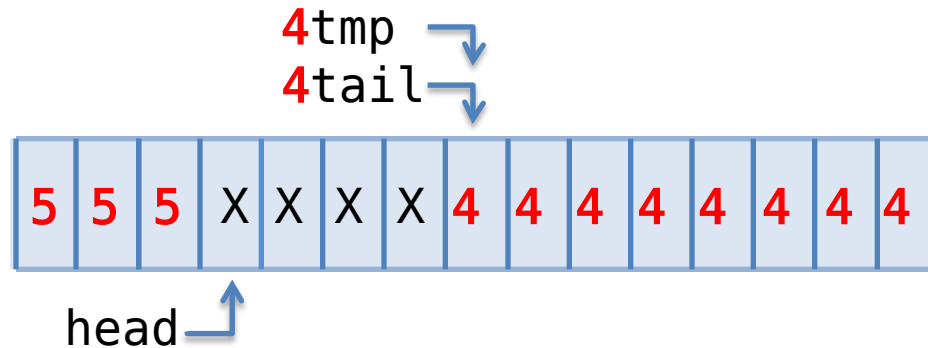


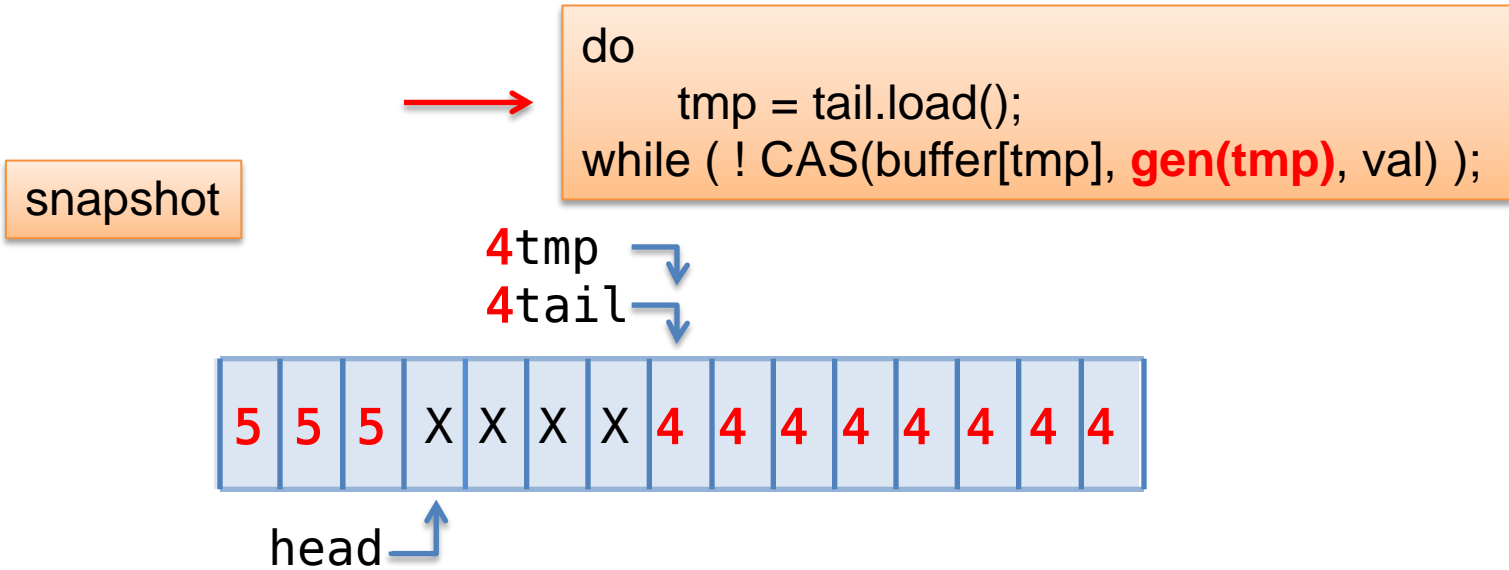
```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], gen(tmp), val) );
```

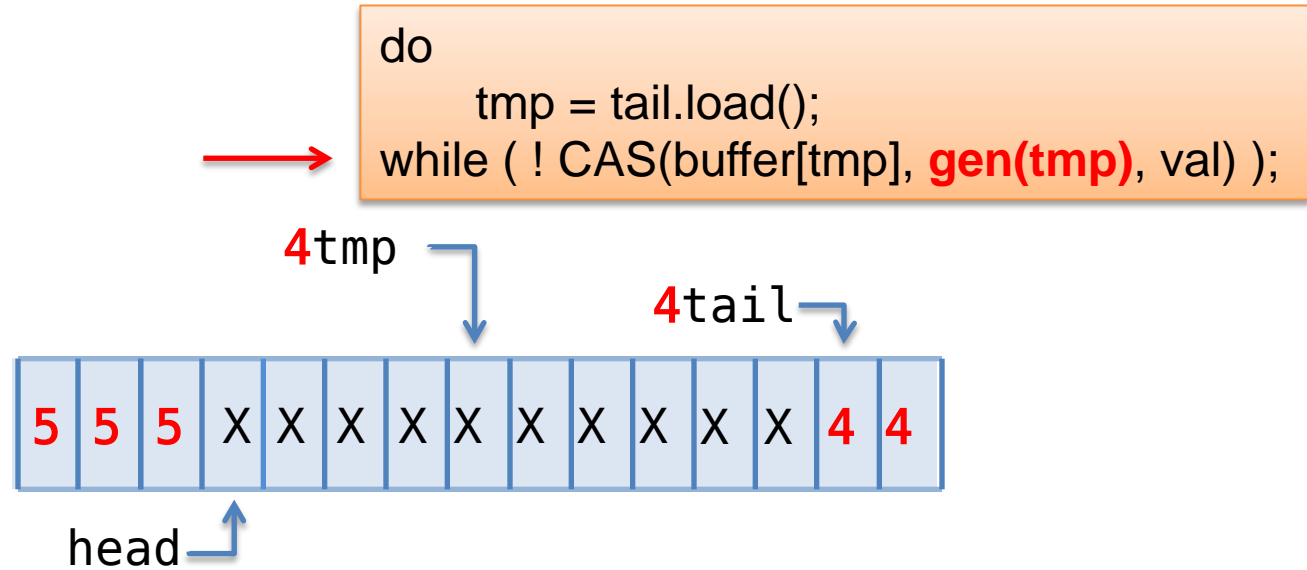


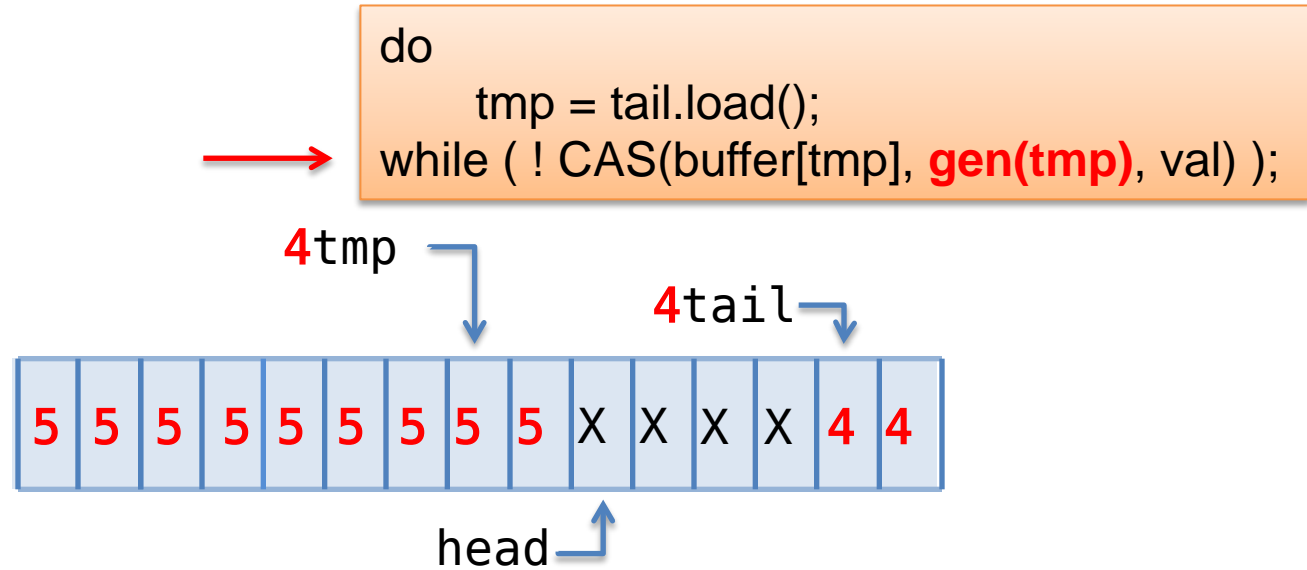


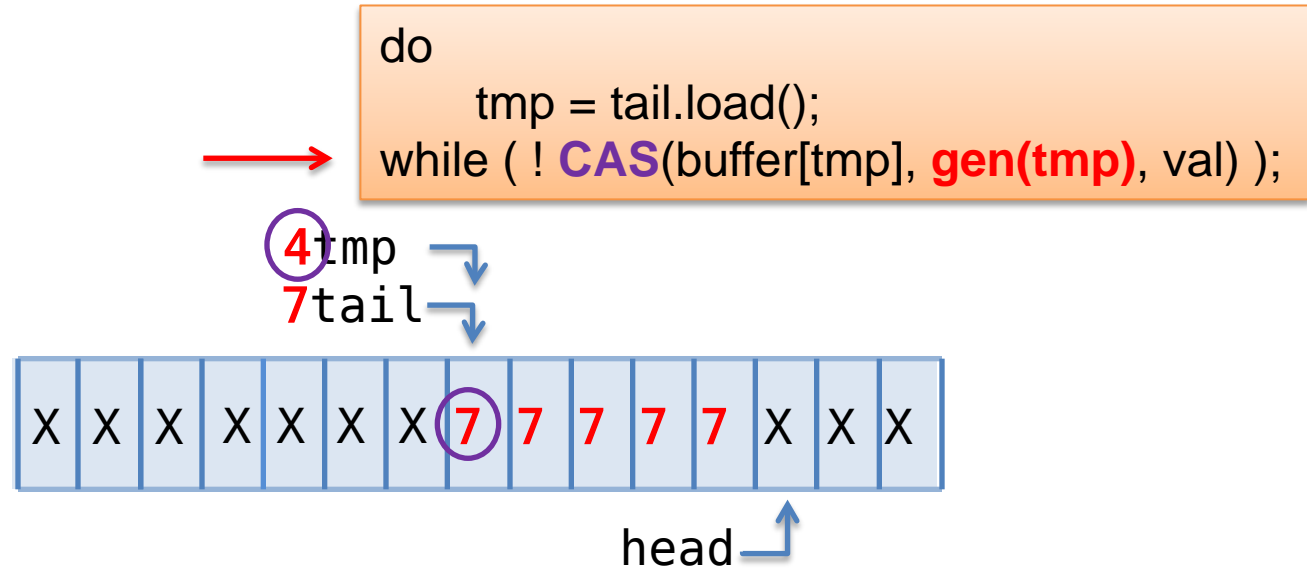
```
do
    tmp = tail.load();
while ( ! CAS(buffer[tmp], gen(tmp), val) );
```







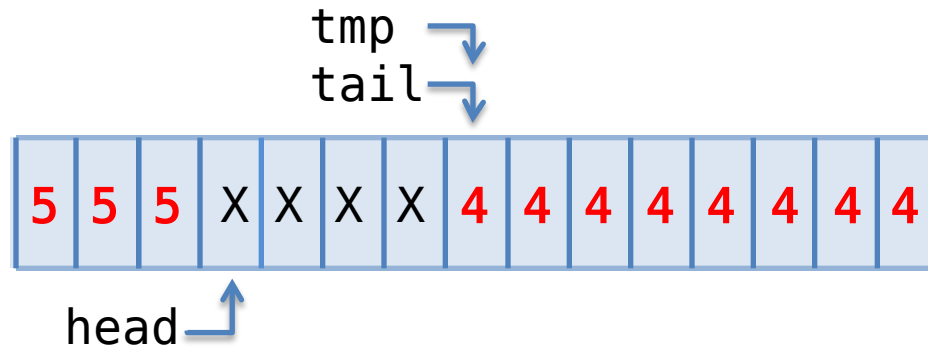




All states are valid states for all lines of code (*)



```
tmp = tail.load();  
while ( ! CAS(buffer[tmp], gen(tmp), val) );
```

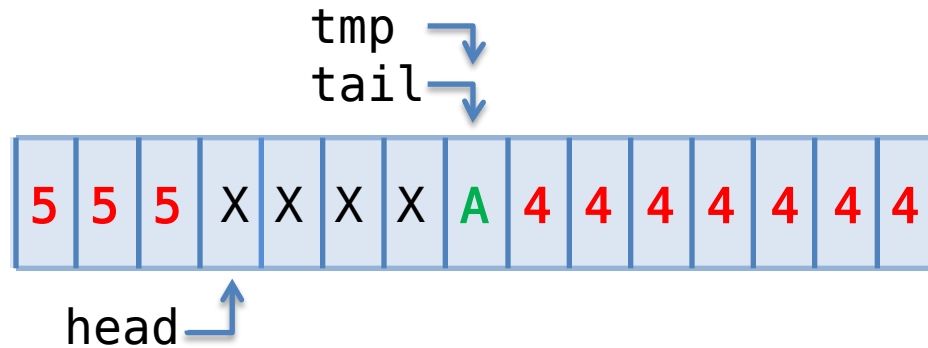




```
do
```

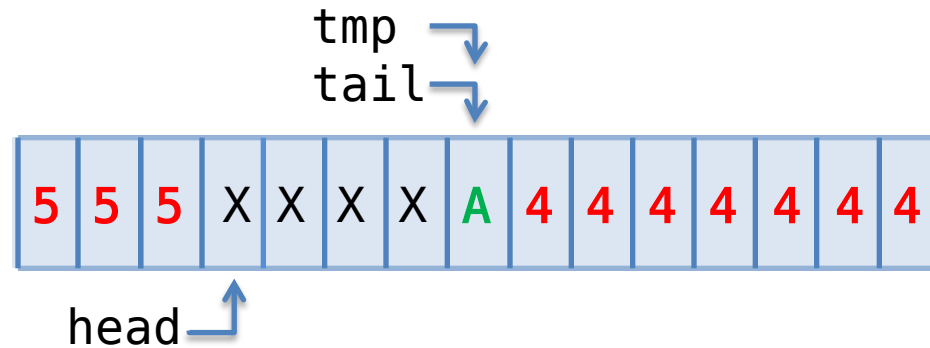
```
    tmp = tail.load();
```

```
    while ( ! CAS(buffer[tmp], gen(tmp), val) );
```





```
do
    tmp = tail.load();
    while ( ! CAS(buffer[tmp], gen(tmp), val) );
    tail++; ///???
```



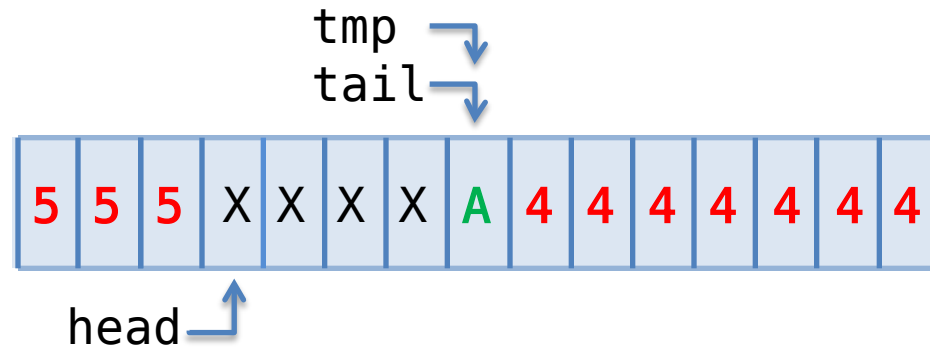


do

tmp = tail.load();

while (! **CAS**(buffer[tmp], gen(tmp), val));

tail++; **//???**





spinlock ?

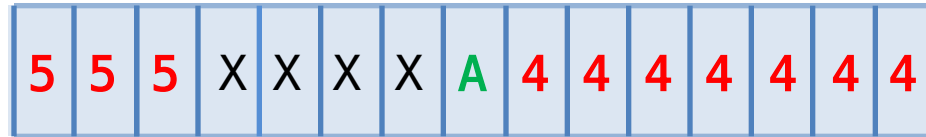
do

tmp = tail.load();

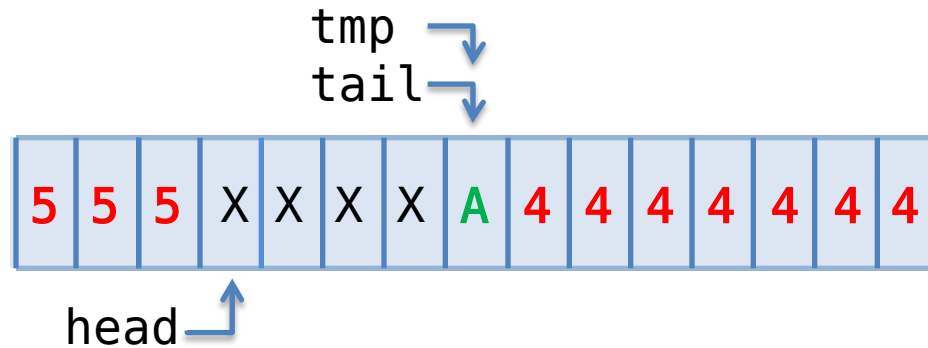
while (! **CAS**(buffer[tmp], gen(tmp), val));

tail++; **//???**

tmp
tail

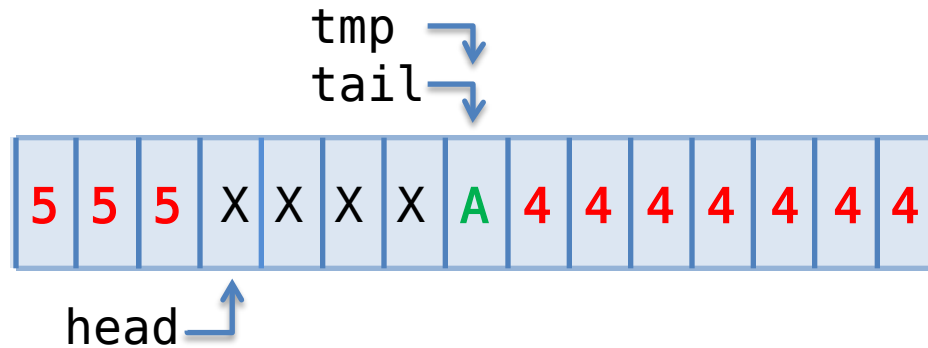


head





```
do {  
    tmp = tail.load();  
    while (buffer[tmp] != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
tail++; // yes!
```

same



```
do {  
    tmp = tail.load();  
    while (buffer[tmp] != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
tail++; // yes!
```

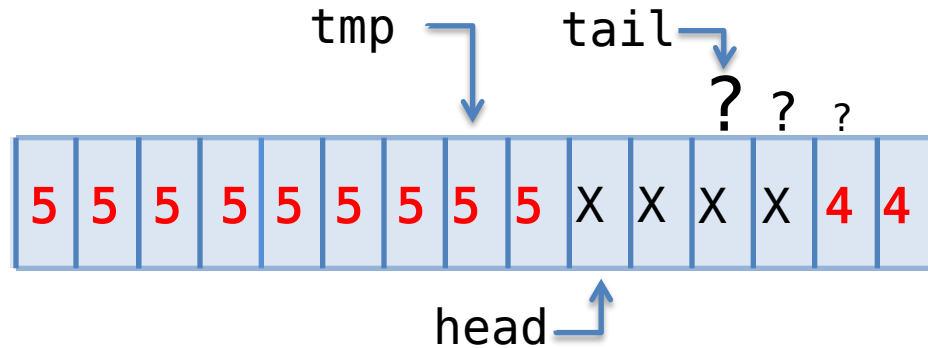
same

tmp  tail 

Sorry Herb...

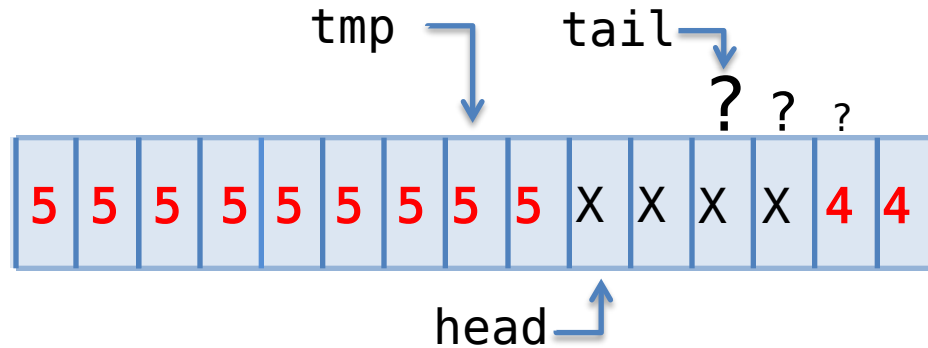


```
do {  
    tmp = tail.load(memory_order_relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
tail++; // yes!
```



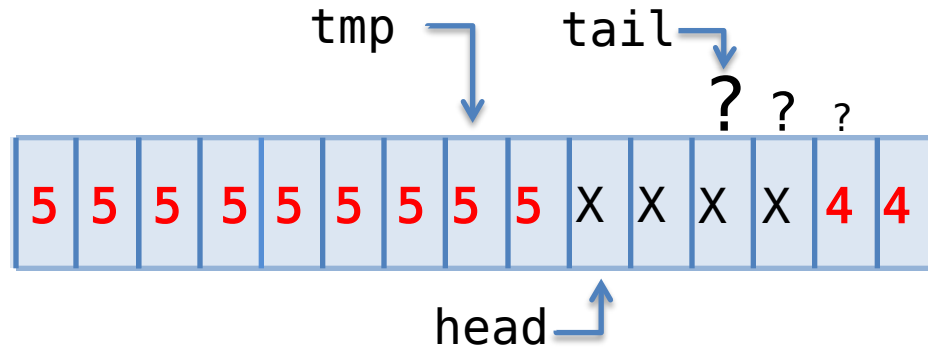


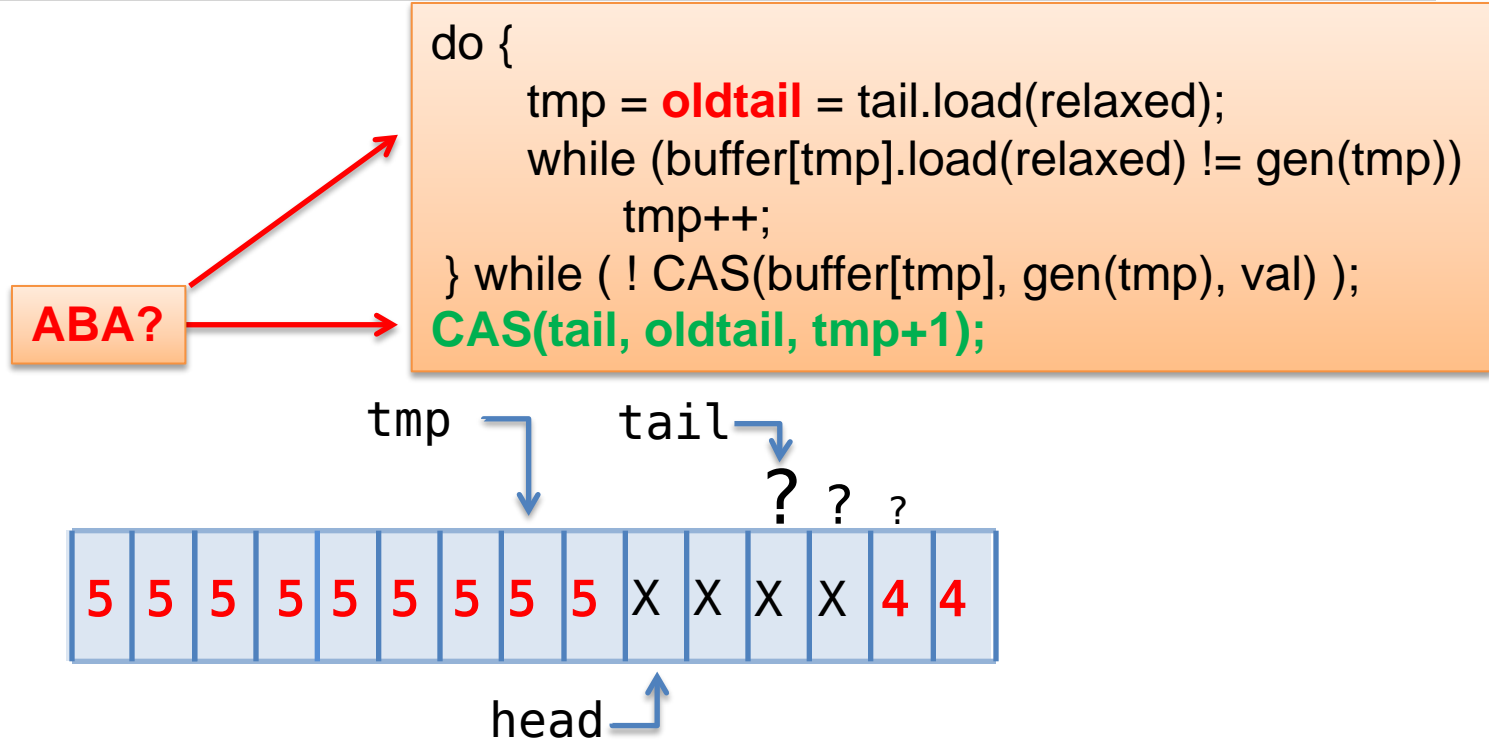
```
do {  
    tmp = tail.load(memory_order_relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
tail = tmp + 1;
```





```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



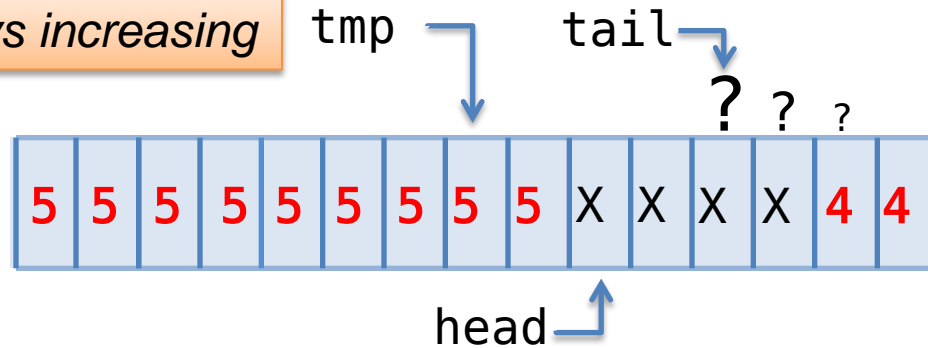




```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
    } while ( ! CAS(buffer[tmp], gen(tmp), val) );  
    CAS(tail, oldtail, tmp+1);
```

ABA?

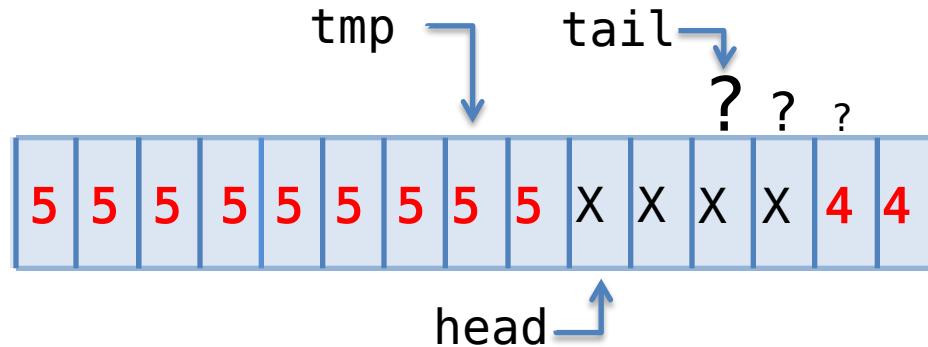
ensure tail is always increasing





```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

Is tail up to date “now”? →





```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

Is tail up to date “now”? →

tmp = tail →
? ? ?



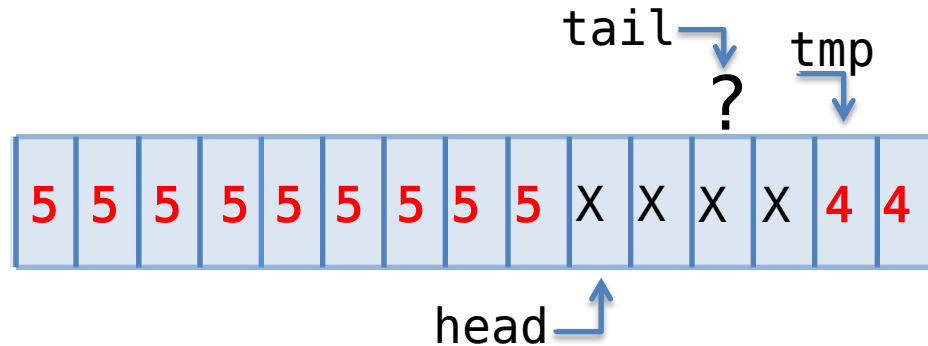
head ↑



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



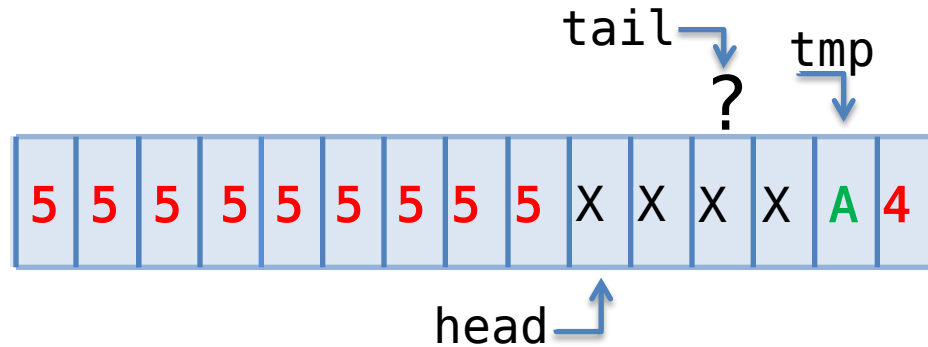
Is tail up to date “now”? →





```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

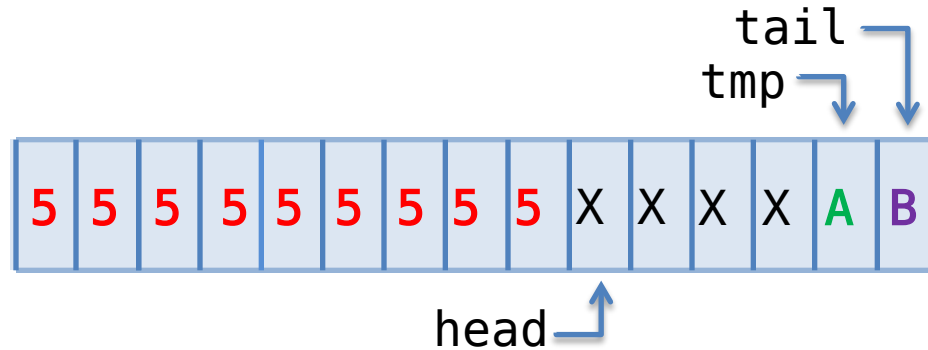
Is tail up to date “now”? →





```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

Is tail up to date “now”? 

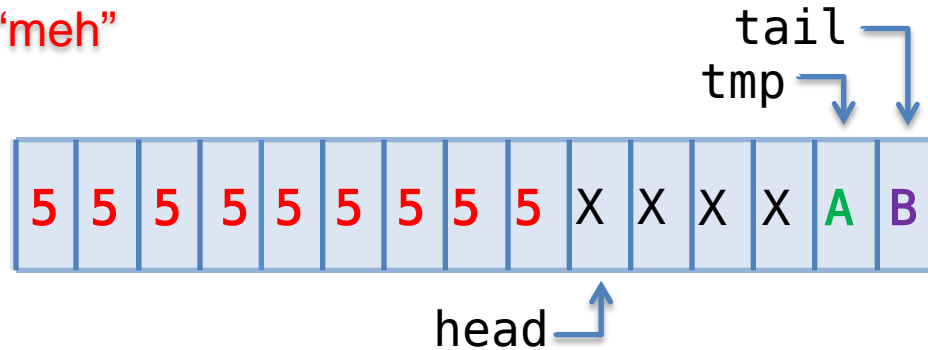




```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

Is tail up to date “now”?

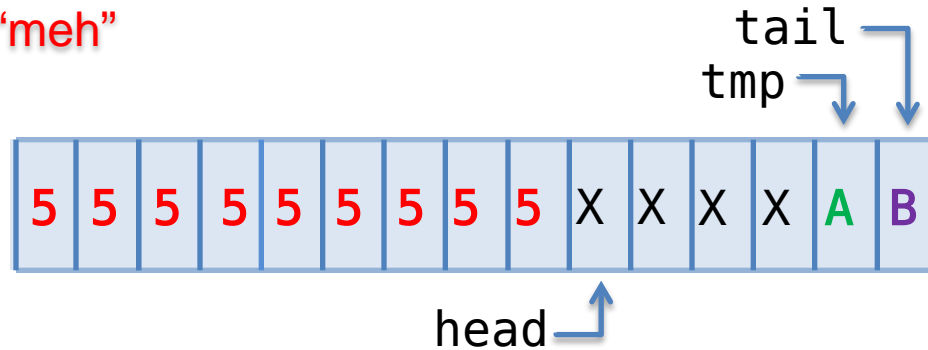
“meh”





```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1, relaxed);
```

Is tail up to date “now”? 
“meh”

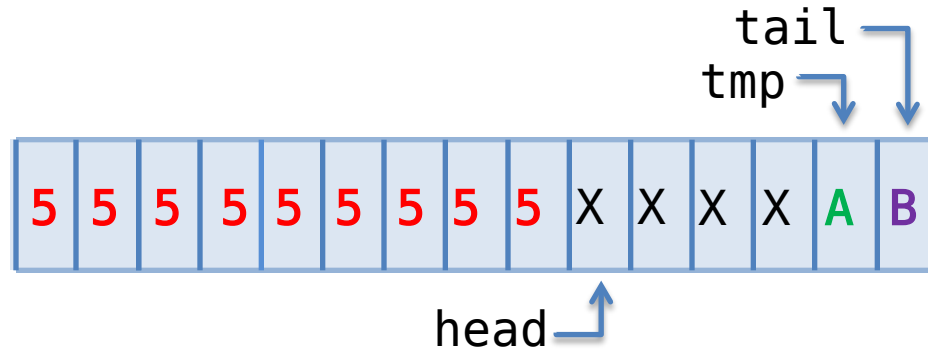




push(val)



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

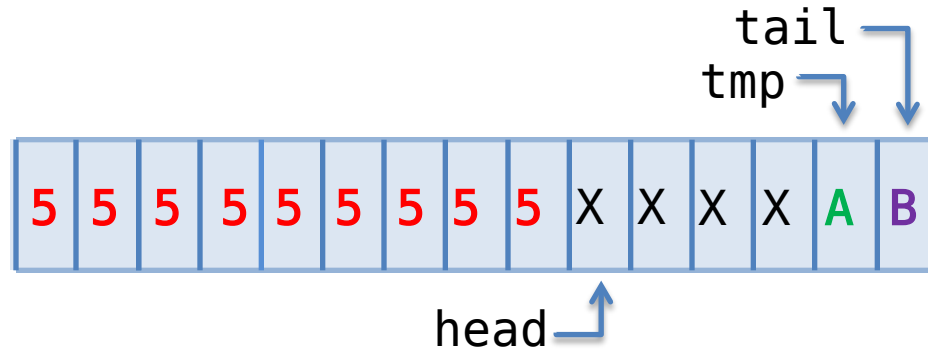




push(val)



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



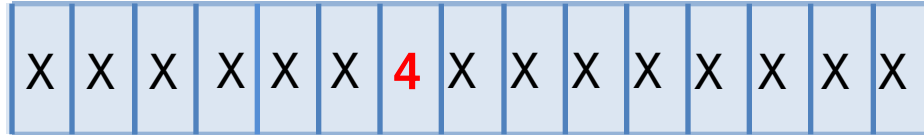
All states are valid states for all lines of code?



push(val)



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



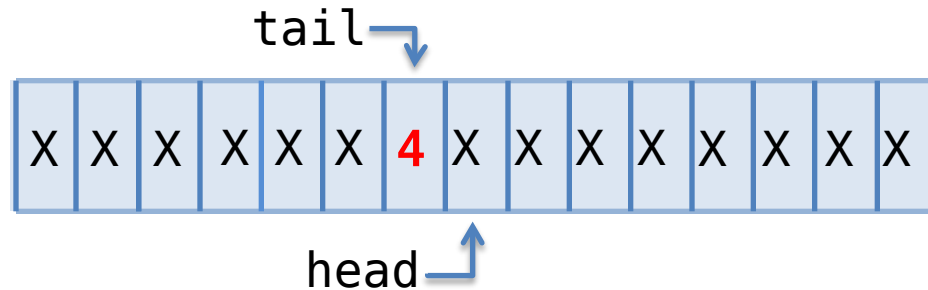
All states are valid states for all lines of code?



push(val)



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



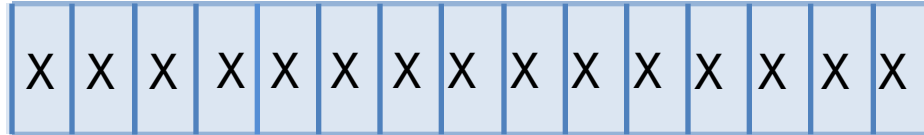
All states are valid states for all lines of code?



push(val)



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



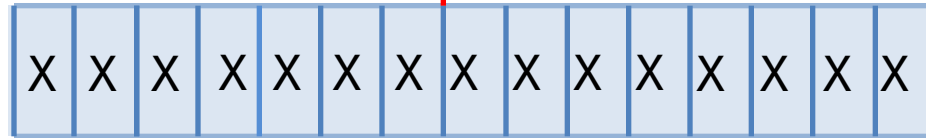
All states are valid states for all lines of code?



push(val)



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



head

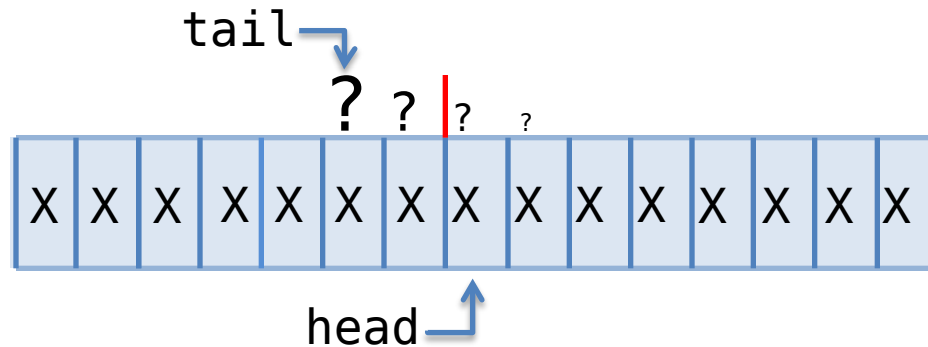
All states are valid states for all lines of code?



push(val)



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



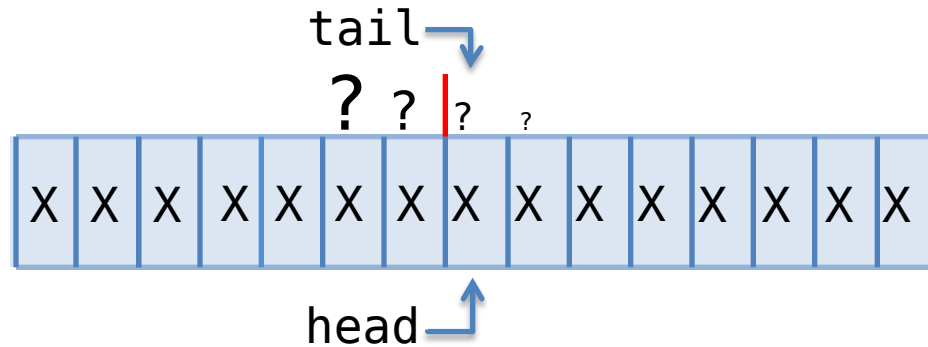
All states are valid states for all lines of code?



push(val)



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?



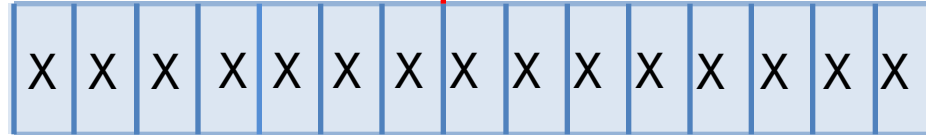
push(val)



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

tail

? ? | ? ?



All states are valid states for all lines of code?



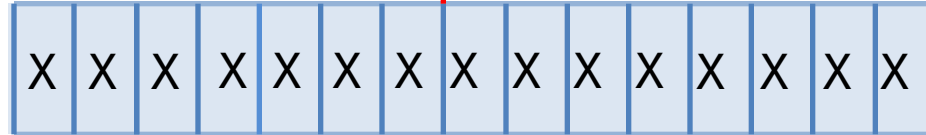
(worse?) spinlock ?



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

tail

? ? | ? ?



All states are valid states for all lines of code?

(worse?) spinlock ?



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

tail

Compromise...

All states are valid states for all lines of code?



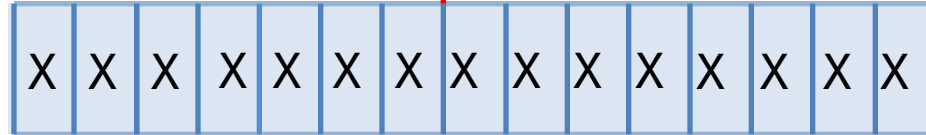
(worse?) spinlock ?
overflow ?



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

tail

? ? | ? ?



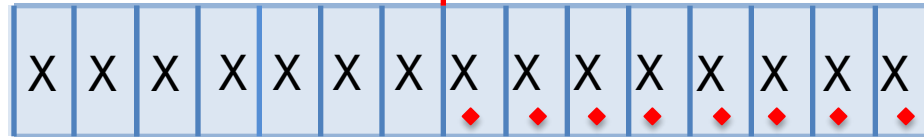
All states are valid states for all lines of code?



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    g = gen(tmp);  
    while ((b = buffer[tmp]) != g && odd(g)==odd(b))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val | odd(gen(tmp))) );  
CAS(tail, oldtail, tmp+1);
```

4tail

? ? | ? ?



All states are valid states for all lines of code?

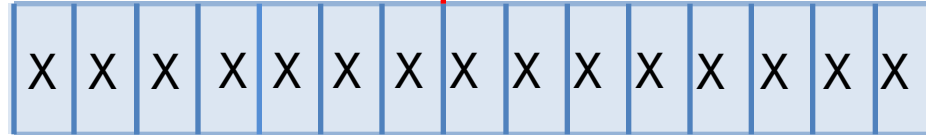


spinlock on full ?

```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp] != gen(tmp) && tmp - oldtail < size)  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

4tail

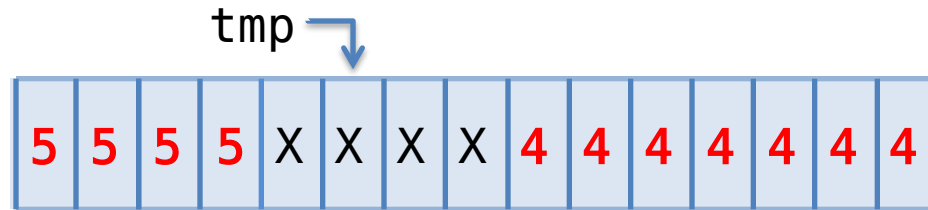
? ? | ? ?



All states are valid states for all lines of code?



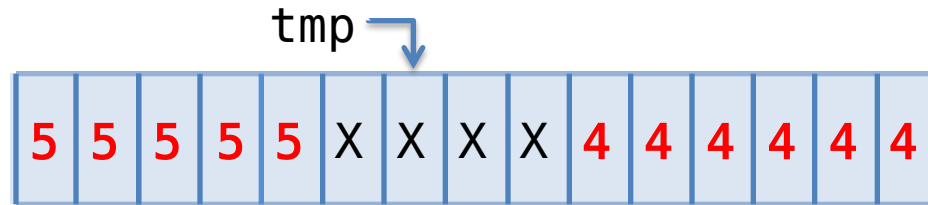
```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp] != gen(tmp) && tmp - oldtail < size)  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?



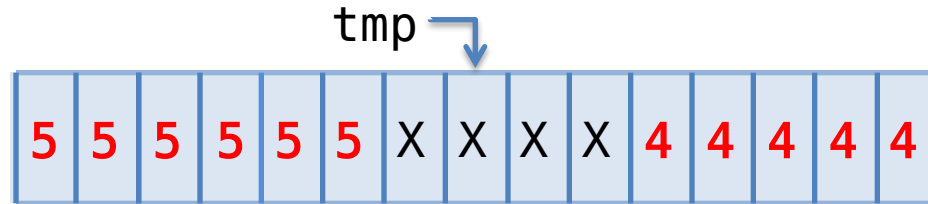
```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp] != gen(tmp) && tmp - oldtail < size)  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?



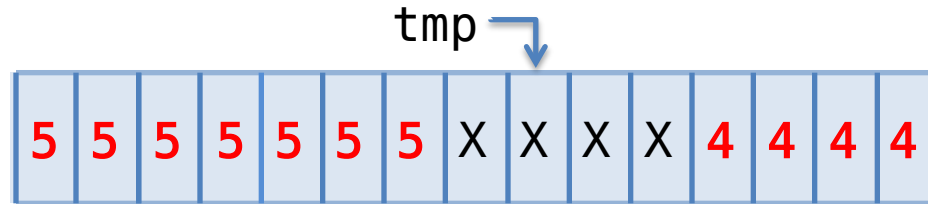
```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp] != gen(tmp) && tmp - oldtail < size)  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?



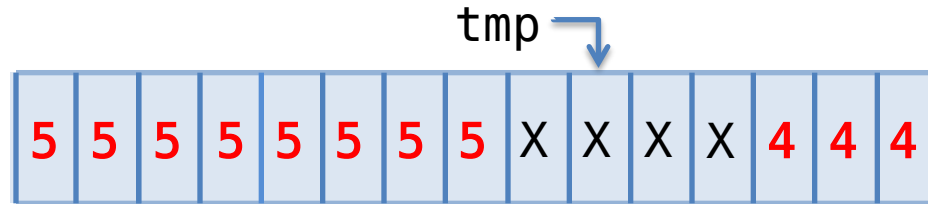
```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp] != gen(tmp) && tmp - oldtail < size)  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp] != gen(tmp) && tmp - oldtail < size)  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

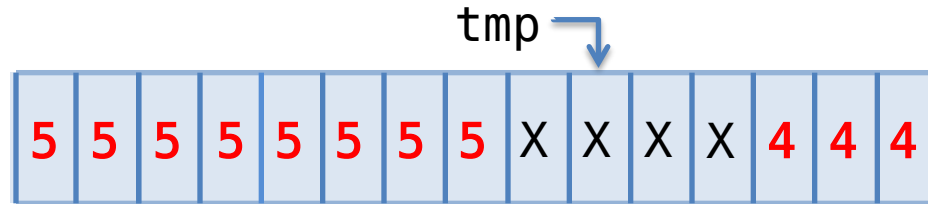


All states are valid states for all lines of code?



spinlock **NOT** full ?

```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp] != gen(tmp) && tmp - oldtail < size)  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?

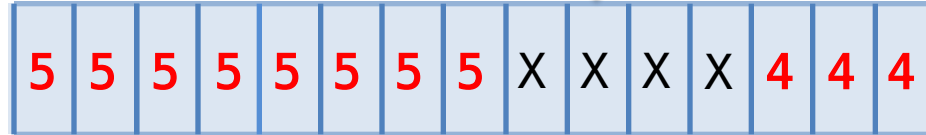


“fullish”



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    tmp = find_tail(tmp, &oldtail);  
    if (tmp == FULL) ...??;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

tmp



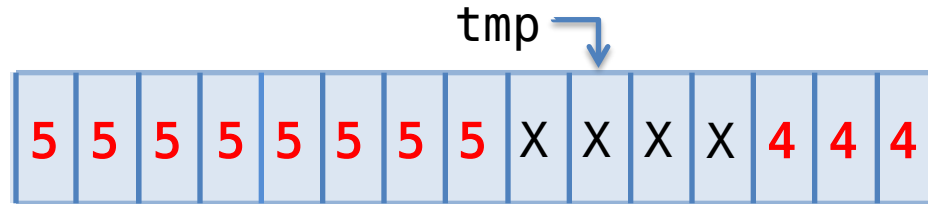
All states are valid states for all lines of code?



```
if (some_state)
{
    // still some_state???
    ...
}
```



```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```



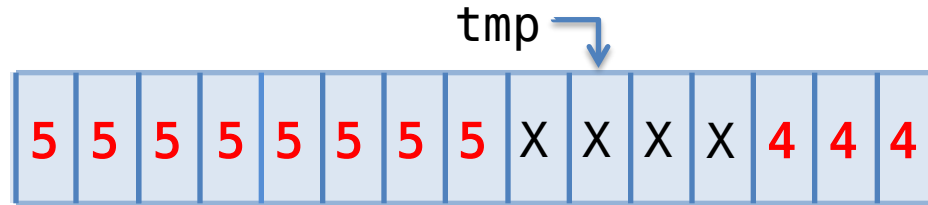
All states are valid states for all lines of code?



```
if (full)
{
    // still full???
    // or now empty?
    ...
}
```



```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```



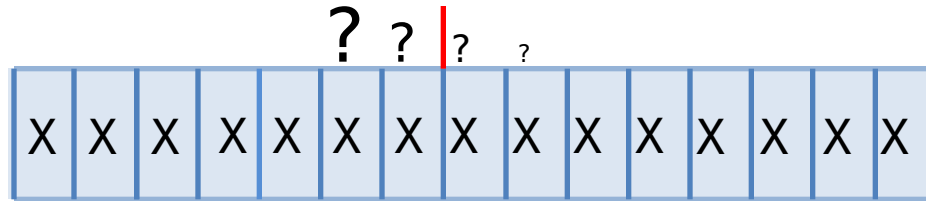
All states are valid states for all lines of code?



```
if (full)
{
    // still full???
    // or now empty?
    ...
}
```



```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```



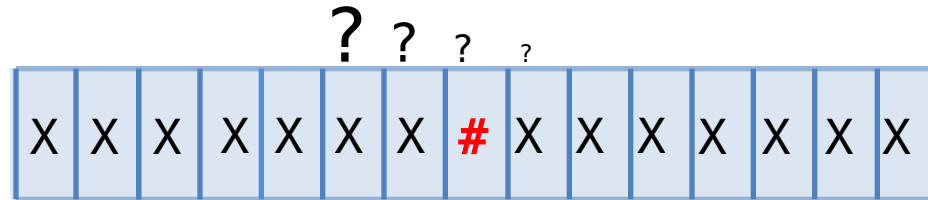
All states are valid states for all lines of code?



```
if (full)
{
    // still full???
    // or now empty?
    ...
}
```



```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```

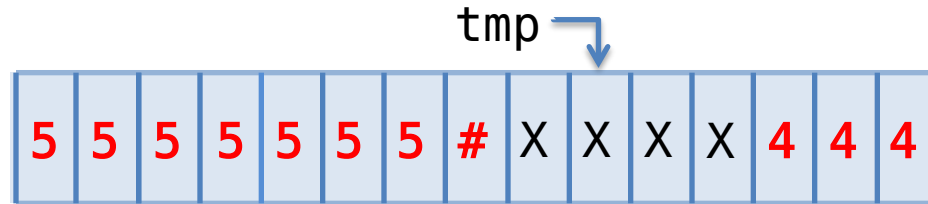


All states are valid states for all lines of code?



```
if (full)
{
    // still full???
    // or now empty?
    ...
}
```

```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```



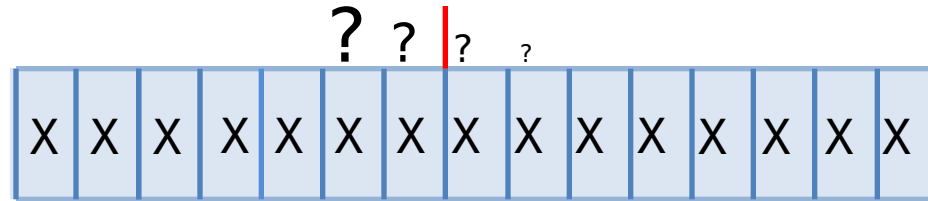
All states are valid states for all lines of code?



```
if (full)
{
    // still full???
    // or now empty?
    ...
}
```



```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```

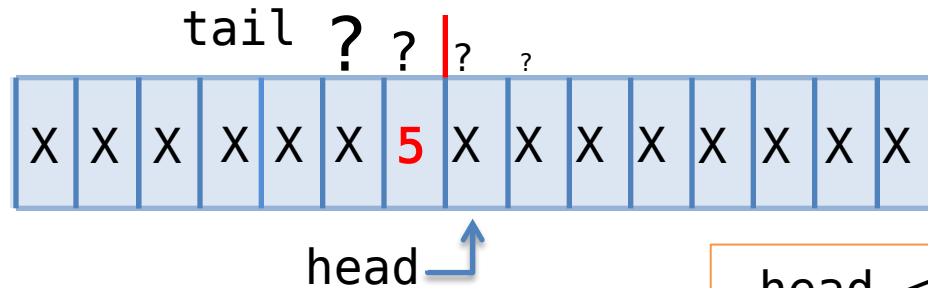


All states are valid states for all lines of code?



```
if (full)
{
    // still full???
    // or now empty?
    ...
}
```

```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```



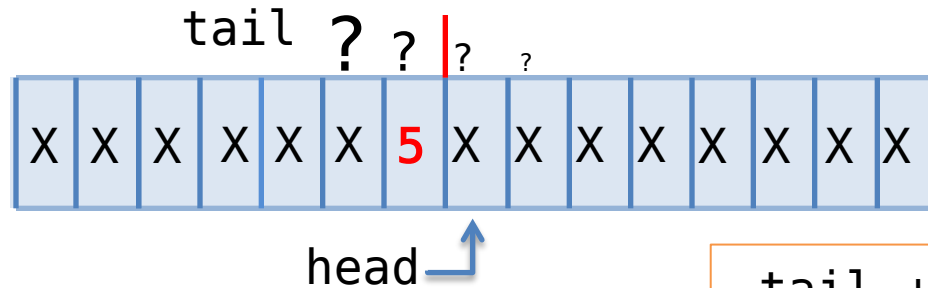
All states are valid states for all lines of code?

head < tail ?



```
if (full)
{
    // still full???
    // or now empty?
    ...
}
```

```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???.;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```



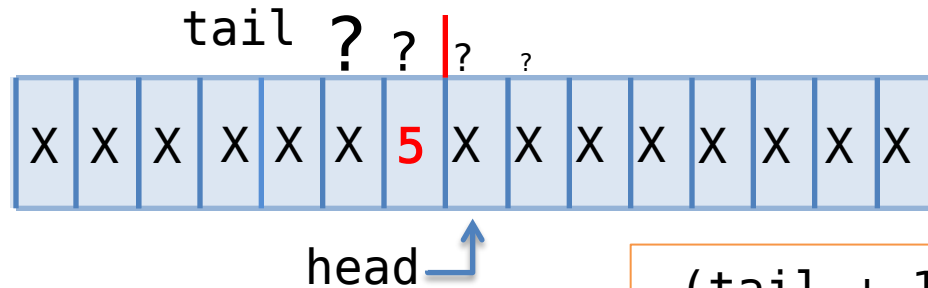
All states are valid states for all lines of code?

$\text{tail} + 1 \neq \text{head}?$



```
if (full)
{
    // still full???
    // or now empty?
    ...
}
```

```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```



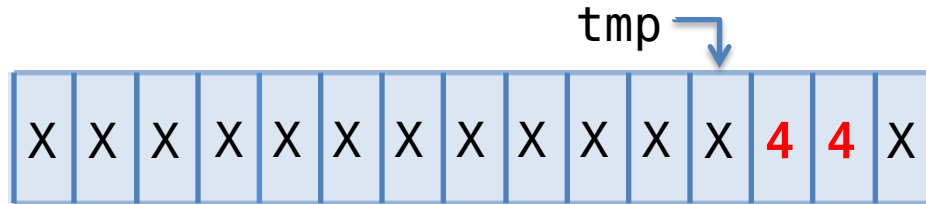
All states are valid states for all lines of code?

$(tail + 1) \% SZ \neq head \% SZ$?

“fullish”



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    tmp = find_tail(tmp, &oldtail);  
    if (tmp == FULL) ...???;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

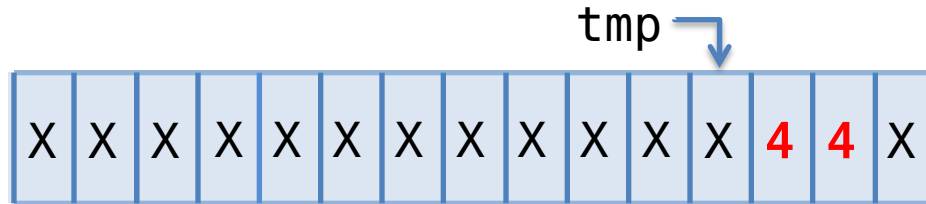


All states are valid states for all lines of code?

“fullish”



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    tmp = find_tail(tmp, &oldtail);  
    if (tmp == FULL) wait_for_space();  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



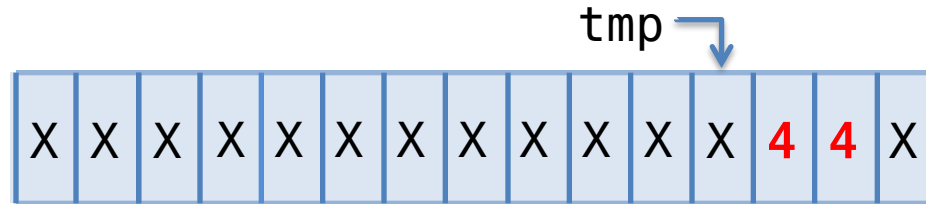
All states are valid states for all lines of code?



“fullish”



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    tmp = find_tail(tmp, &oldtail);  
    if (tmp == FULL) { wait_for_space(); continue;}  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

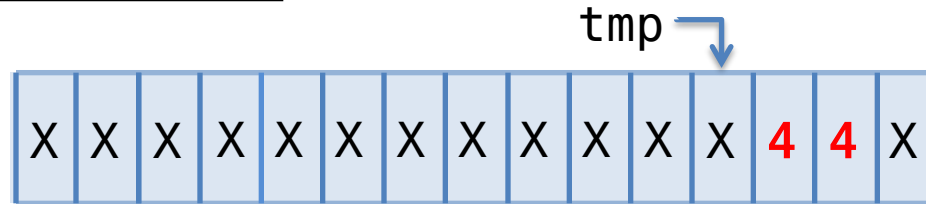


All states are valid states for all lines of code?



```
wait_for_space()
{
    unique_lock lock(mutex);
    while (still_fullish())
        cond_full.wait(lock);
}
```

```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) { wait_for_space(); continue; }
    while ( ! CAS(buffer[tmp], gen(tmp), va) );
    CAS(tail, oldtail, tmp+1);
}
```



All states are valid states for all lines of code?

Lock-free by Example

(one very complicated example)

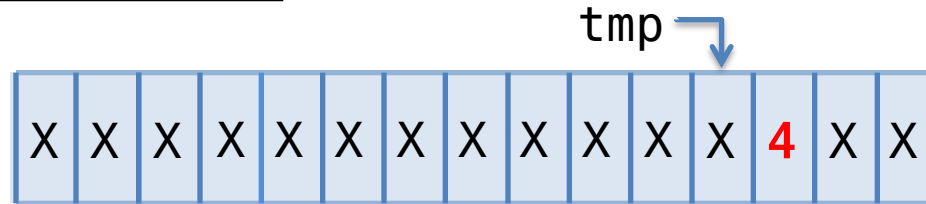
Tony Van Eerd

C++Now, 2015



```
{  
  unique_lock lock(mutex);  
  
  while (still_fullish())  
    cond_full.wait(lock);  
}
```

```
do {  
  tmp = oldtail = tail.load(relaxed);  
  tmp = find_tail(tmp, &oldtail);  
  if (tmp == FULL) { wait_for_space(); continue; }  
  } while ( ! CAS(buffer[tmp], gen(tmp), val) );  
  CAS(tail, oldtail, tmp+1);  
}
```

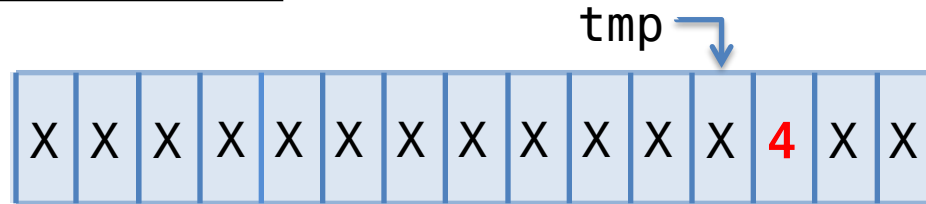


All states are valid states for all lines of code?



```
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```

```
do {  
    tmp = oldtail = tail.load(relaxed);  
    tmp = find_tail(tmp, &oldtail);  
    if (tmp == FULL) { wait_for_space(); continue;}  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

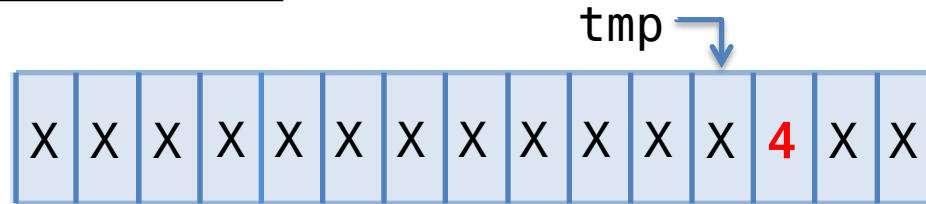


All states are valid states for all lines of code?

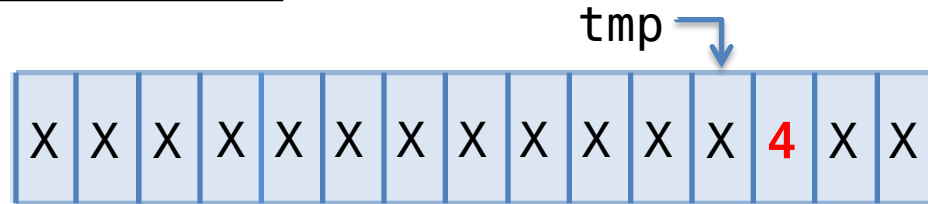
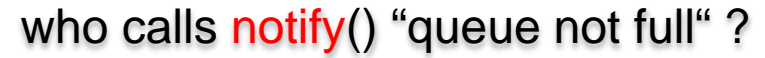


```
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```

```
do {  
    tmp = oldtail = tail.load(relaxed);  
    tmp = find_tail(tmp, &oldtail);  
    if(tmp == FULL)wait_for_space(&tmp,&oldtail);  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?



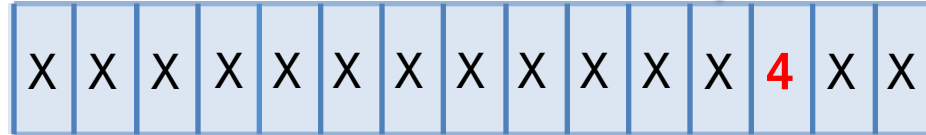


```
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```



who calls **notify()** “queue not full” ?

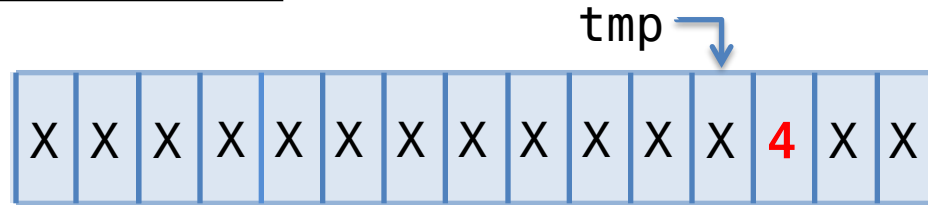
tmp ↘



```
int pop() {  
    ...  
    cond_full.notify();  
}
```



```
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```



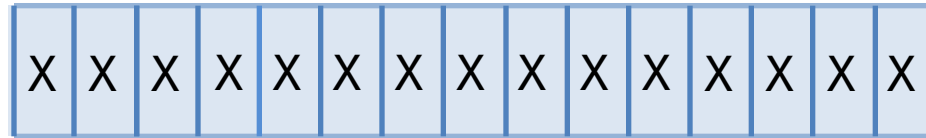
```
int pop() {  
    ...  
    cond_full.notify();  
}
```



```
int pop() {  
    ...  
    unique_lock lock(mutex);  
    cond_full.notify();  
}
```



```
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```



```
int pop() {  
    ...  
    cond_full.notify();  
}
```



```
int pop() {  
    ...  
    unique_lock lock(mutex);  
    cond_full.notify();  
}
```



```
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```



```
int pop() {  
    ...  
    cond_full.notify();  
}
```



```
int pop() {  
    ...  
    unique_lock lock(mutex);  
    cond_full.notify();  
}
```

Lock-free by Example

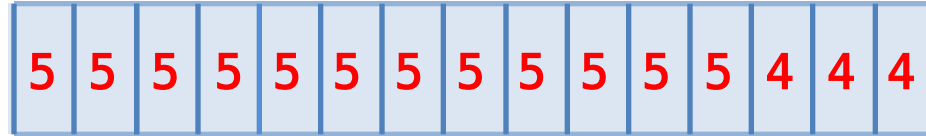
(one very complicated example)

Tony Van Eerd

C++Now, 2015



```
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```



```
int pop() {  
    ...  
    cond_full.notify();  
}
```

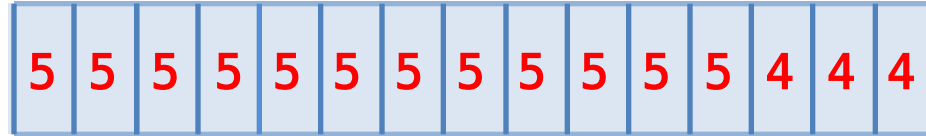


```
int pop() {  
    ...  
    unique_lock lock(mutex);  
    cond_full.notify();  
}
```





```
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```



```
int pop() {  
    ...  
    cond_full.notify();  
}
```



```
int pop() {  
    ...  
    unique_lock lock(mutex);  
    cond_full.notify();  
}
```



```
waiting = true;
{
    unique_lock lock(mutex);

    while ( ! ...find_tail... )
        cond_full.wait(lock);
}
```

I'm
waiting!



```
int pop() {
    ...
    cond_full.notify();
}
```



```
int pop() {
    ...
    unique_lock lock(mutex);
    cond_full.notify();
}
```



```
waiting = true;
{
    unique_lock lock(mutex);
    while ( ! ...find_tail... )
        cond_full.wait(lock);
}
```

I'm
waiting!

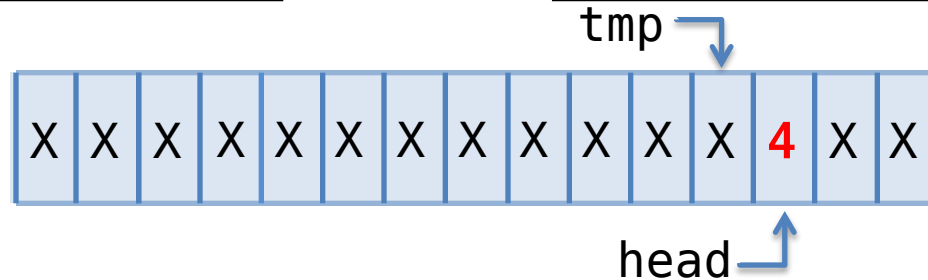
```
int pop() {
    ...
    unique_lock lock(mutex);
    cond_full.notify();
}
```





I'm waiting!

```
int pop() {
    ...
    if (waiting) {
        unique_lock lock(mutex);
        cond_full.notify();
    }
}
```

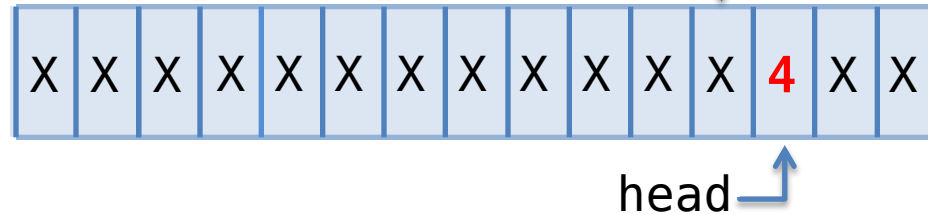




```
waiting = true;
{
    unique_lock lock(mutex);
    while ( ! ...find_tail... )
        cond_full.wait(lock);
}
waiting = false;
```

I'm
waiting!

```
int pop() {
    ...
    if (waiting) {
        unique_lock lock(mutex);
        cond_full.notify();
    }
}
```

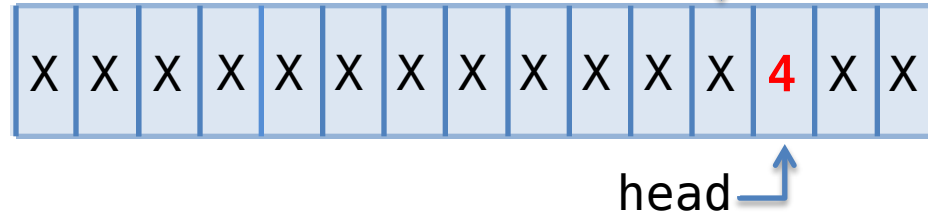




```
waiting++;  
{  
    unique_lock lock(mutex);  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}  
waiting--;
```

I'm
waiting!

```
int pop() {  
    ...  
    if (waiting) {  
        unique_lock lock(mutex);  
        cond_full.notify();  
    }  
}
```

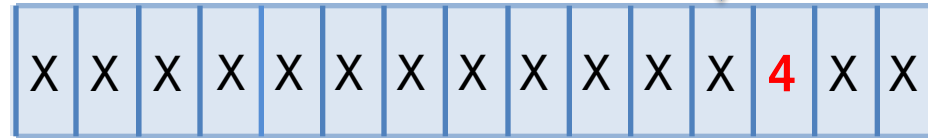




```
waiting++;  
{  
    unique_lock lock(mutex);  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}  
waiting--;
```

I'm
waiting!

```
int pop() {  
    ...  
    if (waiting) {  
        unique_lock lock(mutex);  
        cond_full.notify();  
    }  
}
```



tmp

head

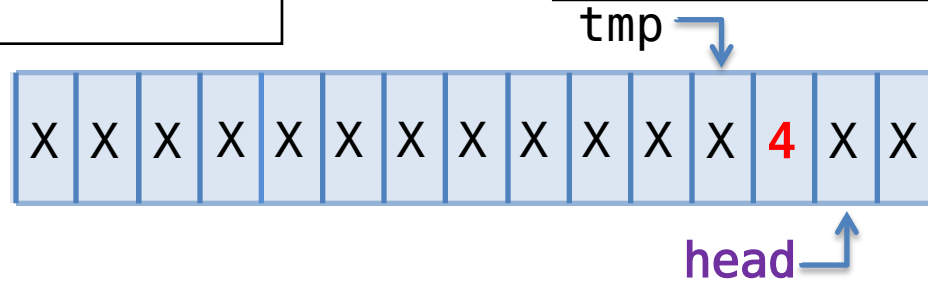
rarely

always



I'm waiting!

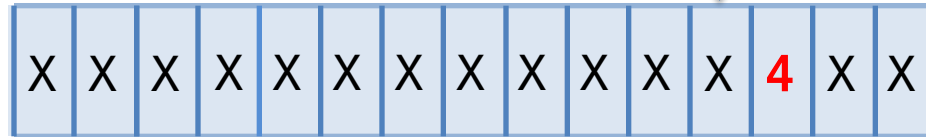
```
int pop() {
    ...CAS(head, oldhead, tmp+1);
    if (waiting) {
        unique_lock lock(mutex);
        cond_full.notify();
    }
}
```





```
{  
  unique_lock lock(mutex);  
  if (waiting++ == 0)  
    head.set_waitbit();  
  while ( ! ...find_tail... )  
    cond_full.wait(lock);  
  if (--waiting == 0)  
    head.clear_waitbit();  
}
```

```
int pop() {  
  ...CAS(head, oldhead, tmp+1);  
  if (oldhead.waitbit()) {  
    unique_lock lock(mutex);  
    cond_full.notify();  
  }  
}
```

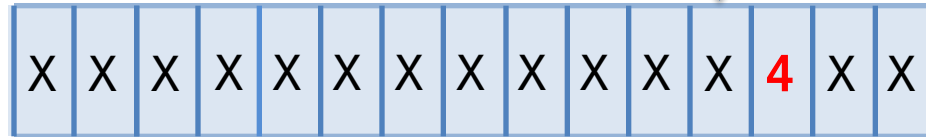


*head



```
{  
    unique_lock lock(mutex);  
    if (waiting++ == 0)  
        head.set_waitbit();  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
    if (--waiting == 0)  
        head.clear_waitbit();  
}
```

```
int pop() {  
    ...CAS(head, oldhead, tmp+1);  
    if (oldhead.waitbit()) {  
        unique_lock lock(mutex);  
        cond_full.notify();  
    }  
}
```

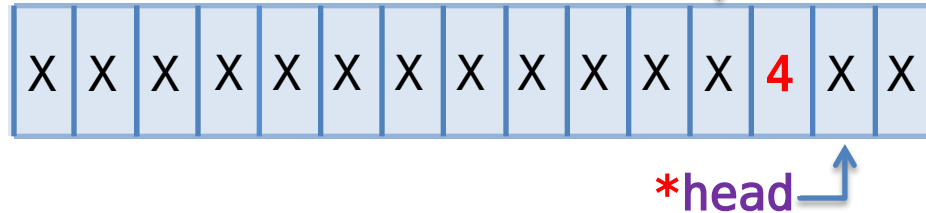


*head



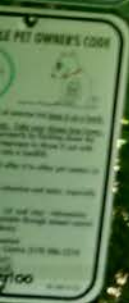
```
{  
  unique_lock lock(mutex);  
  if (waiting++ == 0)  
    head.set_waitbit();  
  while ( ! ...find_tail... )  
    cond_full.wait(lock);  
  if (--waiting == 0)  
    head.clear_waitbit();  
}
```

```
int pop() {  
  ...CAS(head, oldhead, tmp+1);  
  if (oldhead.waitbit()) {  
    unique_lock lock(mutex);  
    cond_full.notify();  
  }  
}
```



NOTE: **waiting** is NOT atomic







Looking Back



Looking Back

`push()`



Looking Ahead



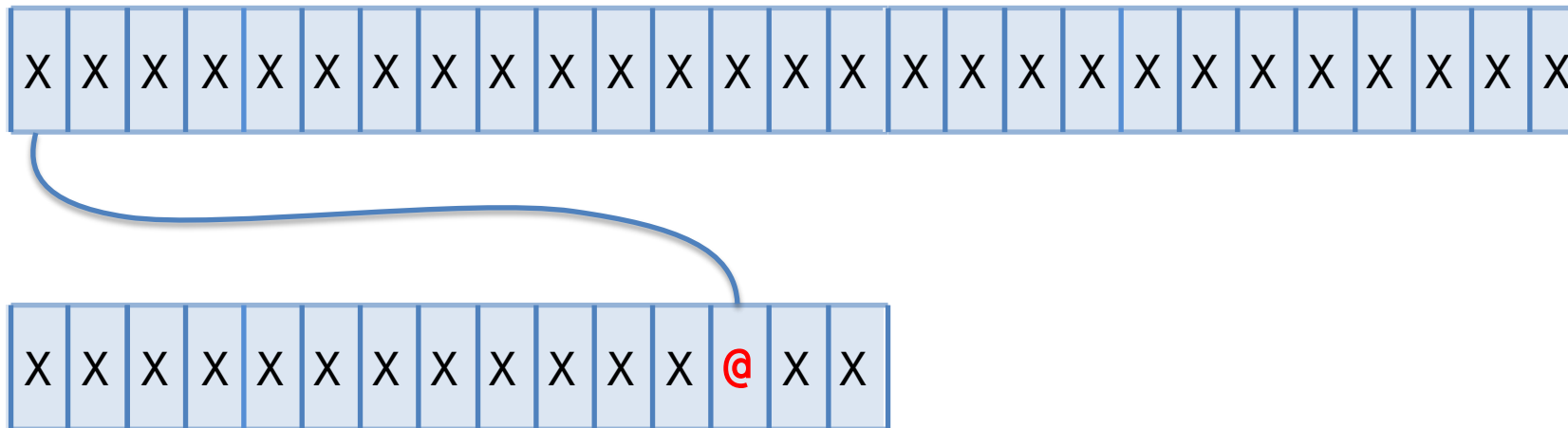
X	X	X	X	X	X	X	X	X	X	X	X	4	X	X
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

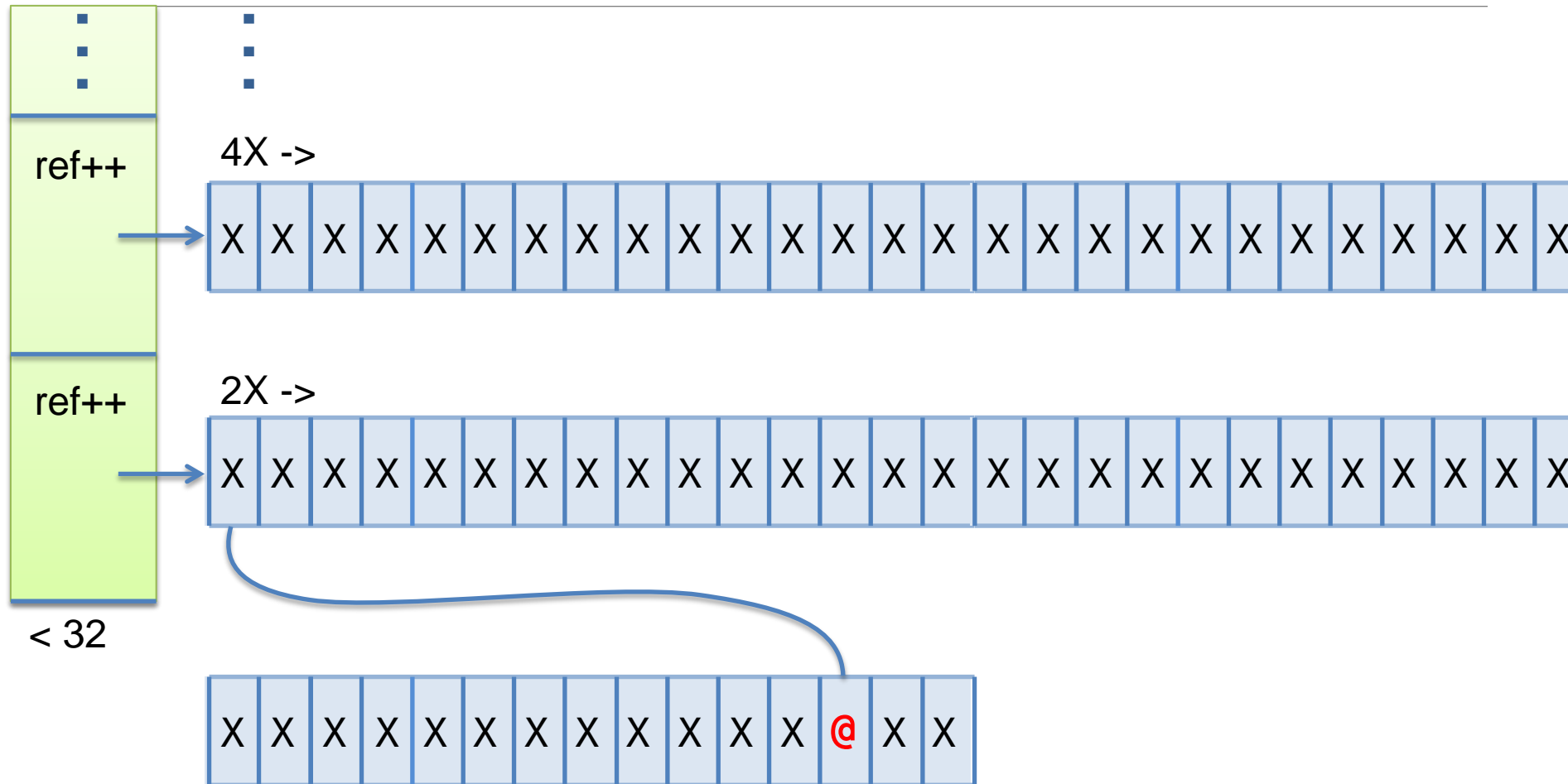


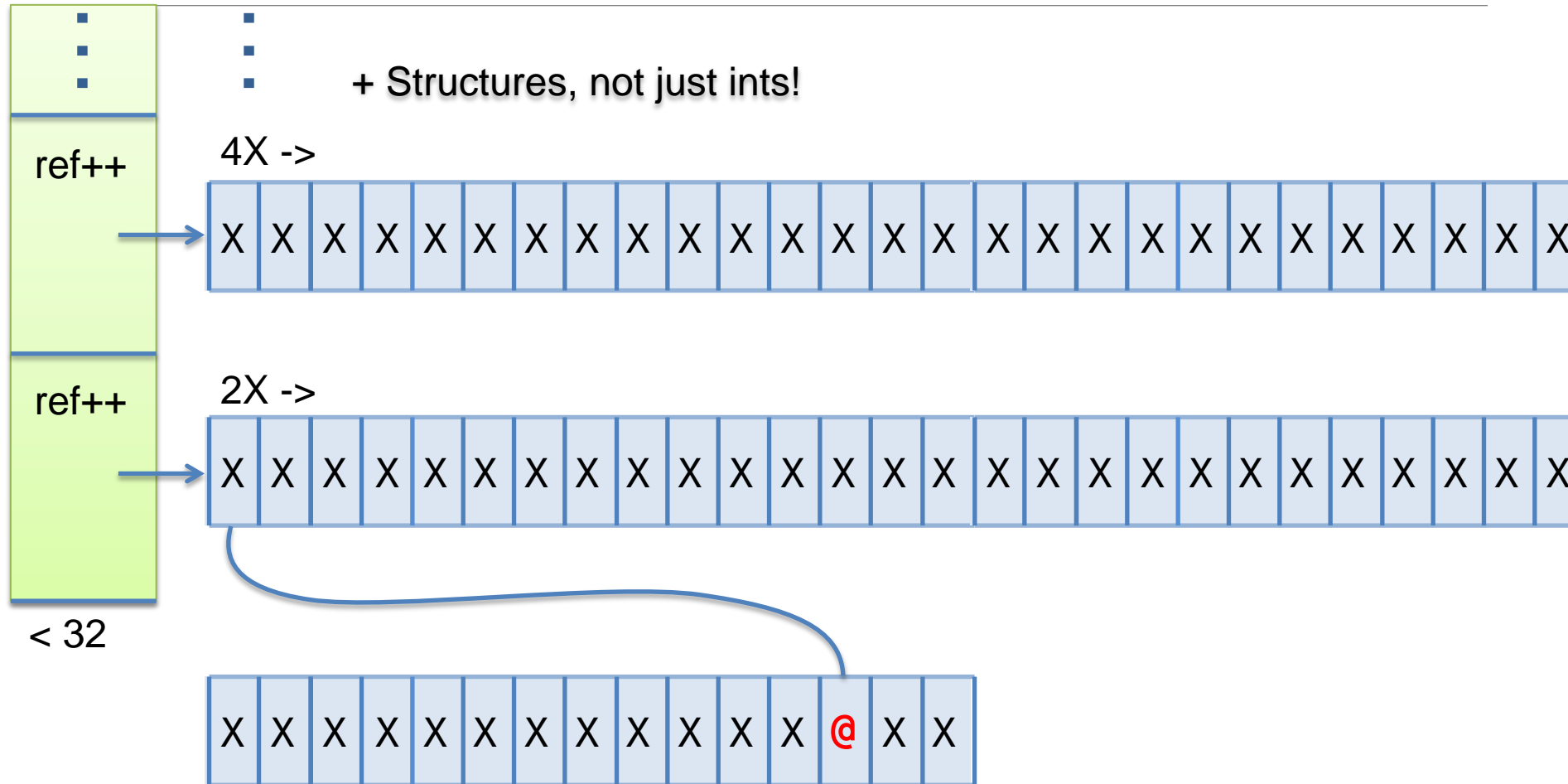
X	X	X	X	X	X	X	X	X	X	X	X	4	X	X
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---



2X ->

















“The Problem with Threads”

<http://ptolemy.eecs.berkeley.edu/>

<http://ptolemy.eecs.berkeley.edu/publications/papers/06/problemwithThreads/>

“A part of the Ptolemy Project experiment was to see whether **effective software engineering practices** could be developed for an academic research setting. We developed a process that included a code maturity rating system (with four levels, red, yellow, green, and blue), **design reviews, code reviews, nightly builds, regression tests**, and **automated code coverage metrics**. The portion of the kernel that ensured a consistent view of the program structure was written in early 2000, design reviewed to yellow, and code reviewed to green. The **reviewers included concurrency experts**, not just inexperienced graduate students (Christopher Hylands (now Brooks), Bart Kienhuis, John Reekie, and myself were all reviewers). We wrote **regression tests that achieved 100 percent code coverage**. The nightly build and regression tests ran on a two processor SMP machine, which exhibited different thread behavior than the development machines, which all had a single processor. The Ptolemy II **system** itself began to be **widely used**, and every use of the system exercised this code. **No problems were observed until the code **deadlocked** on April 26, 2004, four years later.**”



All states are valid states for all lines of code!